

# Physics of magnetically dominated plasma: dynamics, dissipation and particle acceleration

*Maxim Lyutikov (UBC)*

*Cracow, June 2006*

# Dynamics and energy dissipation in electromagnetically-dominated plasmas

*Maxim Lyutikov*  
(*McGill University, CITA*)

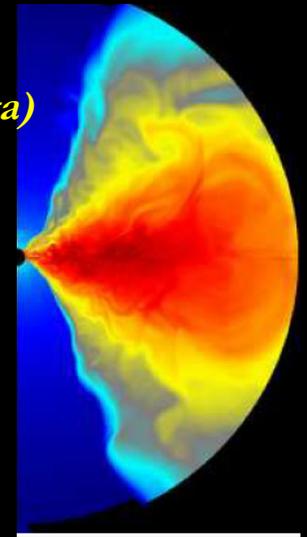
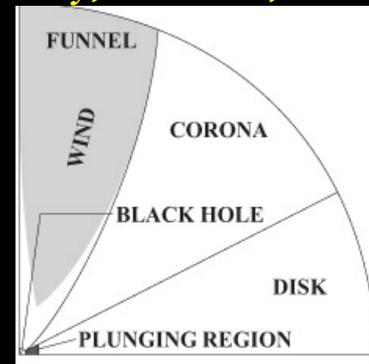
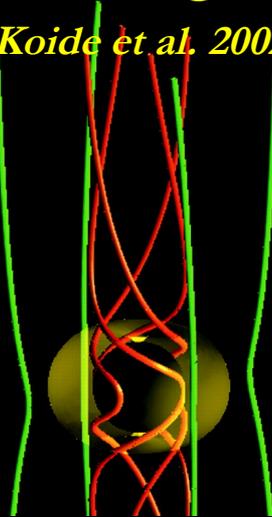
*Cracow, June 2003*

# Relativistic outflows may be produced and collimated by large scale B-fields

- *AGN jets: ergosphere and Black hole itself can act as a Faraday disk (Blandford-Znajek, Lovelace), creating B-field dominated jets*
- *Numerical simulations begin to show this dynamically*



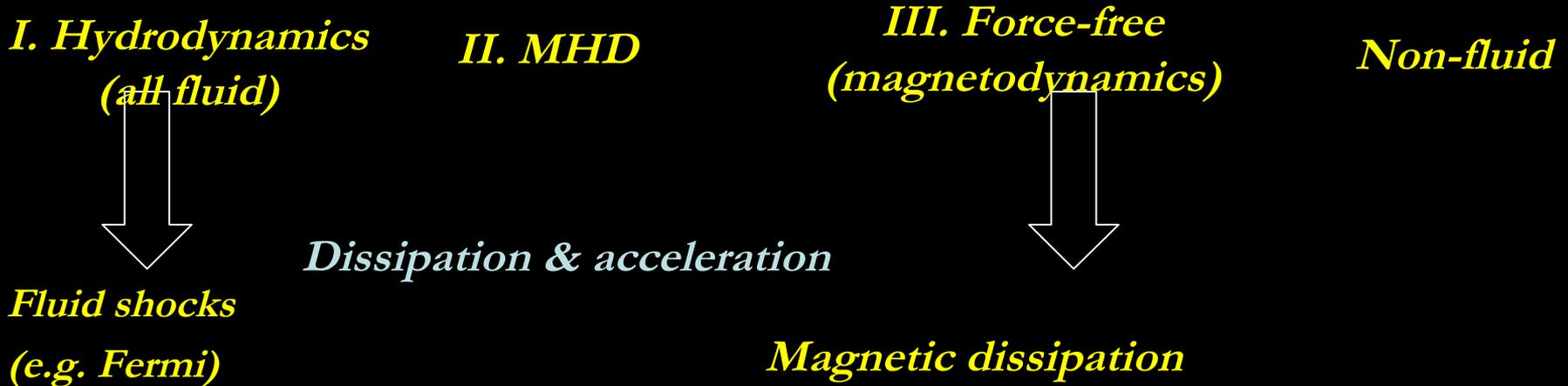
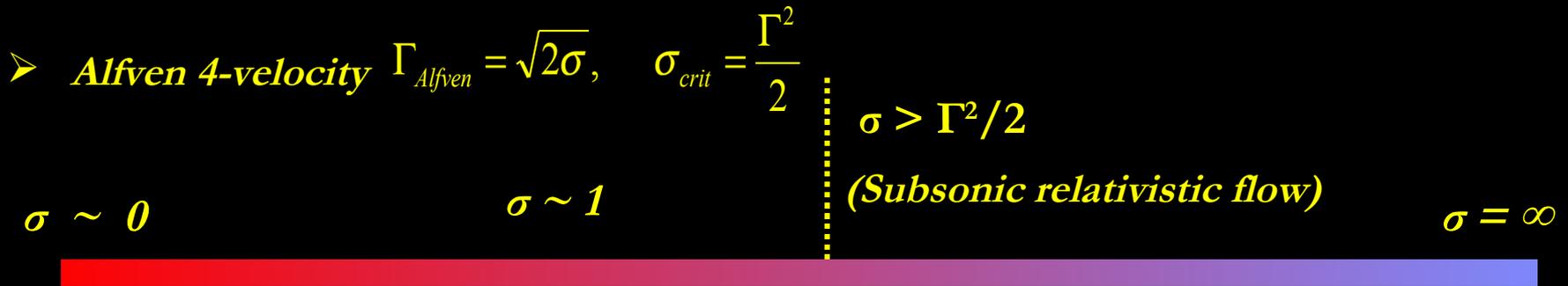
*(Koide et al. 2002), (McKinney, Gammie, Krolik, Proga)*



*Large scale, energetically dominant magnetic fields may be expected in the launching region of relativistic jets and may (should?) continue into emission regions*

# New plasma physics regime: magnetically dominated plasma

- *In plasma rest frame:*
  - *Magnetic energy*  $U'_B = B^2/8\pi$ ,
  - *Plasma energy: rest-mass,  $\rho c^2$*
- *Magnetization parameter*  $\sigma = \frac{U'_B}{U'_p} \Rightarrow \frac{B^2}{8\pi\rho c^2}$   
( $\sigma^{1/2} = \mu^{1/3}$ )
- *Magnetically dominated:  $\sigma > 1$*

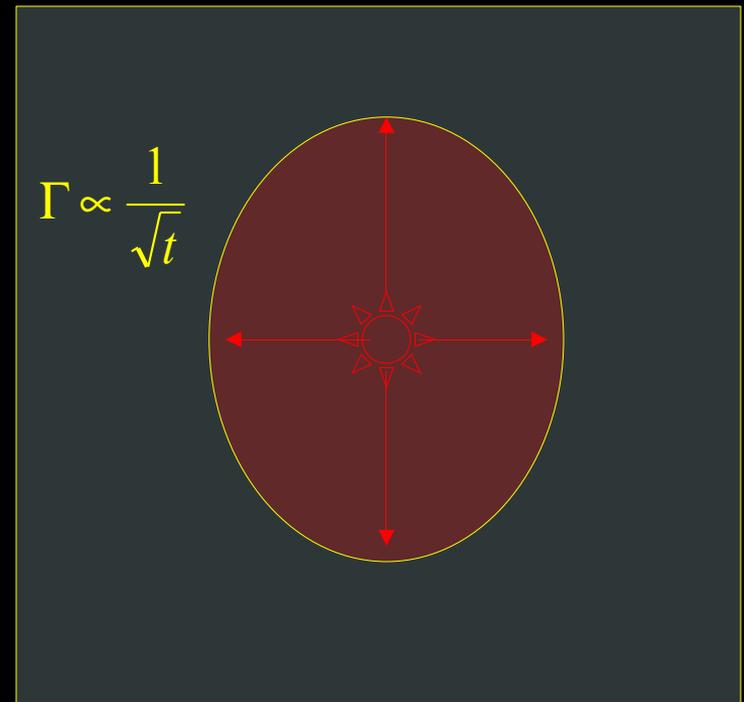
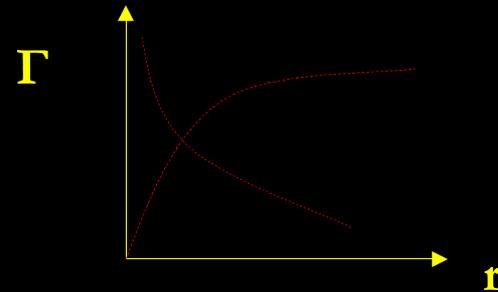


# Dynamics

# Expansion of $\sigma \gg 1$ wind

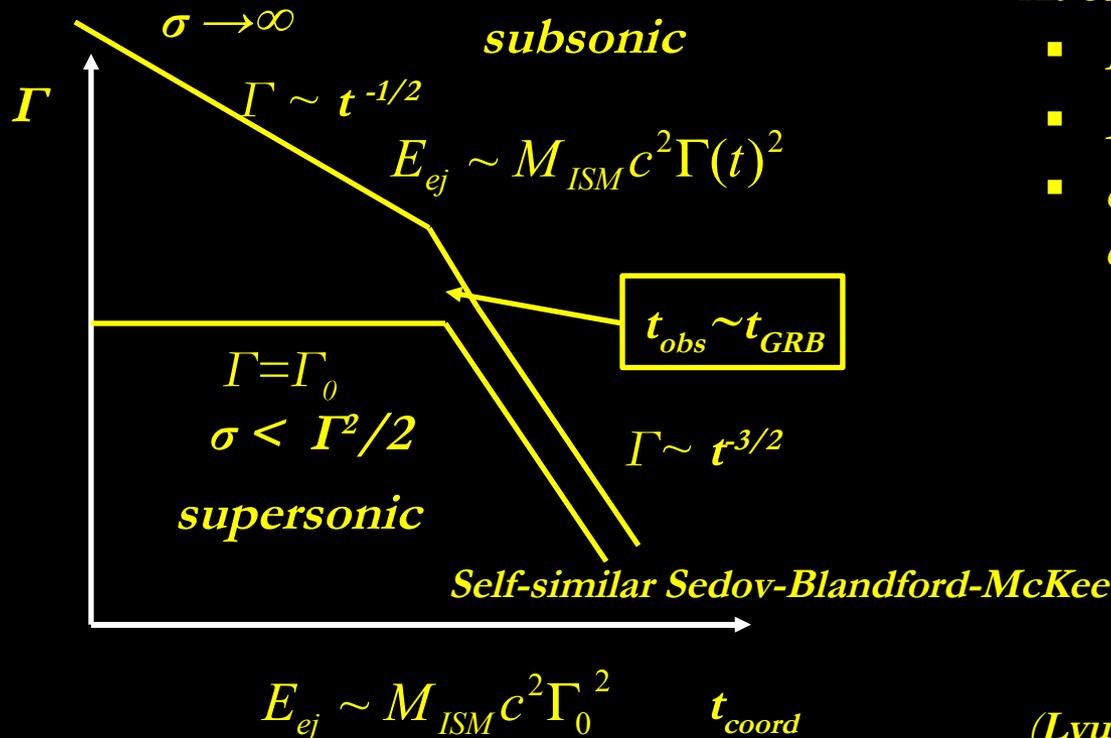
- *supersonic (MHD),  $\Gamma^2 > \sigma$ , in vacuum: flow acceleration determined by internal flow dynamics: flow passes through fast sonic points (eg  $\Gamma_F \sim \sqrt{\sigma}$ ), becomes causally disconnected (Michel)*
- *subsonic,  $\Gamma^2 < \sigma$ , : acceleration limited by external medium, causally connected flows*
  - *pressure balance at the contact*

$$\frac{L}{4\pi R^2 \Gamma^2 c} \sim \frac{B^2}{8\pi \Gamma^2} \sim \Gamma^2 \rho_{\text{ext}} c^2$$



