



**Recent achievements on KMHD**  
*and applications in the ICM*

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*Collaboration:*

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Turbulence understanding have greatly improved in the past years;

**Aims:** understanding of energy transfer (scales) and diffusion of matter in the ISM

“direct” comparison of observables :

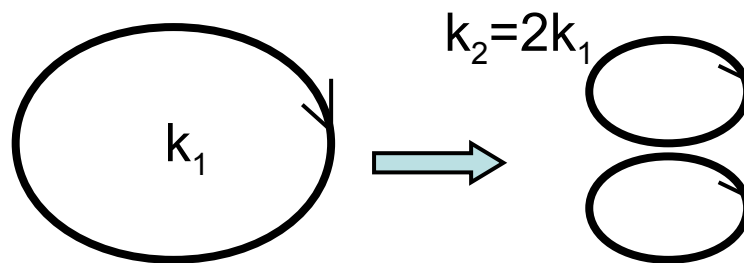
**velocity** (Esquivel et al. + Pogosian et al. + Falceta-Goncalves et al.)

**density** (Kowal et al. + Burkhart et al.)

**magnetic fields** (Falceta-Goncalves et al. + Falgarone et al. + Heitch et al.)

## Turbulence: Kolmogorov's theory

*incompressible fluids:  
Homogeneity + Isotropy + Scale invariance + Locality*



*Energy “flows” from large to small scales:*  $\dot{\epsilon} \approx \delta v_l^2 / \tau_l$

*being*  $\tau_l \approx l / \delta v_l$  *therefore*  $\delta v_l \approx (\dot{\epsilon} l)^{1/3}$  *and, since*

$$\delta v_l^2 \approx \int_{k=1/l}^{\infty} E(k') dk' \text{ we get } E(k) \approx \dot{\epsilon}^{2/3} k^{-5/3}$$

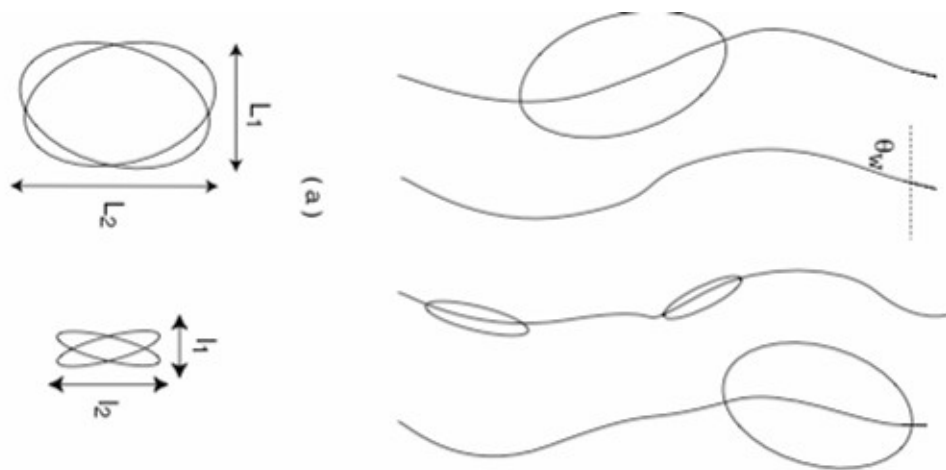
**Magnetized Turbulence: Goldreich-Sridhar theory**

**strong wave-wave interactions**

**Anisotropy!**

$$\tau_A \sim \tau_S \Leftrightarrow l_{\parallel} / l_{\perp} \sim v_A / \delta \omega_l \quad l_{\parallel} \sim v_A \epsilon^{-1/3} l_{\perp}^{2/3} \sim k_{\parallel 0}^{-1} (l_{\perp} / l_*)^{2/3}$$

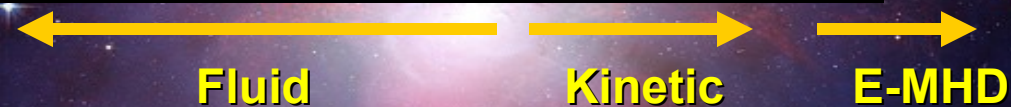
**Kolmogorov spectrum for perpendicular direction**



