Magnetars: why, where and how flares occur.

Maxim Lyutikov (Purdue U.)

Monday, October 27, 14

Magnetars' bursts and flares

- Magnetars: special class of NS:

- Produce X-ray bursts, flares and persistent emission

- Powered by B-field, $B \sim 10^{14} \text{ G}$ outside, > 10^{15} G inside

- How?





Location and discovery date of the 5 SGRs



S.Mereghetti

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Mostly young, ~ 10^{4-5} yrs, high(ish) B-fields, > 10^{13} G

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Magnetars are powered by dissipation of super-strong B-field, B~ 10¹⁴⁻¹⁵ G

- $L_{\chi} = 10^{34} 10^{36} \text{ erg s}^{-1} > 100 L_{\text{spindown}}$, $L_{\text{spindown}} = I \Omega \dot{\Omega}$ (not rotationally powered)
- Spin periods P = 5 12 s slow
- Characteristic ages 3 10³ -- 4 10⁵ yr

Thompson & Dunkan

- From spindown $I\Omega\dot{\Omega}\sim B^2R_{NS}^2c\left(rac{\Omega R_{NS}}{c}
ight)^4$

 $B \sim 10^{14} - 10^{15} G$

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- From flare energetics: $E_{\rm flare} \sim E_{\rm tail} \sim B^2 R_{NS}^3$

Amplification of magnetic field: Dynamo in neutron stars: first 10 secs



- Turbulence dies out, NS relaxes to an MHD equilibrium.
- Big Q.: What is the stable B-field structure of fluid stars?
- B-field must be a combination of toroidal and poloidal field, otherwise unstable
- Pure toroidal is unstable to sausage instability:
- Pure poloidal is also unstable:



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(Prendergast, Fawley & Ruderman, Braithwaite, Lander and Jones)

Stability! (?)

• Braithwaite & Spruit:





Large initial toroidal flux

Small initial toroidal flux

- Similar toroidal and poloidal fluxes needed for stability
- Lander and Jones: any barotropic $(p(\rho))$ B-field equilibrium is unstable need $p(\rho, \epsilon)(?)$

For stability B-field must be linked



@ 100 secs crust freezes

no shear stresses at freezing (was fluid)

Electron MHD:

- After freezing ions form a fixed lattice
- electrons flow as fluid, J = n e v
- B-field frozen into_electrons:

$$\mathbf{E} = -\mathbf{v} \times \mathbf{B} = \frac{\mathbf{J}}{ne} \times \mathbf{B}, \ \mathbf{J} = \frac{c}{4\pi} \nabla \times \mathbf{E}$$

$$\frac{\partial \mathbf{B}}{\partial t} = -\frac{c}{4\pi e} \nabla \times \left(\frac{\nabla \times \mathbf{B}}{n} \times \mathbf{B}\right)$$

• Electrons flow as an inertialess fluid



ne

• MHD: $\mathbf{J} \times \mathbf{B} = \nabla p + \rho \nabla \Phi$ • EMHD: $\mathbf{E} = -\mathbf{v} \times \mathbf{B} = \frac{\mathbf{J}}{-} \times \mathbf{B}$

$$\nabla \times \frac{\mathbf{J} \times \mathbf{B}}{\rho} = -\frac{\nabla p \times \nabla \rho}{\rho^2}$$
$$\nabla \times \frac{\mathbf{J} \times \mathbf{B}}{n} = 0$$

• MHD:
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Non-barotropic EoS



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Freezing of MHD equilibrium
results in non-equilibrium
EMHD state
mu-gradient
Non-barotropic EoS

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Non-barotropic EoS

After freezing B-field starts evolving in the crust under EMHD conditions

Electron MHD: Very heavy ions, very light electrons $\omega_{B,e} \gg \omega \gg \omega_{B,i}$

- NS crusts
- Turbulent cascade in collisionless plasmas (Solar wind, BH magnetospheres, clusters of galaxies)



• sub-ion skin depth dynamics in reconnection layers



Electron MHD

- Normal modes: whistlers (Fully non-linear!) $\omega = c^2 k^2 |\cos \theta| \omega_B / \omega_p^2$
- Energy and helicity conserved $\partial_t B^2/2 + \nabla \cdot (\mathbf{E} \times \mathbf{B}) = 0 \quad \partial_t (\mathbf{A} \cdot \mathbf{B}) = -\nabla \cdot (\mathbf{A} \times \dot{\mathbf{A}})$ $\mathbf{E} = \nabla \times \mathbf{B} \times \mathbf{B}$
- Time scales

$$\tau_H = \frac{L^2 \omega_p^2}{c^2 \omega_B} \approx 100 \,\mathrm{yrs} \left(\frac{L}{1 \,\mathrm{km}}\right)^2 \rho_{10} b_{15}^{-1} \,\mathrm{yr}$$

 can vary from ~ 1yr for small patches near the surface, to 1Mys at the base of the crust for magnetars

Quo Vadis: are there stable/attractors configurations in EMHD?