# GRBs: $\sigma < \Gamma^2/2$ and $\sigma > \Gamma^2/2$ have different early dynamics

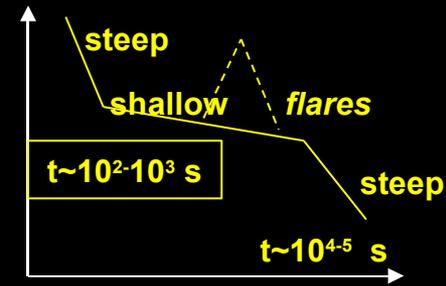
- $\sigma > \Gamma^2/2$  – subsonic flow
- $\sigma < \Gamma^2/2$  – supersonic flow (reached terminal  $\Gamma_0$ )



- At late times,  $t \gg t_{\text{GRB}}$  (self-similar), composition of ejecta is not important
- At early times:
  - MHD,  $\sigma < \Gamma^2/2$
  - Force-free  $\sigma > \Gamma^2/2$
  - $\sigma > 1$ : weak or no reverse shock emission

(Lyutikov 2003,2006)

# Observations?



- *Swift results are very puzzling:*

*flares and lightcurve breaks at  $t \sim 10 - 10^5$  sec*

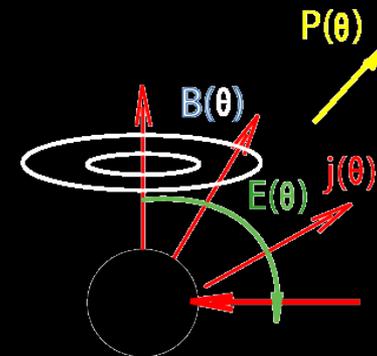
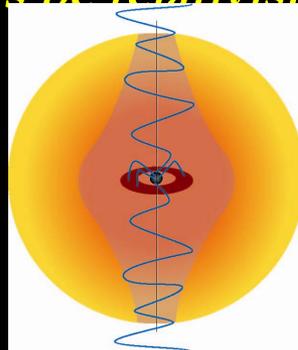
(Nousek; Zhang)

*(two “breaks” were expected,  $t_{GRB} \sim 100$  sec and @  $\Gamma \sim 1/\theta$ ,  $10^5$  sec)*

- *For  $\sigma < 1$  strong reverse shock emission is expected*
  - *For  $\sigma > 1$  no reverse shock is weak or non-existent*
- *Reverse shock in fireball: same type as internal shocks: microphysics is fixed by prompt emission*
  - *Expected optical flash  $m \sim 12-18$ .*
  - *Cooling: Flux  $\sim t^{-2}$ ; later: cooling to radio emission.*
- *In the Swift era absolute majority of GRBs do not show predicted RS behavior (despite UVOT and numerous robotic telescopes).*
- *This may indicate highly magnetized ejecta,  $\sigma > 1$* 
  - *Other possibilities to produce some optical emission (e.g.  $e^\pm$  by  $\gamma$ )*

# Long GRBs: expansion inside a star of a $\sigma > 1$ wind. As long as expansion is non-relativistic there **must** be dissipation

- *Energy and  $B_\varphi$ -flux is injected linearly with  $v \sim c$*
- *for non-relativistic expansion volume is near constant,  $B_\varphi \sim t$*
- *Energy  $\sim B_\varphi^2 \sim t^2$  ??? (c.f. Gunn & Rees PWNs)*
- *Need to destroy  $B_\varphi$  – flux: inductance break down  $\rightarrow$  dissipation*
- *Energy goes into  $e^\pm$ - $\gamma$  ( $\sim$  first 3 sec): lost after photosphere*
- *This is different from AGNs (c.f magnetic tower of Lynden-Bell), where expansion can always be relativistic, but not for GRBs*

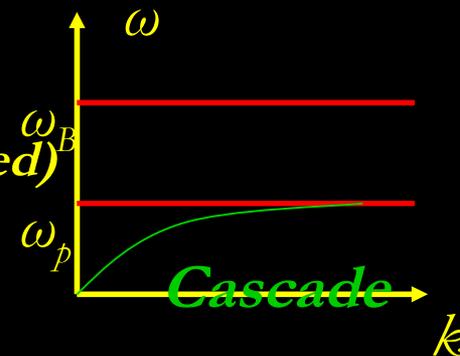
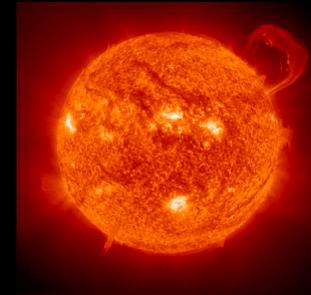


(Lyutikov & Blandford, 03)

# Dissipation in magnetically-dominated plasma

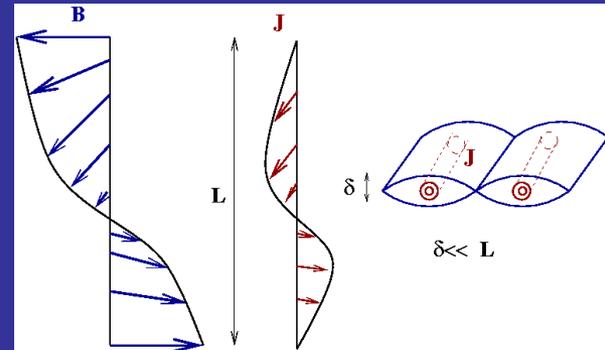
# Dissipation: $\sigma > 1$ – energy in B-field

- $\sigma > 1$ : shock are weak; do not exist for  $\sigma > \sigma_{crit}$
- **B-field dissipation due to current instabilities (“reconnection”)**
  - B-fields are strongly non-linear systems: dissipation property of the emission region, **NOT** of the source activity (e.g. Solar B-field generated on  $\sim 22$ yr time scales, flares can rise in minutes)
- $\sigma > 1$  – new plasma regime
  - Adopt non-relativistic schemes:
    - **Magnetodynamical tearing mode**
    - **Relativistic reconnection**
  - new acceleration schemes (no hydro or non-relativistic analogues)
    - **Charge-starved plasma, turbulent EM cascade**



# Resistive instability of relativistic force-free current layer (unsteady reconnection)

- Resistivity is usually very small ( $\tau_R \sim L^2/\eta \gg \tau$ )
- Current sheets are unstable – formation of small scale sub-sheets
- Tearing mode  $\tau \sim (\tau_A \tau_R)^{1/2}$   
 $\tau_A \sim L/v_A \sim L/c, \quad \tau_R \sim L^2/\eta$
- Similar to hydro (waves forms shocks) resistive RFF forms dissipative current layers
- Essential for RFF simulations, EM turbulent cascade



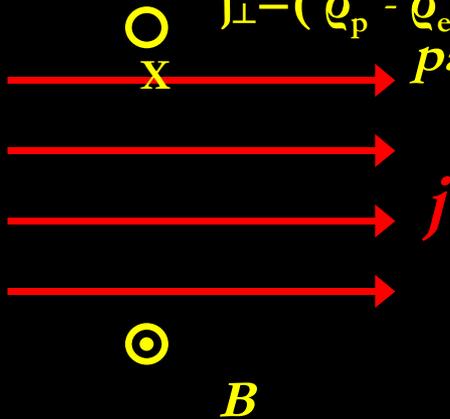
# Tearing mode in $\sigma=\infty$ plasma

- $\sigma = \infty$  : matter inertia is not important, force-free currents ensure  $\mathbf{J} \times \mathbf{B} + \rho_e \mathbf{E} = 0$  and decay resistively

$$\mathbf{j} = (\nabla \mathbf{E}) \frac{(\mathbf{E} \times \mathbf{B})}{B^2} + \frac{\mathbf{B} \cdot (\nabla \times \mathbf{B}) - \mathbf{E} \cdot (\nabla \times \mathbf{E})}{B^2} \mathbf{B}$$

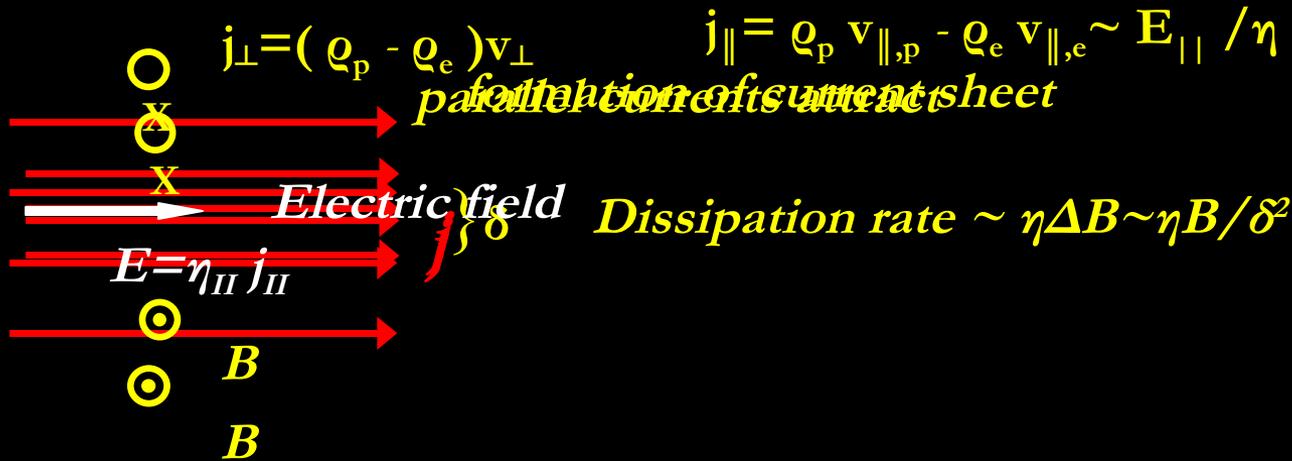
$$\mathbf{j}_\perp = (\rho_p - \rho_e) \mathbf{v}_\perp \quad \mathbf{j}_\parallel = \rho_p \mathbf{v}_{\parallel,p} - \rho_e \mathbf{v}_{\parallel,e} \sim \mathbf{E}_\parallel / \eta$$

*parallel currents attract*



# Tearing mode in $\sigma=\infty$ plasma

- $\sigma = \infty$  : matter inertia is not important, force-free currents ensure  $\mathbf{J} \times \mathbf{B} + \rho_e \mathbf{E} = 0$  and decay resistively



(Lyutikov 03)

- very fast

Resistive (tearing) EM instability

New plasma physics regime, same expression for growth rate?  
 (come from very different dynamical equations: Maxwell and MHD)

# Tearing mode in $\sigma=\infty$ plasma

➤ *slow motion in  $\sigma = \infty$  plasma*

$$\nabla \mathbf{B} = 0$$

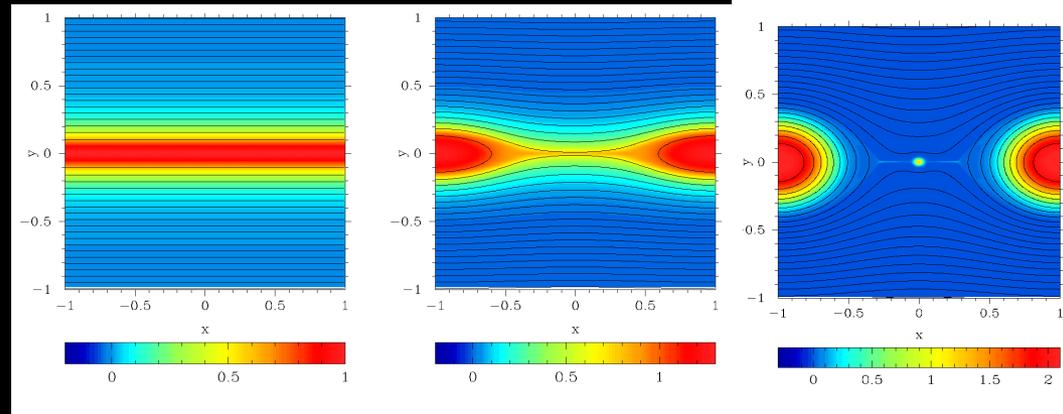
$$\partial_t \mathbf{B} - \nabla \times (\mathbf{V} \times \mathbf{B}) - \eta \Delta \mathbf{B} = 0$$

$$\partial_t \rho + \nabla \cdot (2\rho \mathbf{V}) = 0$$

$$\partial_t (\rho \mathbf{V}) + \nabla \cdot \left( g \frac{\mathbf{B}^2}{4\pi} - \frac{\mathbf{B} \otimes \mathbf{B}}{8\pi} \right) = 0$$

$$\rho = \frac{B^2}{8\pi c^2}, \quad \mathbf{V} = \frac{\mathbf{E} \times \mathbf{B}}{B^2} c$$

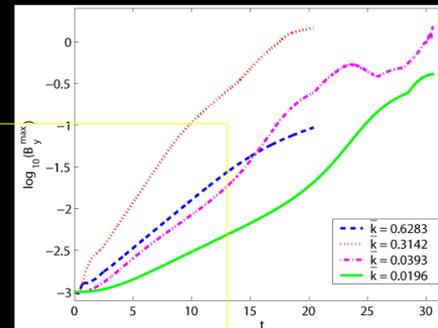
➤ *Non-linear stage: formation of magnetic islands*



very similar to incompressible MHD!