**Anisotropy is:  
SCALE-DEPENDENT  
and LOCAL**



	$L$	$\lambda_{\text{mfp}}$	$\rho_{\text{ion}}$
ISM	$10^2$ pc	10 AU	$10^5$ km
ICM	100 kpc	1kpc	$10^6$ km



ISM	$v_{ii} \gg \Omega$
ICM	$v_{ii} \ll \Omega$

**Maxwellian dist.**

**Anisotropic pressure**

# Modeling collisionless plasma

... under fluid approximation

**In the collisionless regime**

$$\frac{\partial \rho}{\partial t} + \nabla \cdot (\rho \mathbf{v}) = 0,$$

$$\frac{\partial \rho \mathbf{v}}{\partial t} + \nabla \cdot \left[ \rho \mathbf{v} \mathbf{v} + \left( P + \frac{B^2}{8\pi} \right) I - \frac{1}{4\pi} \mathbf{B} \mathbf{B} \right] = \mathbf{f},$$

$$\frac{\partial \mathbf{B}}{\partial t} - \nabla \times (\mathbf{v} \times \mathbf{B}) = 0,$$

**moments of Vlasov equation**

$$P = p_{\perp} \hat{I} + (p_{\parallel} - p_{\perp}) \hat{b} \hat{b}$$

**Closure**

$$\frac{\partial S_{\perp}}{\partial t} + \nabla \cdot (S_{\perp} \mathbf{v}) = 0,$$

$$\frac{\partial S_{\parallel}}{\partial t} + \nabla \cdot (S_{\parallel} \mathbf{v}) = 0,$$

$$S_{\perp} = p_{\perp} B^{1-\gamma_{\perp}}$$

$$S_{\parallel} = p_{\parallel} (B/\rho)^{\gamma_{\parallel}-1}$$

(Chew, Goldberger, Low 1956)