Stability of EMHD configurations

- RT-type instability: the system can decrease it energy internally
 - the energy principle reaching a special state with min E.
 - MHD
- KH-type instability: energy of the system does not change, re-distributed to "other" modes
 - incompressible fluid no special state
 - turbulence transferring energy to small scales and dissipating

EMHD: no energy principle

Whistlers do no work (infinitely stiff lattice, no dynamo in EMHD)

$$\mathbf{v} \cdot \mathbf{j} \times \mathbf{B} \propto \mathbf{j} \cdot \mathbf{j} \times \mathbf{B} = 0.$$

- (in MHD $\mathbf{v} \cdot \mathbf{j} \times \mathbf{B} \neq 0$)
- There is no energy principle in EMHD: cannot change energy internally

 $(\omega - \omega^*) \int dV \mathbf{B} \cdot (\xi \times \xi^*) = 0$ (even with varying density) $\omega = \omega^*$ - neutrally stable

unless
$$\mathbf{B} \cdot (\xi \times \xi^*) = 0$$

Wood, Hollerbach, Lyutikov, 2014

KH-like instability in EMHD



Wood, Hollerbach, Lyutikov, 2014

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KH-like instability in EMHD



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Density-shear instability in electron MHD

- Driven both by B-field and density gradients
 - $\text{ driven by } \quad \frac{B'}{B}\frac{n'}{n} > 0 \\$
 - need $L_n \leq L_B$
 - $k_{\parallel}L_B < 1$
 - growth rate ~ Hall time scale





$\mathbf{B} \cdot (\boldsymbol{\xi} \times \boldsymbol{\xi}^*) = 0$

rotation by whistler



Shearing instability of EMHD

• Shear against rotation in whistler mode, v'<0

$$k_{\rm along B} \le 1/L_{\perp B}$$

• circular - elliptic - linear - instability

Density-shear instability in NSs



Large B-field (fast evolution) Right conditions for instability

Density-shear instability in NSs



Lyutikov 2014

Sidetrack: EMHD turbulence

- Unstable whistlers launched in the crust: non-linear interaction?
- Whistler interaction is very different from Alfven waves
- Whistlers do not interact for
 - co-linear propagation (including counterpropagating case)
 - k₁ = k₂, (but propagating in different directions)

MHD & EMHD turbulence

• MHD: counter-propagating Alfven wave packets interact







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(Weak) EMHD turbulence: different from MHD

$$\begin{aligned} \partial_t n &= \pi \int \left[|V_{0\leftrightarrow 1,2}|^2 f_{k\leftrightarrow 1,2} \delta(\mathbf{k} - \mathbf{k}_1 - \mathbf{k}_2) \delta(\omega - \omega_1 - \omega_2) + 2|V_{1\leftrightarrow k,2}| f_{1\leftrightarrow 0,2} \delta(\mathbf{k}_1 - \mathbf{k} - \mathbf{k}_2) \delta(\omega_1 - \omega - \omega_2) \right] d\mathbf{k}_1 d\mathbf{k}_2 \\ f_{0\leftrightarrow 1,2} &= n_1 n_2 - n(n_1 + n_2) \end{aligned}$$

- 3-way processes are important!
- simple decay favors highly oblique modes
- Very stiff: $\partial_t n \propto k^6$



- Non-universal depends on the injection (coupled to MHD: perp. driving, freezing of MHD - quasi-isotropic driving)
- Quasi-isotropic (given enough time) resonance condition couples very different angles and scales
 - transiently show anisotropy
- Remains weak
- -2 spectrum
- May not reach steady state at all


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Idealized plasma physics problem: NS crusts are different!

EMHD waves are dissipated by plastic deformations of the crust and production of bursts and flares

How magnetars work: Star-quakes vs Solar flares

- Thompson & Duncan: 100 msec ~ shear time scale
 - magnetic field strong enough can break the crust
 - sudden unwinding
 - dissipation in the magnetosphere
 - Needs crust to crack



- Lyutikov: 100 mu-sec ~ Alfven time over the magnetosphere
- slow evolution of crustal fields twists outside field
- kink instability
- dissipation in the magnetosphere
- Crust can respond plastically (or can be infinitely rigid)



I. Star-quake (Thompson & Dunkan)

- Lorentz force $\mathbf{J} imes \mathbf{B}$ induced shear/strain in the NS crust.
- If that strain is larger than critical, the crust cracks
- Due to stratification only rotation allowed.
- A plate rotates, twists the outside B-field flare!
- Shear time scale, 100 msec (flare duration)
- Not clear if crust allows cracking (usually need shear velocity > sound not satisfied in NS crusts).



Assume the crust can crack

Levin & Lyutikov 2012: Even if plastic properties of the crust allow cracking, the release of the elastic energy in magnetic-induced crack is small









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waves



$$\zeta = \zeta_0(x) - (x - vt)\zeta_0'(0)$$



B-field cannot do that!