This may be a step towards formation of reconnection layers.

Applications: magnetars (growth rate  $\sim$  msec, similar to flare rise time), AGN, GRB jets

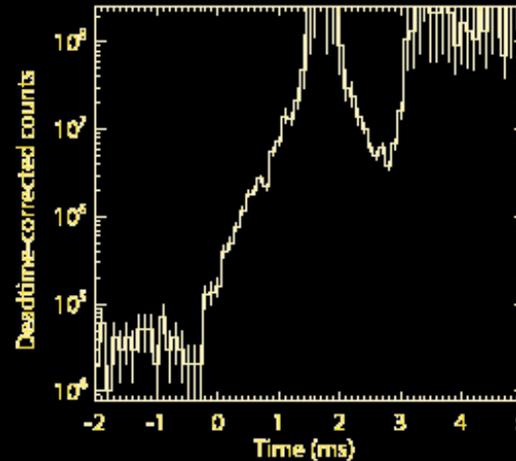


Growth rates in excellent agreement with analytics

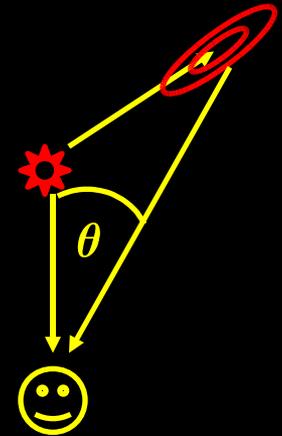
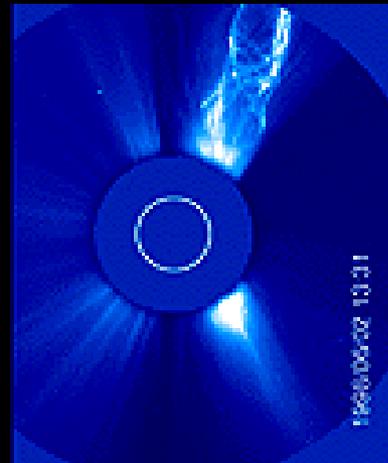
# Applications: magnetars, AGN, GRB jets.

(Lyutikov 2006)

- *Giant flare SGR 1806:*
- *Time scales: observed rise time,  $< 250 \mu\text{sec}$ , implies reconnection in the magnetosphere (Alfven time,  $t \sim R_{\text{NS}}/c \sim 30 \mu\text{sec}$ )*
- *Similar to Solar Coronal Mass Ejection (CME). Magnetar jets (plumes)?*
- *Late constant velocity, sub-relativistic outflow may be just a projection effect*



(Palmer et al. 2005)



$$\beta_{\text{app}} = \beta \text{ctg } \theta/2$$

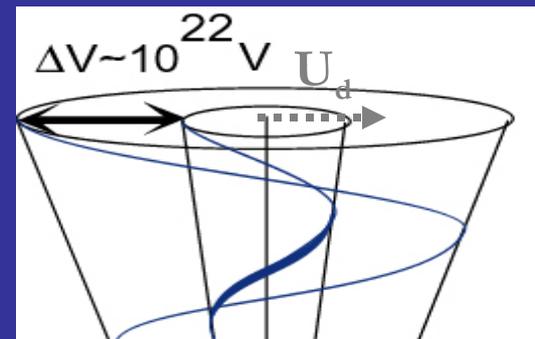
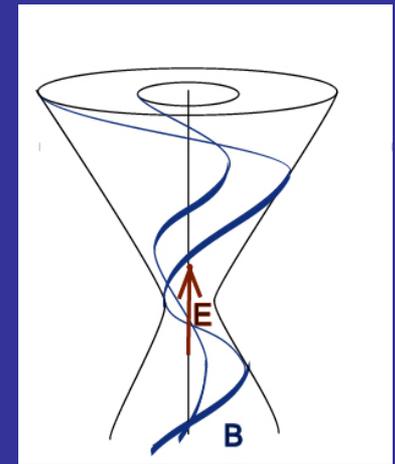
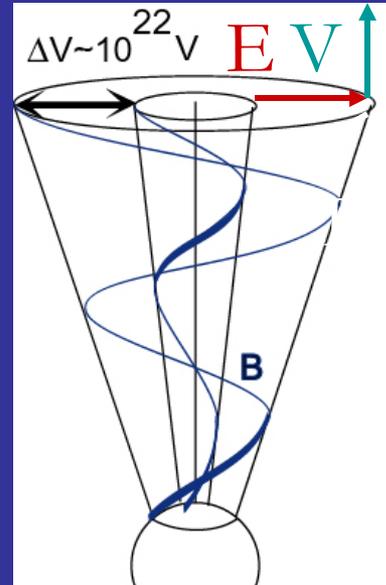
# Acceleration of UHECRs

# UHECRs:

- $E_{\max} \sim 3 \cdot 10^{20} \text{ eV}$
- *Isotropic, perhaps small scale clustering*
- *UHECRs must be produced locally, < 100 Mpc*
- *Perhaps dominated by protons above  $\sim 10^{18} \text{ eV}$*
- *Hard(ish) acceleration spectrum,  $p \sim 2-2.3$*

# Acceleration by large scale inductive E-fields: $E \sim \int v \cdot E ds$

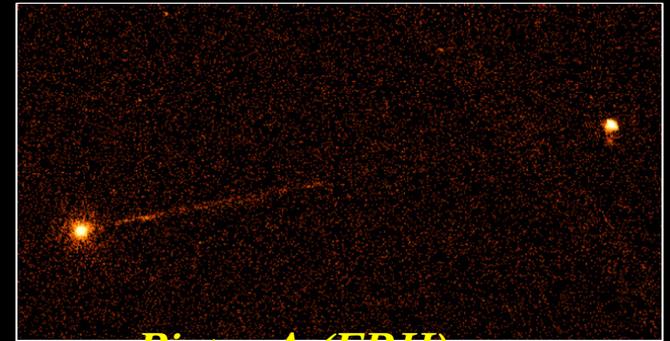
- *Potential difference is between different flux surface (pole-equator)*
- *In MHD plasma is moving along  $V = E \times B / B^2$  – cannot cross field lines*
- *Bring flux surfaces together – Z-pinch collapse (Trubnikov et al 95)*
- *Kinetic motion across B-fields- particle drift - (Bell, Blasi, Arons)*



# $\mathbf{E} \perp \mathbf{B}$ : Inductive potential

$$\Phi \leq \sqrt{\frac{4\pi L_{EM}}{c}}, \quad I \sim \sqrt{\frac{Lc}{4\pi}},$$

$$R \sim \frac{4\pi}{c} \sim 377\Omega, \quad L_{EM} \sim EI$$

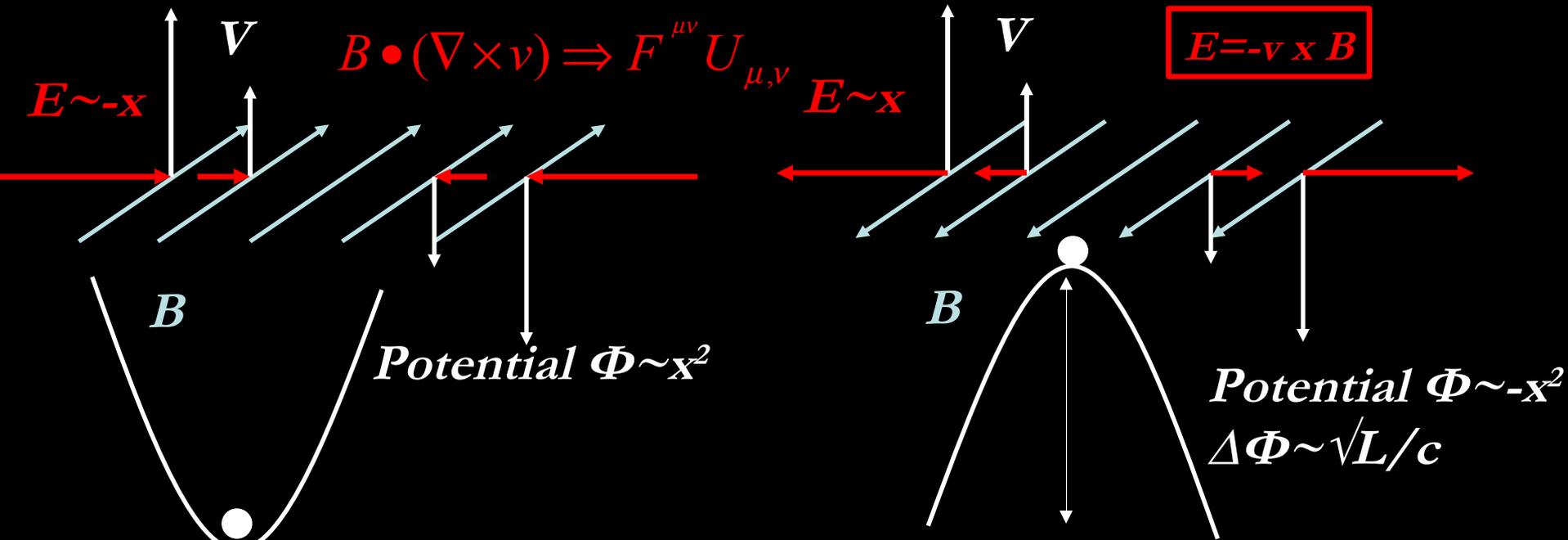


*Pictor A (FR II)*

- To reach  $\Phi = 3 \cdot 10^{20}$  eV,  $L_{EM} > 10^{46}$  erg/s (for protons)
- This limits acceleration sites to high power AGNs (FR II, FSRQ, high power BL Lac, and GRBs)
- There may be few systems with enough potential within GZK sphere (internal jet power higher than emitted), the problem is acceleration scheme