**Instabilities:**

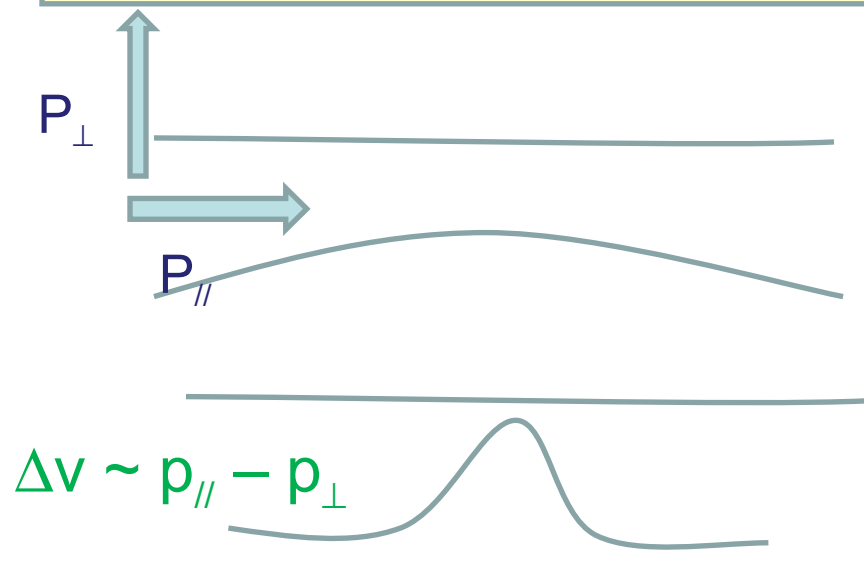
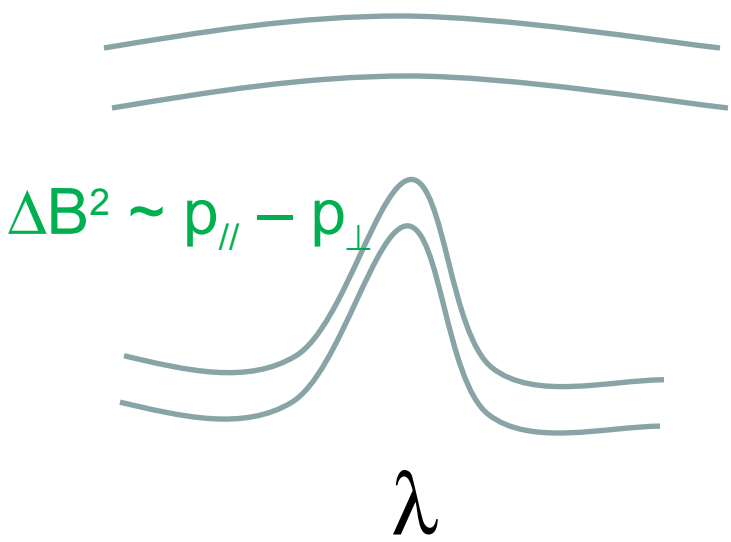
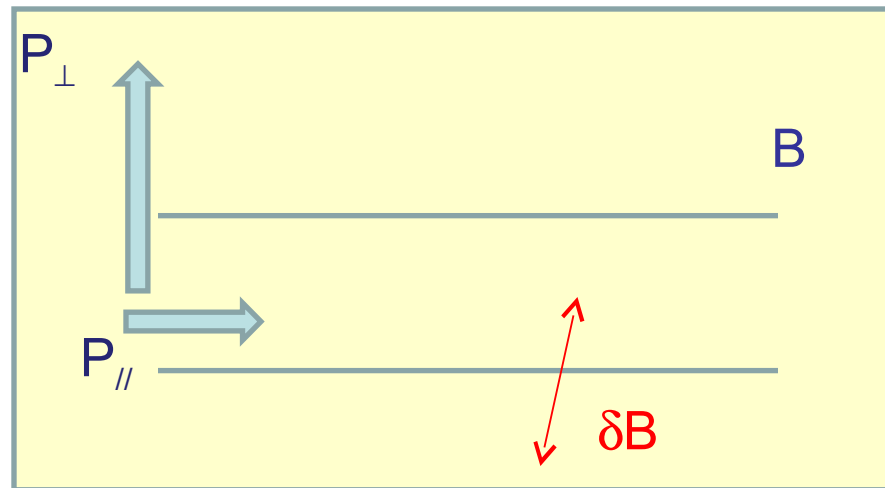
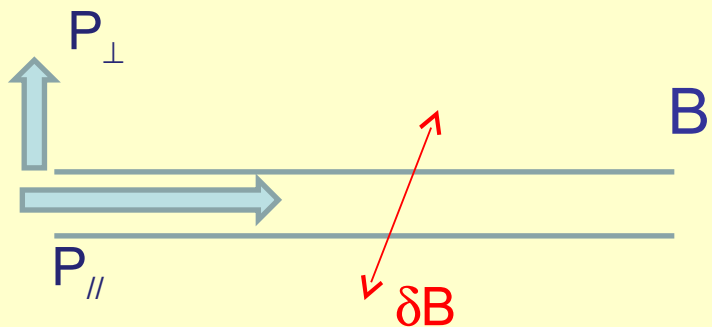
$$\beta_{\parallel} > 2\beta_{\perp}$$

$$\delta p_{\perp} \sim (1 - T_{\perp}/T_{\parallel}) \delta B$$

**Double-isothermal case (the simplest case – not much):**

$$p_{\perp} = a_{\perp}^2 \rho \text{ and } p_{\parallel} = a_{\parallel}^2 \rho$$