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Current sheet: jxB that stops the plates!



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$$\partial_t B_x = \partial_z (B_z v_x) = B_z v_0 \delta(z)$$



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Additional condition: continuity of B-field. **Resistivity!**

$$\left(\partial_t - \eta \partial_z^2\right) \left(\partial_t^2 - c_s^2 \partial_z^2\right) \zeta = v_A^2 \partial_t \partial_z^2 \zeta$$

resistive wave shear wave

Magnetic cracking 2 Amplitude of shear wave is negligibly small $\propto \sqrt{\eta}$ Ν -1 -2⁻Displacement ¹ B-field - continuos

Even if crust allows cracking, the post-crack evolution proceeds on slow, resistive time-scale. Only B-field energy within the crack is released (not within the shear waveaffected volume).

Crack will evolve on resistive time scale $\Delta\xi\propto e^{-x^2/_3(\eta t)}$

II. Solar-flare-like events (Lyutikov 2004-2006)

- Lyutikov 2006: 100 mu-sec ~ Alfven time over the magnetosphere
 - slow EMHD evolution of crustal fields twists outside field
 - kink instability
 - dissipation in the magnetosphere
 - Crust can respond plastically (or can be infinitely rigid)





Plastic deformations of the crust

- At low strain rates most materials respond plastically (pure AI)
- plasticity controlled by lattice defects
- At low temperatures both the density of defects and their mobility is controlled by strain (Gillman)

$$\rho_d = \left(\frac{\epsilon}{b}\right)^2$$
 and $v = c_s e^{-\epsilon_{crit}/\epsilon}$

• terminal strain in the lattice

$$\epsilon_t \approx \frac{\epsilon_{crit}}{\ln\left(\frac{c_s t_H}{b}\right)} \approx 10^{-4}$$

- Reached within Maxwell time
- $t_M \approx \epsilon_t t_H \approx \text{months} \text{years}$



B-field in the magentosphere: twisting by EMHD drift, resistive untwisting

- B-field in the crust evolves due to Hall drift
- Strain in the crust is plastically relieved no cracking
- B-field outside is still twisted by the Hall drift $\tau_H = \frac{L^2 \omega_p^2}{c^2 \omega_B} \approx 100 \,\mathrm{yrs} \left(\frac{L}{1 \,\mathrm{km}}\right)^2 \rho_{10} b_{15}^{-1} \,\mathrm{yr}$
- Twist = current -> dissipation
- If resistive time < Hall time: persistent emission $L_X \sim B^3$ - observable only in magnetars $B \sim r^{-2-p} F(\cos \theta), \ 0$
- If resistive time > Hall: flares
 - Small flares medium B-fields
 - Giant flares only in magnetars

Lyutikov 2014

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Flares are magnetospheric instabilitiesSome internal dissipation need

- Post-flare increase of surface emission (~ week): internal dissipation (Shultz et al.)
- "Cut" the flux tube: Alfven pulse reflects, launches whistler pulse $\partial_t \xi_e = i \frac{\omega_B c^2}{\omega_n^2} \xi''_e$ Schrodinger eq.





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Whistler dissipation in the crust

• Strain created by whistler pulse increase with distance



- more coherent at larger distances
- In addition: amplitude grows (smaller speed: larger B) $\delta B \propto n^{1/4}$
- Deep dissipation due to plasticity, at $\rho \sim 10^{10} {\rm g cm^{-3}}$, heat diffuses up to the surface in ~ week

CME model of giant flares

Lyutikov 2003, 2006



Magnetic bubble/flux rope expands, CME is ejected

Flares: Double-T, effective R>>R_{NS}



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Magnetically-trapped fireball



- $k_B T \ll \hbar \omega_B$ all particles on lowest Landau levels $B > \alpha B_Q, \ \alpha = \hbar c/e^2$
- Pair plasma

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In super-strong B-field collisions are more efficient

Collision of particles with the same e/m do not lead to dipolar emission Lyutikov, submitted

• Attractive

- Only parallel acceleration (usually aperp dominates emission)
- Low frequency limit ~ ω^2 (usually ω^0)
- Normalization ~ 3 orders lower
- Only O-mode emitted



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Scattering in B-field



E_x hardly move the electron

$$v_d/c \sim (E/B_0)$$

 $\sigma_O \approx \sigma_T \\ \sigma_E \approx \left(\frac{\omega}{\omega_B}\right)^2 \sigma_T$

- E-mode can escape from deeper-in:
- smaller radius
- higher temperature
- Importance: topologically confined fireball, not a flux tube connected to the surface. Consistent with the idea that topologically-changing instabilities are responsible for flares.

Conclusion

Magnetar flares

- Magnetars' bursts and flares are magnetospheric, not crustal events
- magnetically stressed crust cannot crack efficiently
- crust responds plastically
- Flares: externally triggered events
- Some energy is dissipated inside the NS