# Potential energy of a charge in a sheared flow

$$\Delta\Phi = \frac{4\pi}{c} B \cdot (\nabla \times v)$$



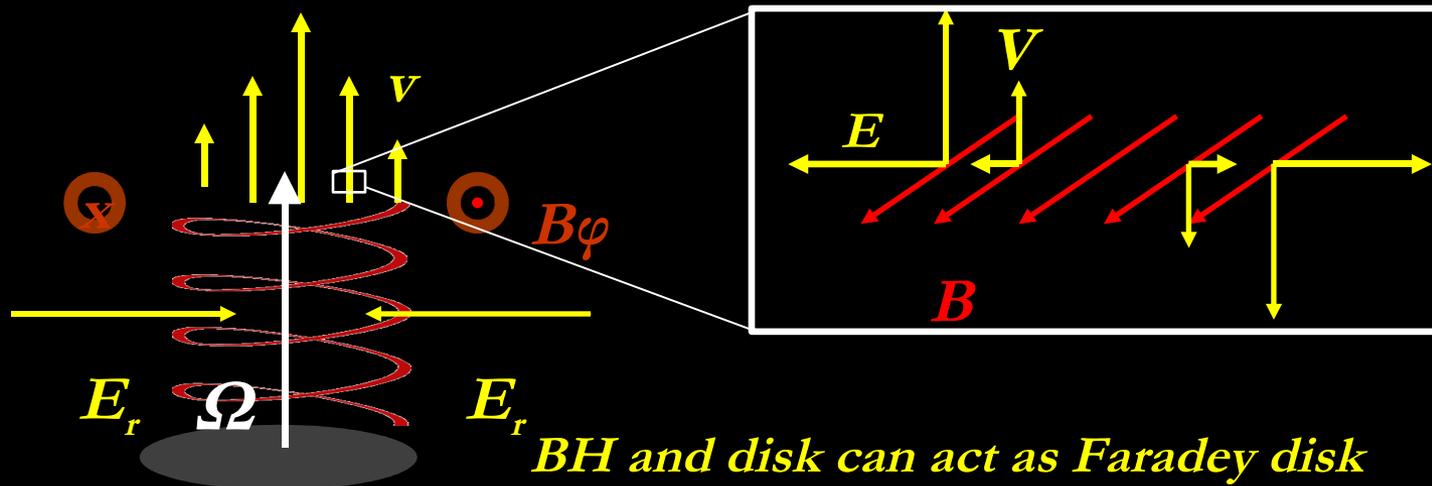
Depending on sign of (scalar) quantity ( $B \cdot \text{curl } v$ ) one sign of charge is at potential maximum

Protons are at maximum for negative shear ( $B \cdot \text{curl } v < 0$ )

# Astrophysical location: AGN jets

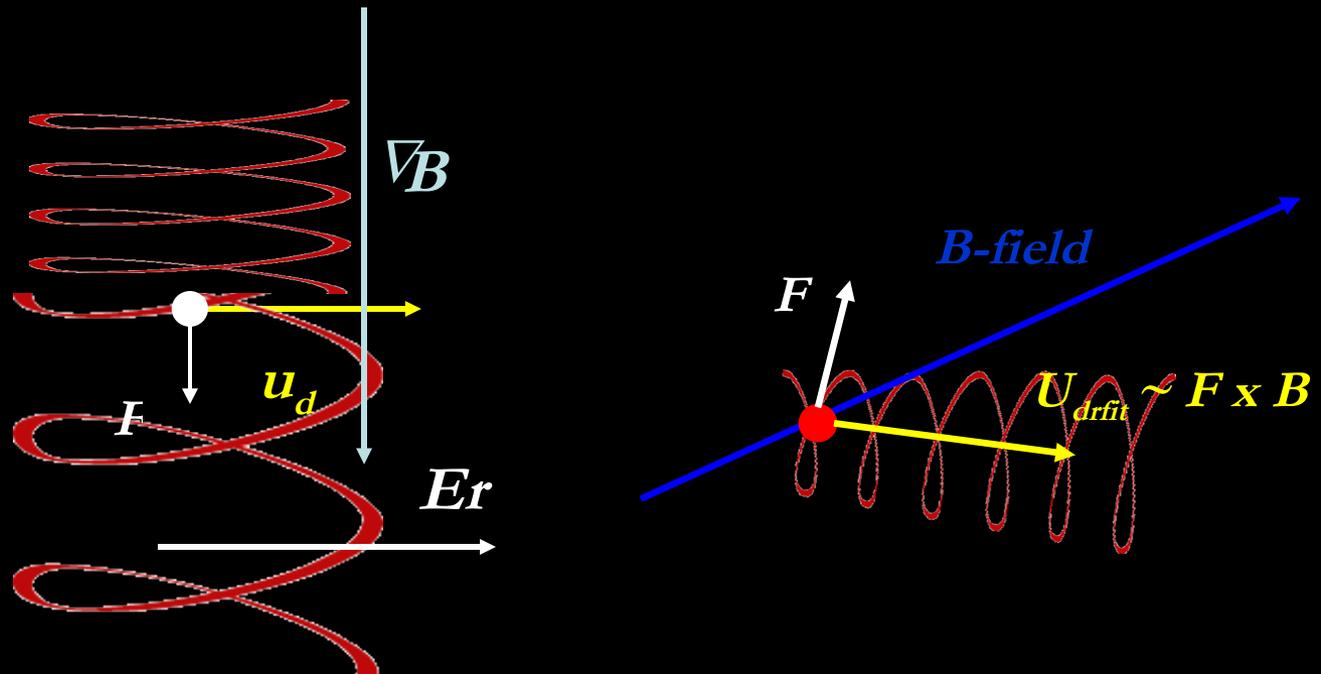
- *There are large scale B-fields in AGN jets*
- *Jet launching and collimation (Blandford-Znajek, Lovelace)*
- *Observational evidence of helical fields*
- *Jets may collimate to cylindrical surfaces (Heyvaerts & Norman)*
- *Jets are sheared (fast spine, slow edge)*

*Protons are at maximum for negative shear ( $B \cdot \text{curl } v < 0$ ).  
Related to  $(\Omega \cdot B)$  on black hole*



# Drift due to sheared Alfvén wave

- Electric field  $E_r \sim -v_z \times B_\phi$  : particle need to move radially, but cannot do it freely ( $B_\phi$ ).
- Kinetic drift due to waves propagating along jet axis  $\omega = V_A k_z$
- $B_\phi(z) \rightarrow U_d \sim \nabla B_\phi \times B_\phi \sim e_r$



# Why this is all can be relevant?

Very fast energy gain :

$$\tau_{acc} \sim \frac{1}{|k_A| c} \sqrt{\frac{ZeBc}{E\eta}}$$

- *highest energy particles are accelerated most efficiently!!!*
- *low Z particles are accelerated most efficiently!!! (highest rigidity are accelerated most efficiently)*
- *Acceleration efficiency **does** reach absolute theoretical maximum  $1/\omega_B$*
- *Jet needs to be  $\sim$  cylindrically collimated; for spherical expansion adiabatic losses dominate*

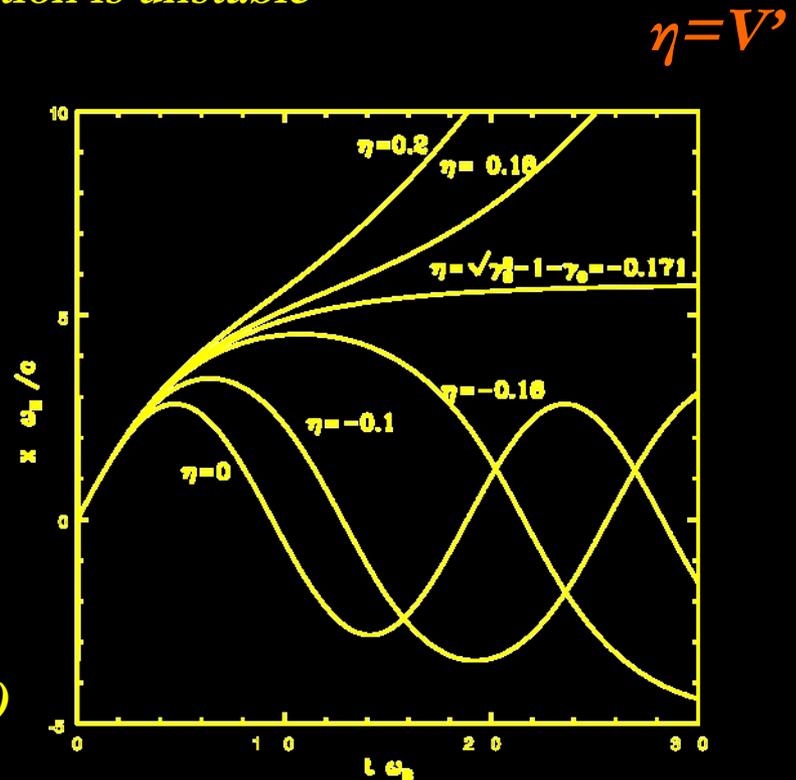
# Acceleration rate DOES reach absolute theoretical maximum $\sim \gamma/\omega_B$

- Final orbits (strong shear),  $r_L \sim R_p$ , drift approximation is no longer valid
- New acceleration mechanism
- For  $\eta < \eta_{crit} < 0$ ,  $\eta_{crit} = -\frac{1}{2} \omega_B/\gamma$ , particle motion is unstable

$$\frac{\eta_{crit}}{\omega_B / \gamma_0} = \gamma_0 \left( -\gamma_0 + \sqrt{\gamma_0^2 - 1} \right) \approx -\frac{1}{2}$$

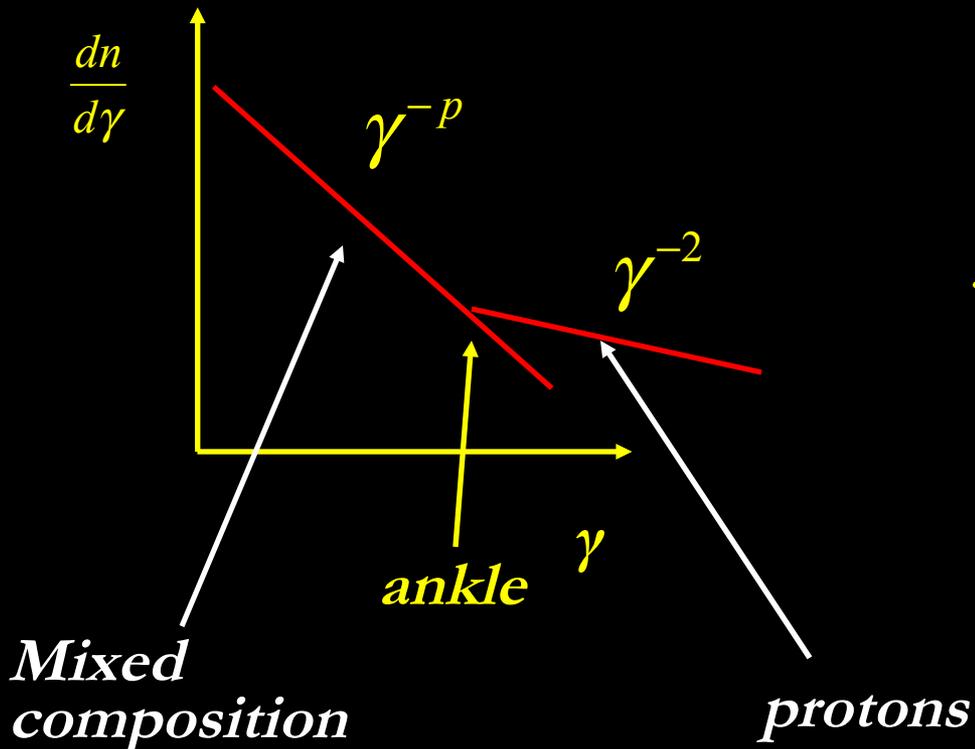
- non-relativistic:  $x = r_L \cos \left( \omega_B \sqrt{1 + \frac{\eta}{\omega_B}} t \right)$   
 $y = \frac{r_L}{\sqrt{1 + \eta/\omega_B}} \sin \left( \omega_B \sqrt{1 + \frac{\eta}{\omega_B}} t \right)$