**Instabilities (Hasegawa 1969):**



Firehose

Mirror



Kowal, Falceta-Goncalves &amp; Lazarian 2011

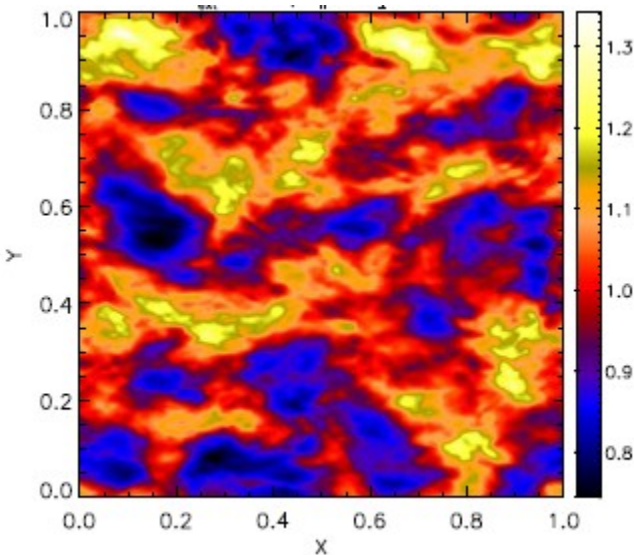
Model	$B_0$	$a_{\parallel}$	$a_{\perp}$	$\xi \equiv a_{\parallel}^2/a_{\perp}^2$	$\mathcal{M}_s \equiv \langle  v /a_{\perp} \rangle$	$\mathcal{M}_A \equiv \langle  v /c_A \rangle$
1	1.0	1.0	2.0	0.25	0.7	0.7
2	1.0	1.0	0.5	4.00	0.7	0.7
3	0.1	0.1	0.2	0.25	7.0	2.0
4	0.1	0.1	0.05	4.00	7.0	2.0
5	0.1	1.0	0.5	4.00	0.7	2.0
6	1.0	0.1	0.2	0.25	7.0	0.7

Res = 256<sup>3</sup>512<sup>3</sup>1024<sup>3</sup>

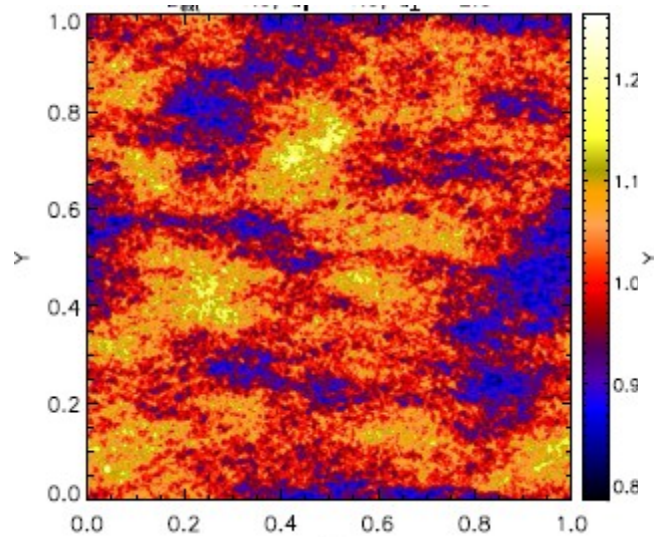
- **Subsonic (supersonic) sub-alfvenic (super-alfvenic)**
- **Firehose / mirror-unstable**

Sub-alfvenic (super-alfvenic are quite similar)