- Acceleration DOES reach theoretical maximum  $\sim \gamma/\omega_B$
- Note: becoming unconfined is GOOD for acceleration (contrary to shock acceleration)



# Spectrum

➤ From injection  $dn/d\gamma \sim \gamma^{-p} \rightarrow dn/d\gamma \sim \gamma^{-2}$

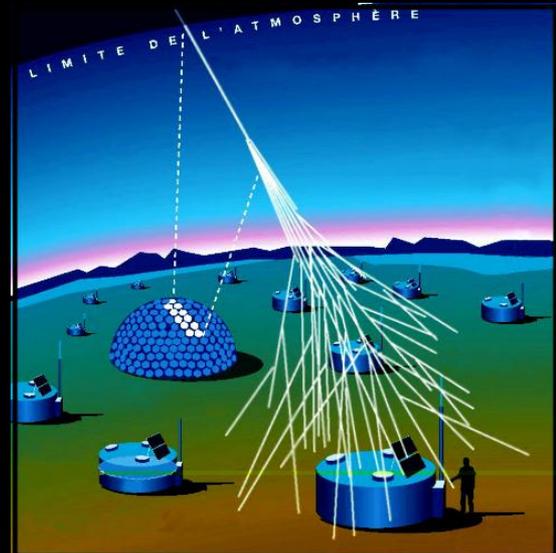


*Particles below the ankle do not gain enough energy to get  $r_L \sim R_j$  and do not leave the jet*

**UHECRs are dominated by protons, below the ankle: Fe**

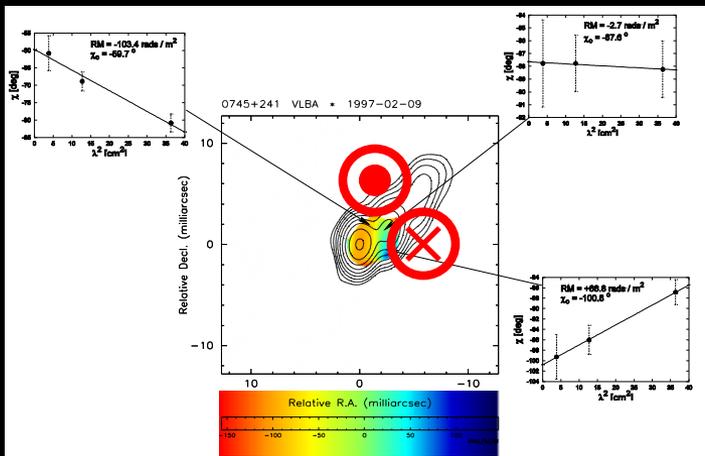
# Astrophysical viability

- *Need powerful AGN FR I/II (weak FR I, starbursts are excluded)*
  - *UHECRs (if protons) are not accelerated by our Galaxy, Cen A or M87*
- *Several powerful AGN within 100 Mpc, far way → clear GZK cut-off should be observed: Pierre Auger: powerful AGNs?*
  - *GZK cut-off*
  - *few sources*
  - *IGM B-field is not well known*
- *Fluxes:  $L_{\text{UHECR}} \sim 10^{43} \text{ erg/sec}/(100 \text{ Mpc})^3$  – 1 AGN is enough*

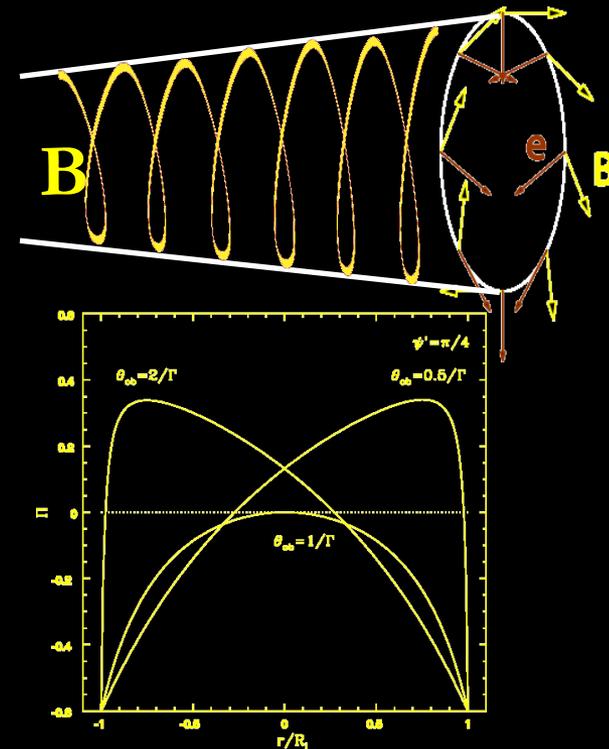


# Faraday Rotation and gradient of linear polarization across the jet in 3C 273

- *Gradient of Rotation Measure across the jet*



- *Gradient of linear polarization*



*(Gabuzda 03, confirmed by Taylor et al)*

- *Possible interpretation: helical field*
- *Need lots of poloidal flux → may come from a disk, not BH*

# Conclusion

- *EM-dominated plasma: may be a viable model for a variety of astrophysical phenomena. Very little is done.*
- *Macrophysical models (ideal dynamics)*
- *Microphysics (resistivity is anomalous,  $\eta \sim c^2/\omega_p$ ,  $\eta \sim c^2/\omega_B$ ; particle acceleration)*
- *Need for simulations (both dynamics and acceleration)*
  - *EM codes with currents*
  - *PIC codes (Nordlund)*
- *Observations seem to be coming along*



- *“Where have you seen plasma, especially in magnetic field?” Landau*
- *“The magnetic field invoked is proportional to someone’s ignorance” Woltjer*

# Radiative losses

- *Equate energy gain in  $E = B$  to radiative loss  $\sim U_B \gamma^2$*

$$r > \frac{Z^2 e^2}{mc^2} \left( \frac{E}{mc^2} \right)^3 \Gamma^{-2} \sim 10^{16} \Gamma_{10}^{-2} \left( \frac{E}{100 \text{ EeV}} \right)^3 \text{ cm}$$

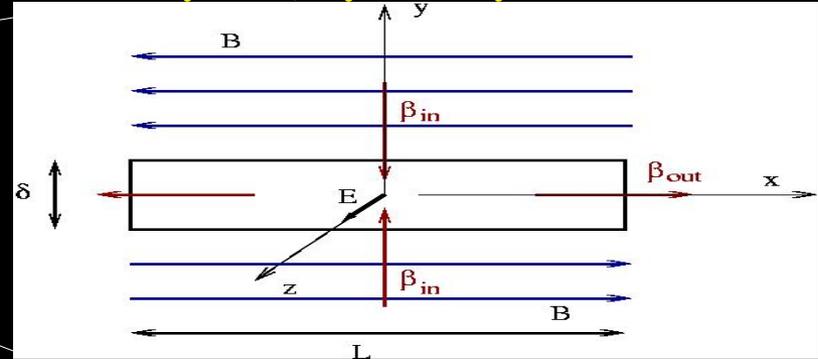
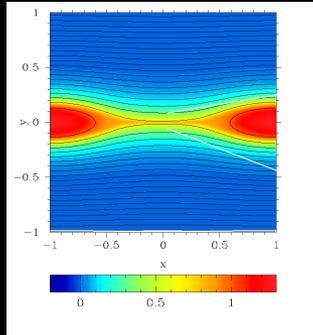
$$B < \frac{m^2 c^4}{Z^3 e^3} \left( \frac{E}{mc^2} \right)^{-2} \Gamma^3 \sim 6 \cdot 10^4 \Gamma_{10}^3 \left( \frac{E}{100 \text{ EeV}} \right)^{-2} \text{ G}$$

$$\Phi \leq \sqrt{\frac{4\pi \beta_0 L}{c}},$$

- *As long as expansion is relativistic, total potential remains nearly constant, one can wait yrs – Myrs to accelerate*

# Relativistic reconnection, $\sigma \gg 1$ (Sweet-Parker)

(Blackman & Field 1994; Lyutikov & Uzdensky 2003; Lyubarsky 2004)



➤ *Two parameters: Lundquist  $S = V_A L / \eta \gg 1$ ,  $\sigma \gg 1$*

➤  $\gamma_{out} \approx (1 + \sigma)\gamma_{in} \gg 1$  *outflow is always relativistic*

➤ *Inflow:*

▪  $\sigma \ll S$  – *non-relativistic inflow*  $\beta_{in} \approx \sqrt{\frac{\sigma}{S}} = \sqrt{\frac{2}{S}}\gamma_A, \frac{\delta}{L} \approx \sqrt{\frac{S}{\sigma}} \ll 1$

▪  $S \ll \sigma \ll S^2$  – *relativistic inflow*  $\gamma_{in} \approx \frac{\sigma}{S}, \gamma_{out} \approx \frac{\sigma^2}{S} \gg 1, \frac{\delta}{L} \approx \frac{1}{\sigma} \ll 1$

➤ *Relativistic reconnection can be fast,  $\sim$  light crossing time*

# Particle acceleration in relativistic reconnection

*Leptons*

➤ *Numerical experiments are only starting (Hoshino02, Larrabee et al 02).*

➤ *Spectra depend on kinetic properties and geometry*

*$\int (v \cdot E) dl$  (McClements)*

➤ *If escape  $\sim r_L$ , then*

$$\frac{dn}{d\gamma} \propto \gamma^{-\beta_{in}}$$

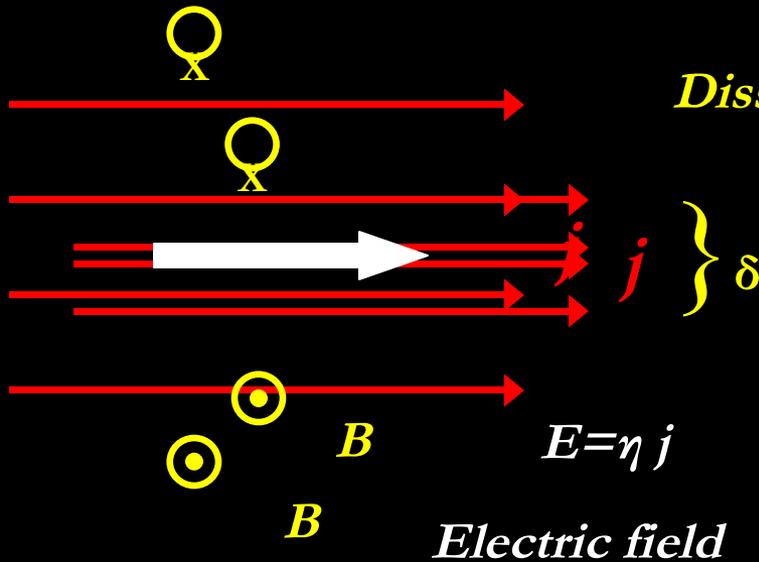
➤ *For GRB we need  $\gamma^1$  (Lazatti), also TeV AGNs (Aharonian)*

➤ *No calculations of acceleration at relativistic tearing mode (should accelerate as well)*

# Why magnetic energy wants to dissipate

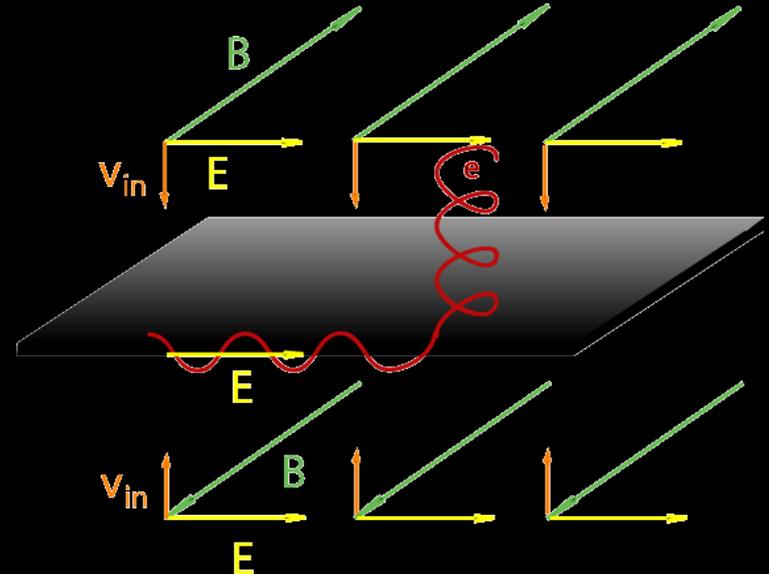
What is needed for magnetic dissipation is presence of electrical current