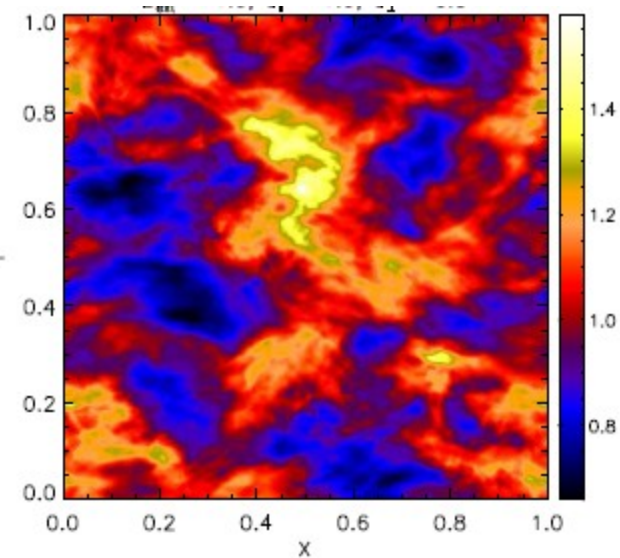
MHD



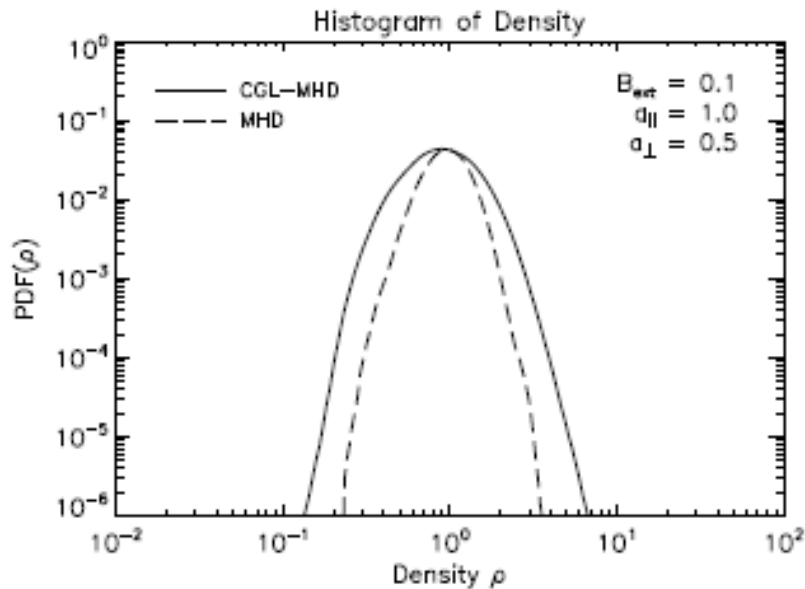
mirror



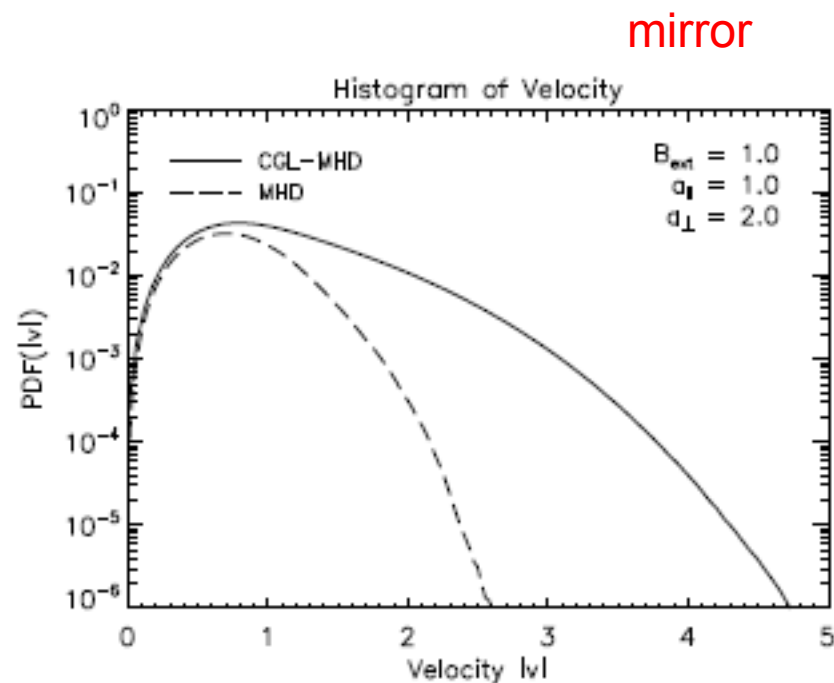