*formation of current sheet*



*Dissipation rate  $\sim \eta \Delta B \sim \eta B / \delta^2$*

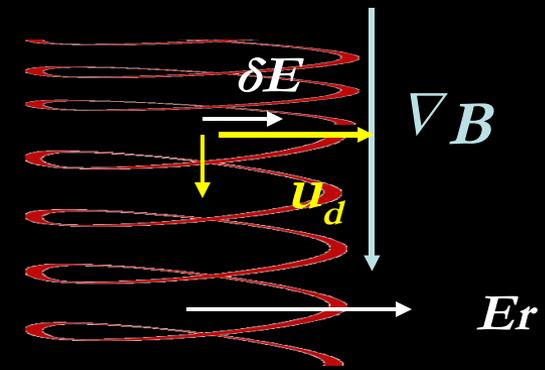
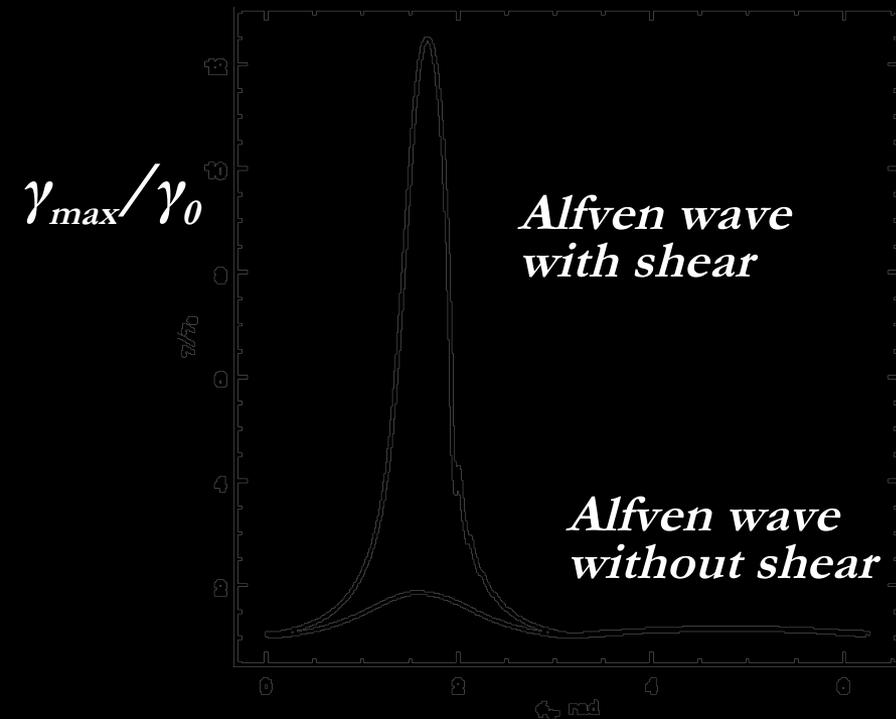
*Anomalous resistivity  $\eta(j)$*



*Next: generalize non-relativistic fluid models to new regime*

# Wave surfing can help

- *Shear Alfvén waves have  $\delta E \sim (V_A/c) \delta B$ ,*
- *Axial drift in  $\delta E \times B$  helps to keep particle in phase*
- *Particle also gains energy in  $\delta E$*



*Most of the energy gain is in sheared E-field (not E-field of the wave, c.f. wave surfing)*

# AGN jet

➤ *In situ acceleration is required ( $t_{\text{synch}} < R/c$ , short time scale variability: 20 min at TeV!)*

➤  *$e^\pm$  winds - strong losses at the source*

➤ *Ion-dominated - hard to get variability, low radiation efficiency (Celotti, Ghisellini)*

*EM- dominated! (Lesch&Birk; Lovelace; ML)*

➤ *Currents needed for collimation; Currents are unstable*

➤ *Resistive modes may not destroy the jet, but re-arrange it (eg, sawtooth in TOKAMAKs, Appl)*

➤ *Relativistic FF jets stabilized by rotation*

➤ *Hard power law may be needed for TeV emission (Aharonian)*

➤ *Polarization from helical B-field (Gabuzda; ML, in prep)*

# Jets start as B-field-dominated, can $\sigma$ changes on the way?

- (Weber & Davis, Goldreich & Julian, Vlahakis & Konigl)
- *Ideal conversion: acceleration*
    - *Acceleration to fast point  $\Gamma_{fast} \sim \sqrt{\sigma_{fast}}$*
    - *At this point  $\sigma \sim \Gamma^2 \gg 1$  : flow remains B-field dominated*
    - *Collimation  $\sigma \rightarrow 1$ , but it is slow  $\sim \ln z$  and unlikely  $\sigma \ll 1$* 
      - *There are some indication (Homan et al , Jorgstad et al.) moving features, (Sudou et al.) increased jet-counter jet brightness, but not conclusive (jet bending & aberration can give visible acceleration).*
  - *Dissipative: on scale  $> R_{BH} \Gamma^2 \sim 10^{17}$  cm (e.g relativistic reconnection  $\beta_{in} \sim 1$ , Lyutikov & Uzdensky)*
    - *blazar  $\gamma$ -ray emission zone (Lyutikov 2003). Variation in  $\Gamma$  produced locally (no large UV variations of disk are seen): (Sikora et al. 2005)*
  - *Jet can remain B-field dominated to pc scales*

# How can the two paradigms ( $\sigma \gg 1$ and $\ll 1$ ) be distinguished?

## 1. Acceleration scheme with predictive power ( $\gamma_{\min}$ , $p$ )

### *Shocks*

- *Spectra of Fermi-accelerated particles (kinetic property) can be derived from shock jump conditions*
- *Electrons need to be pre-accelerated to*  
 $\gamma \sim m_p/m_e \sim 2000$   
*(or  $\sqrt{m_p/m_e} \sim 43$ )*

### *B-field*

- *“Reconnection” spectra are not “universal”, depend on details of geometry (universal in relativistic case,  $p=1$  ?)*
- *No need for pre-acceleration: all particles may be accelerated*

# How can the two paradigms be distinguished?: very hard spectra, $p < 2$

- *Shock typically produce  $p > 2$ , relativistic shocks have  $p \sim 2.2$  (Ostrowki; Kirk)*
- *non-linear shocks & drift acceleration may give  $p < 2$ , e.g.  $p = 1.5$  (Jokipi, Bell & Lucek)*
- *B-field dissipation can give  $p = 1$  (Hoshino; Larrabee et al.); such hard spectra may be needed for TeV emitting electrons ( $\gamma$ - $\gamma$  pair production on extragalactic light Aharonyan; Schroedter).*

*$p < 2$  spectra should not be discarded as unphysical*

## 2. Radiation modeling: not conclusive

➤ **Blazar dominance by IC:**  $U_{ph}' / U_B' \sim \Gamma^4, \Gamma \gg 10;$

under equipartition @  $10^{17}$  cm

$U_{e\pm}' \sim 50-100 U_B'$  (Krawczynski 04).

Outflows in bulk flow?

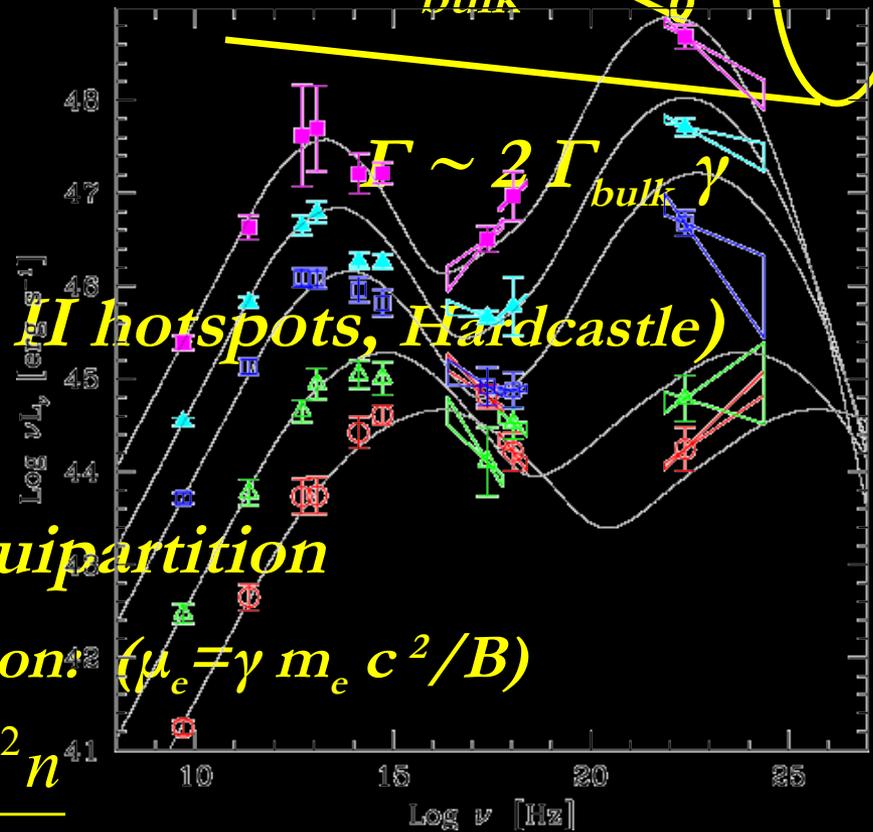
➤ **Equipartition (e.g. in FR II hotspots, Hardcastle)**

▪  $U_B' \sim U_{e\pm}'$

▪ **Amplification: sub-equipartition**

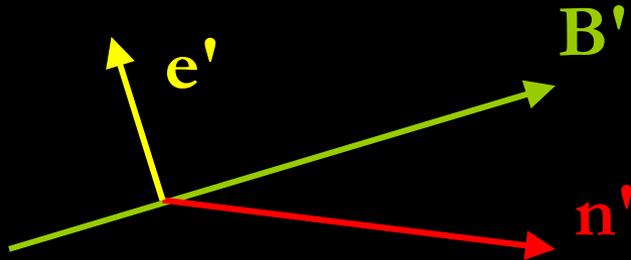
▪ **Dissipation → equipartition:** ( $\mu_e = \gamma m_e c^2 / B$ )

$$\frac{B_{ind}}{B} = \frac{\mu n}{B} = \frac{\gamma m_e c^2 n}{B^2}$$



# Aberration of $\Pi$ : B-field is NOT orthogonal to polarization

➤ *In plasma frame*



$$e' \perp B', n'$$

$$n \sim \gamma^{-p}, \Pi_{\max} = \frac{p+1}{p+7/3}$$

➤ *In laboratory frame*

$$e = \frac{n \times q}{\sqrt{q^2 - (n \cdot q)^2}}$$

$$q = \hat{B} + n \times (v \times \hat{B})$$

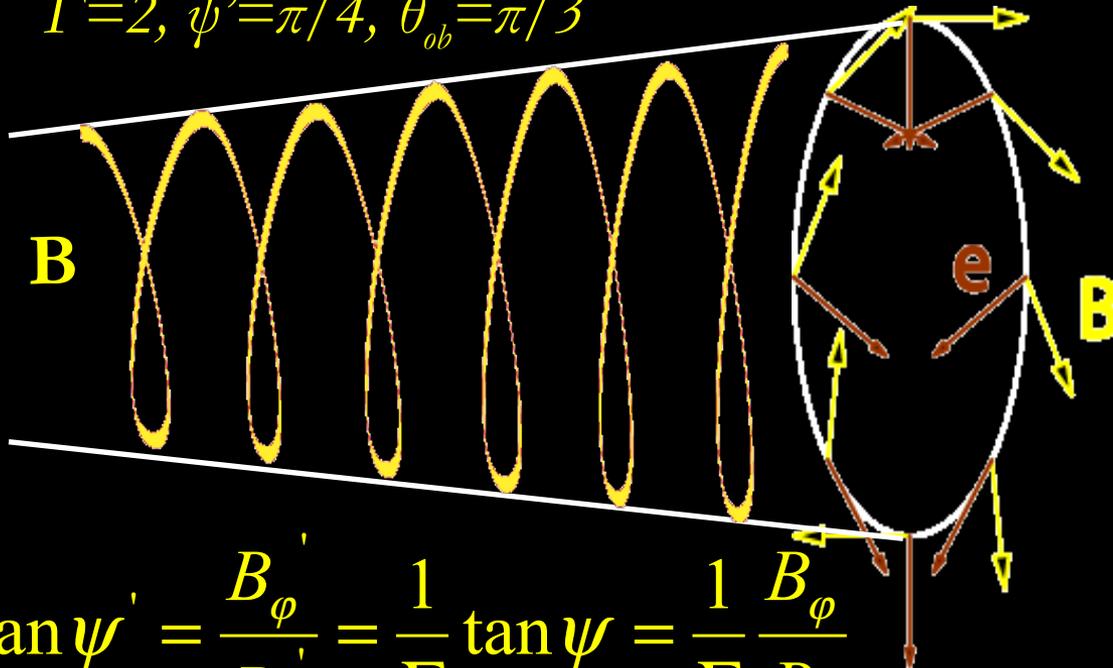
$$(e \cdot \hat{B}) = (e \times n) \cdot (\hat{B} \times v) \neq 0$$

*Both B-field and velocity field are important for  $\Pi$*

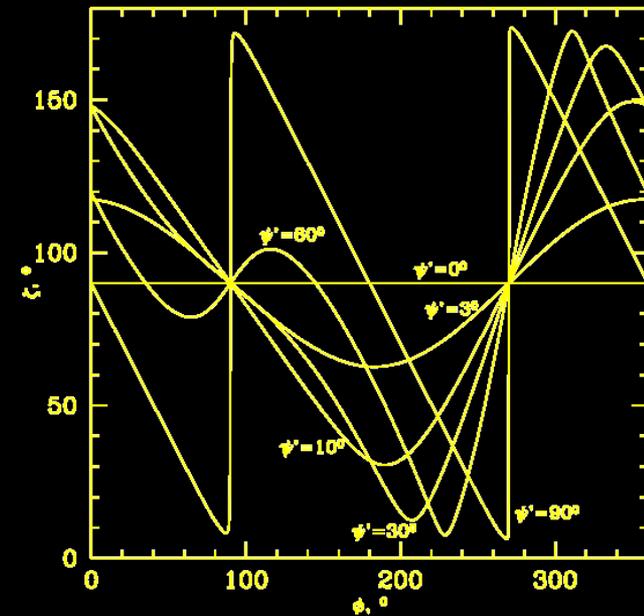
*(Blandford & Konigl 79; Lyutikov, Pariev, Blandford 03)*

# $\Pi$ from relativistically moving cylindrical shell with helical B-field

$$\Gamma=2, \psi'=\pi/4, \theta_{ob}=\pi/3$$

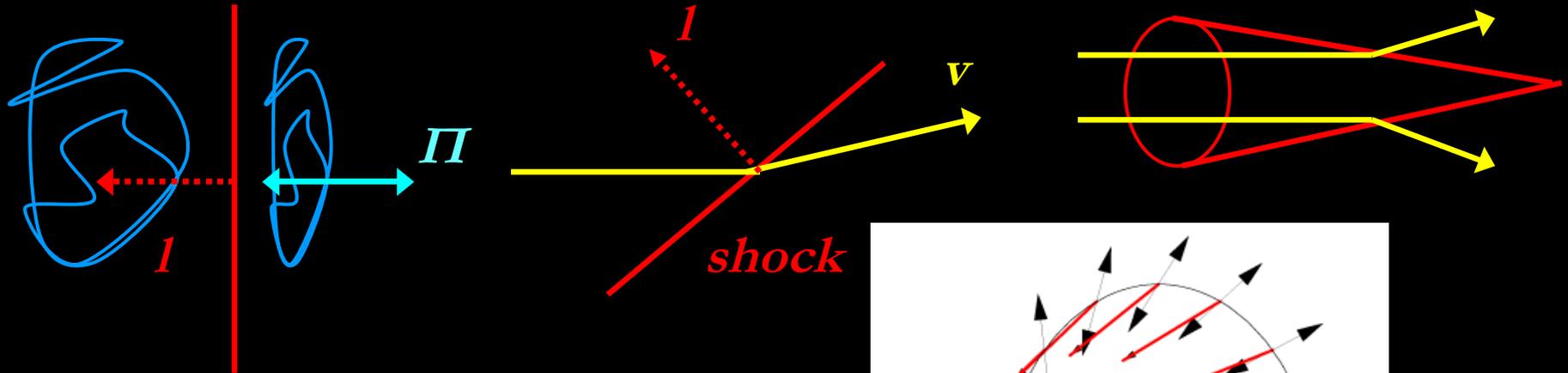


$$\tan \psi' = \frac{B_\phi'}{B_z'} = \frac{1}{\Gamma} \tan \psi = \frac{1}{\Gamma} \frac{B_\phi}{B_z}$$



- $B$  not orthogonal to  $e$
- Jet can be  $B_\phi$  dominated in observer frame and  $B_z$ -dominated in rest

# $\Pi$ from random B-field compressed at an oblique shock

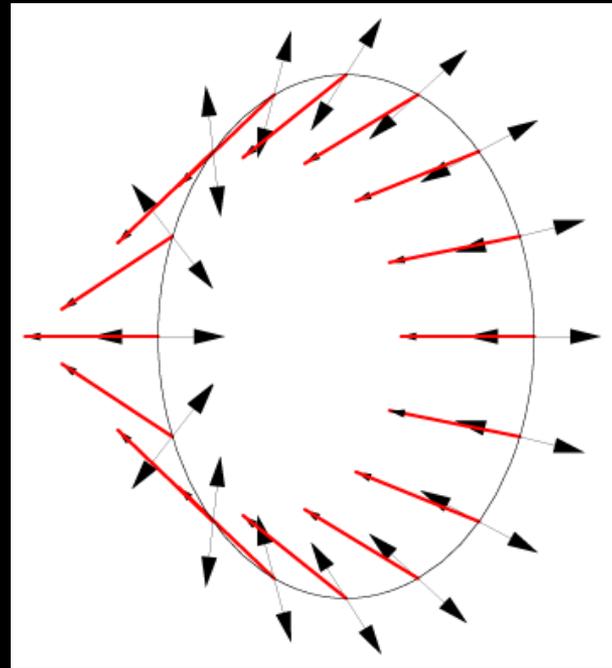


*upstream shock downstream*

$$\mathbf{e} = \frac{\mathbf{n} \times \mathbf{q}}{\sqrt{\mathbf{q}^2 - (\mathbf{n} \cdot \mathbf{q})^2}}$$

$$\mathbf{q} = \mathbf{n} \times \left( \mathbf{l} - \mathbf{n} \times (\mathbf{l} \times \mathbf{v}) - \frac{\Gamma}{\Gamma + 1} (\mathbf{l} \cdot \mathbf{v}) \mathbf{v} \right)$$

*Lyutikov (in prep)*

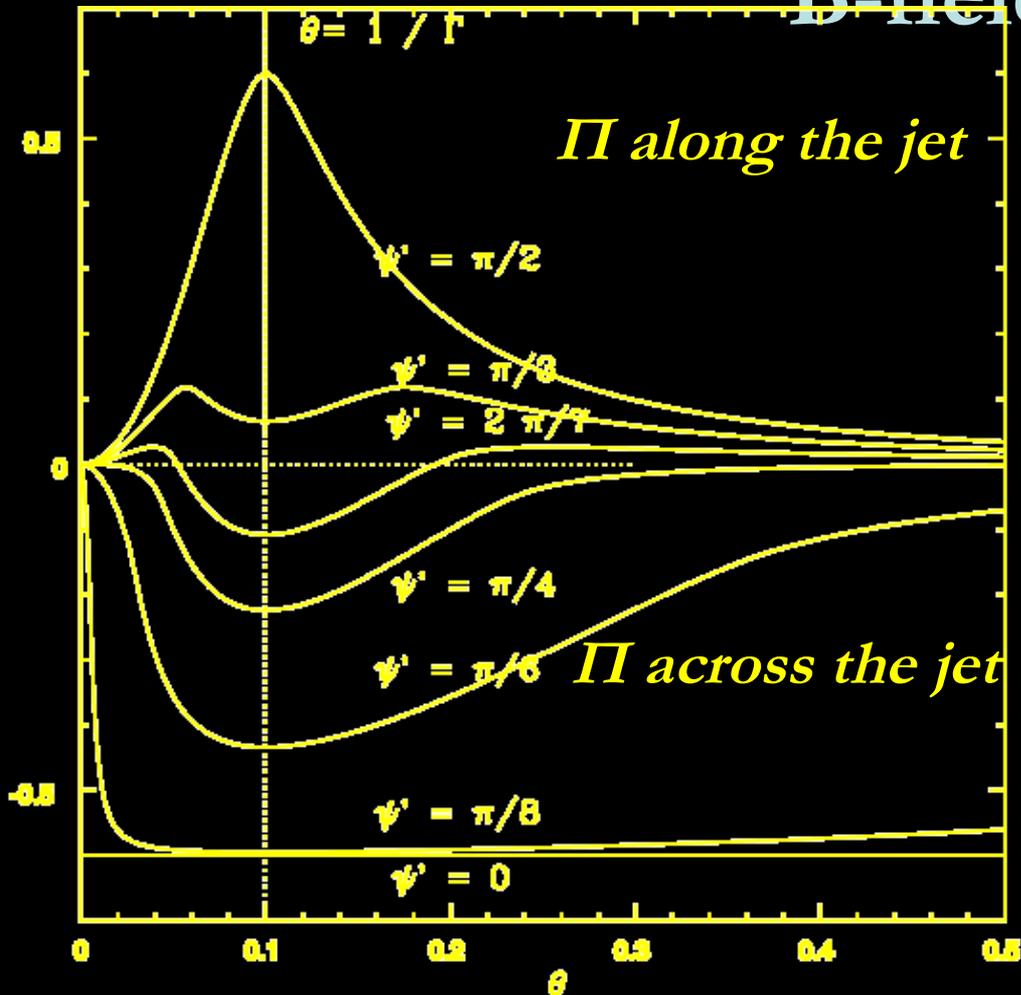


*$\Pi$  not aligned with projection of  $l$ ,  
also Cawthorn & Cobbs*

# Aberration of $\Pi$

- *Direction of  $\Pi$  depends both on B-field and velocity field*
- *Always plot “e”, not “inferred” B-field*
- *One needs to know velocity to infer internal B-field*
- *Symmetries in the velocity field may help*
  - *e.g. if shock is conical, on average polarization along or across jets (Cawthorn & Cobbs)*

# $\Pi$ from cylindrical shell with helical B-field



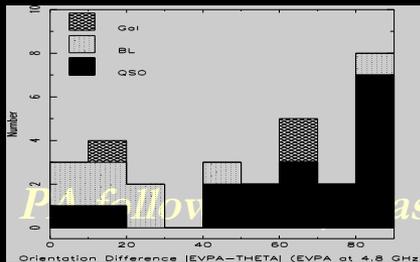
- $\Pi$  depends on  $p$
- Even co-spatial populations with different  $p$  may give different  $\Pi$  (eg Radio & Optical)

$$\tan \psi' = \frac{B_{\phi}'}{B_z'}$$

$\Gamma=10, p=1, \text{ different rest frame pitch angles}$

# Large scale or small scale B-fields in pc-scale AGNs jets

- **Bimodal distribution of PA**

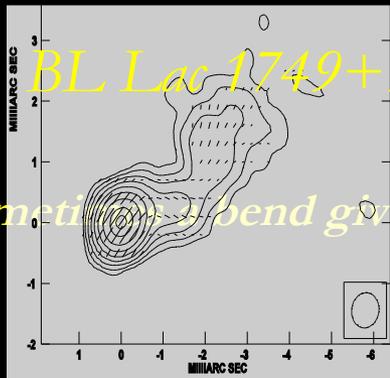


- **PA follows  $\Pi$  as it bends** (Aller et al)

- For cylindrical jet  $U=0$ , average  $\Pi$  along or across the axis. Only conical shocks can give the same.

- For fixed  $\psi$ ,  $\Pi$  mostly keeps its sign. Note: for plane shock there is no correlation between  $\Pi$  and bend direction.

- **Sometimes a bend gives 90 change of PA**

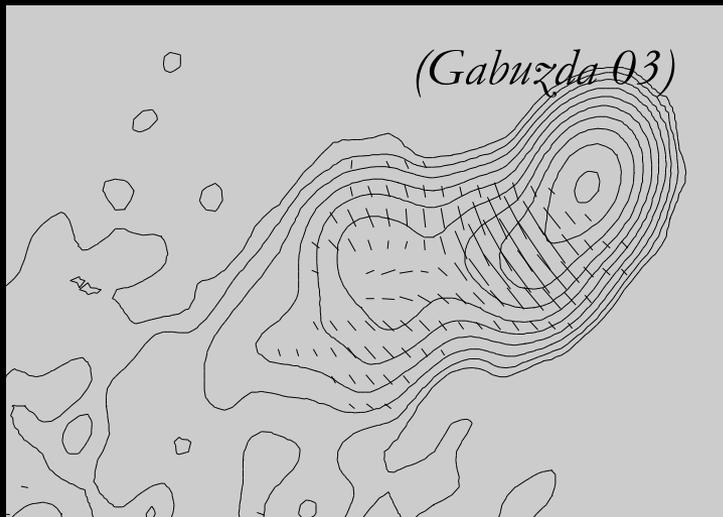
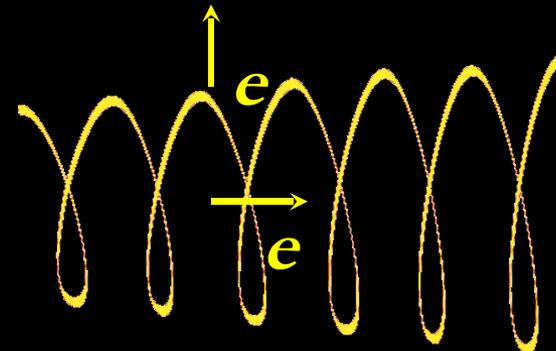


(Gabuzda 03)

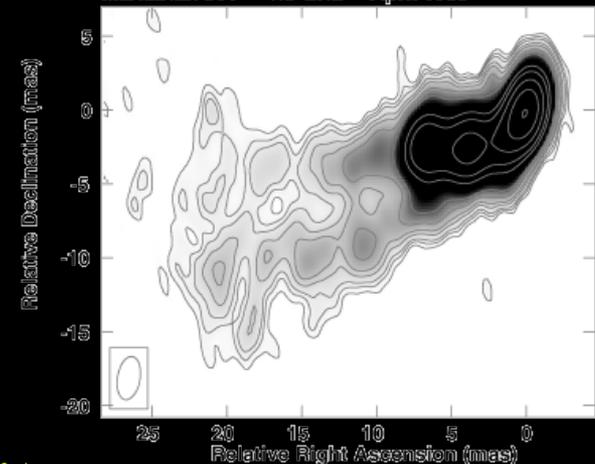
- Sometimes a change does occur

# Resolved jets

- *Resolved jets: center: PA  $\parallel$ , edges: PA  $\perp$* 
  - *Emission is generated in small range  $\Delta r < r$*   
*(shear acceleration? Ostrowski)*
  - *Core is boosted away*

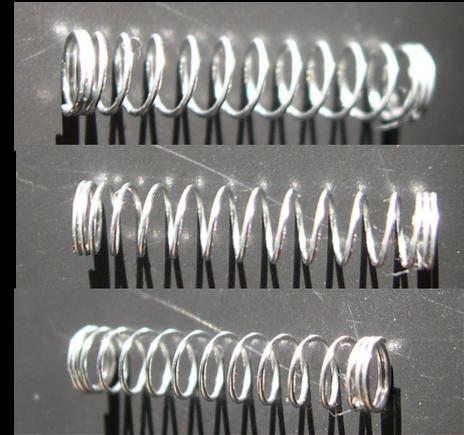
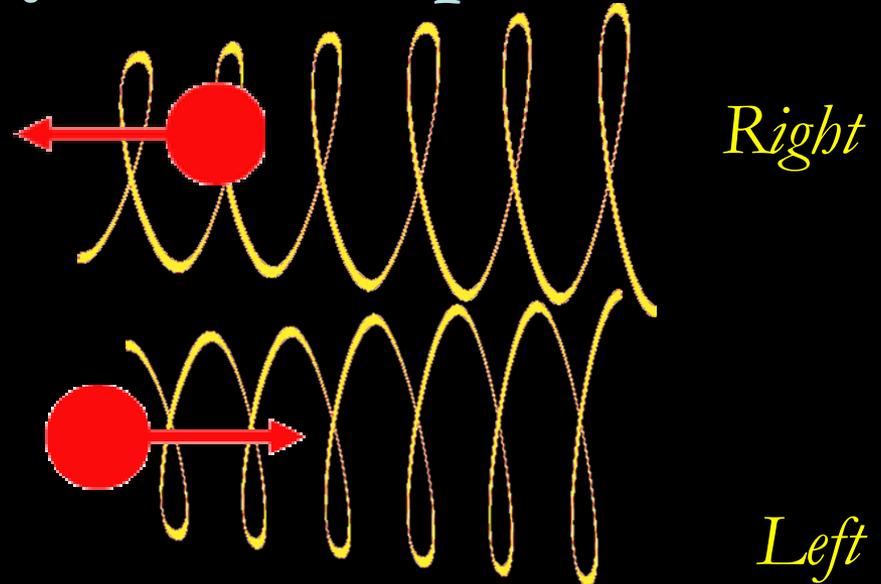
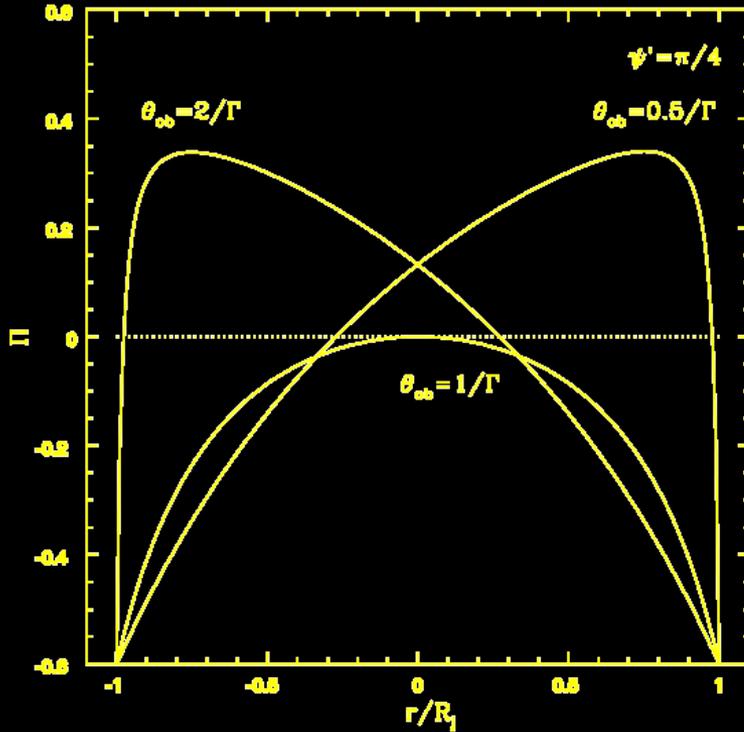


Markarian 501 1.6 GHz April 1993



*Limb-brightening Mkn 501, (Giroletti)*

# Jet polarization may tell the spin of BH

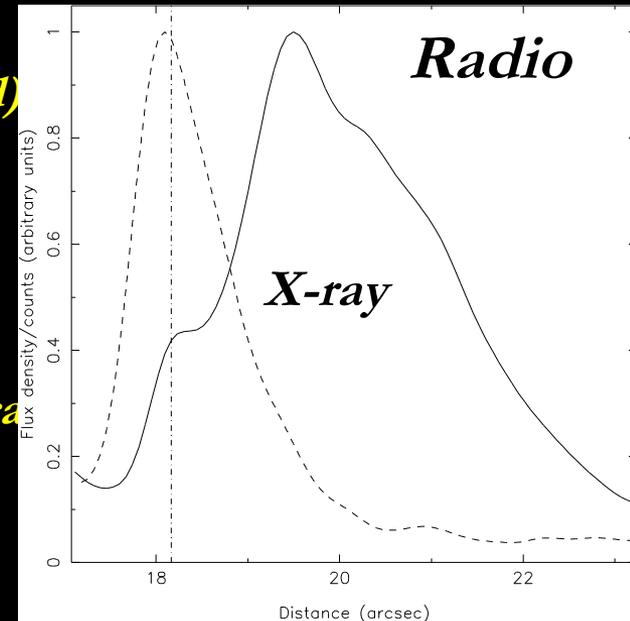


- *Left & Right helixes look different*
- *Different  $\Pi$  signature*
- *Direction of BH or disk spin (if  $\theta\Gamma$  is known)*

# Tests/unresolved issues

- Cen A (Hardcastle et al 2000)**  
*Firmly established flow acceleration at (sub)-pc scales: evidence of B-field conversion*
- *More  $\Pi$  studies, especially CP (unidirectional B-field)*
    - *with MHD codes*
  - *Spectra requiring  $p \rightarrow 1$*
  - *Acceleration rates above*
  - *Very high  $\Pi > 50\%$  in R*
    - *compressed B-fields isotropize on Alfvén time scale dominated by small scale*
    - *turbulence will lead to isotropization*
  - *Different e-acceleration mechanisms?*
    - *X-rays are displaced from O-R (e.g. Cen A)*
    - *Magnetic & shock acceleration? (Kirk)*
    - *NB: similar in Crab pulsar*

$$\tau_{acc} \sim \frac{c^2}{v_s^2} \frac{\gamma}{\omega_B}$$



# Are all ultra-relativistic jet the same?

- $E_{\text{peak}} - L$  correlations
  - GRBs - positive, BL Lac – negative
- Internal shocks in GRBs must be highly (unreasonably?) efficient, in BL Lac – inefficient
- GRS 1915: jets appear after drop of the x-ray flux, blazars: no correlation between UV flux and flares
- jets without BH (Cirnicus X-1)

# Prospects

- *Sept. 2002, Bologna Conference: “Can one “ prove” reconnection? – Not from first principles”*
  - *By analogy to some Solar phenomena*
  - *Nothing else can do*
- *May be we can...*