firehose



# Density and Velocity PDFs

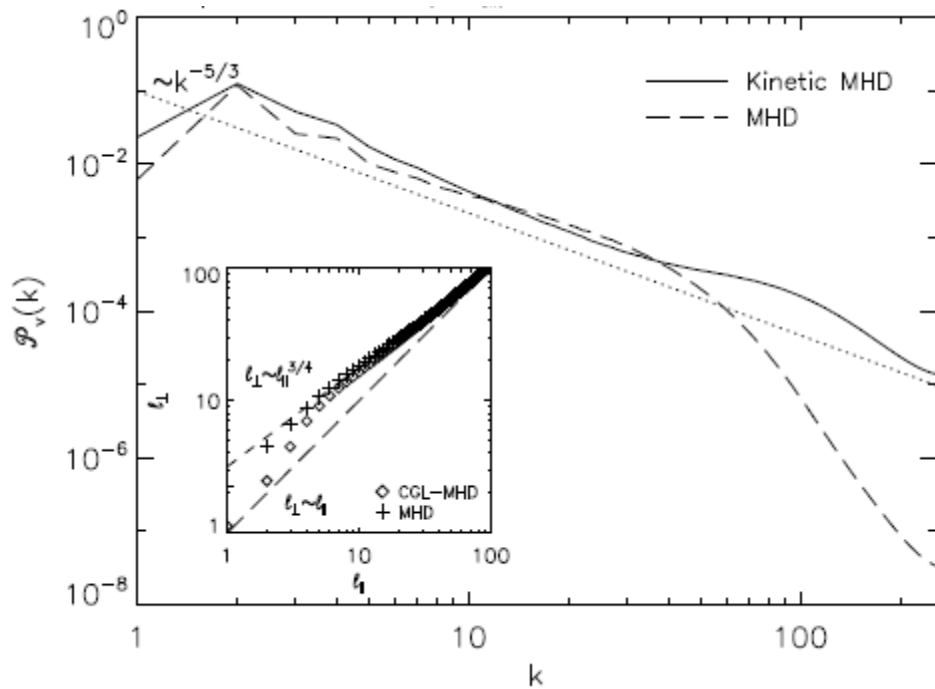


firehose

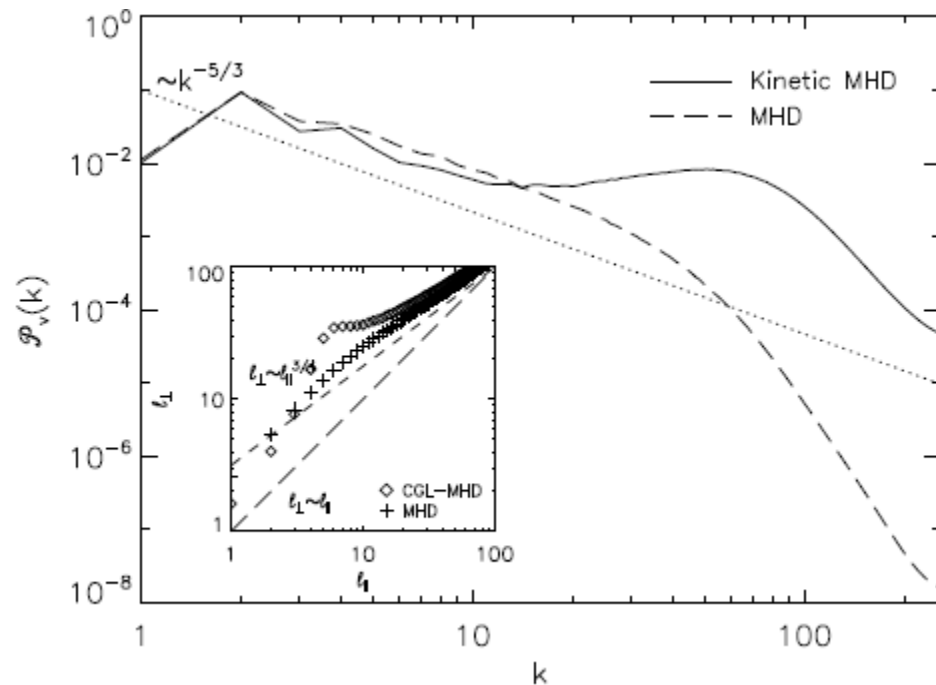


mirror

# Spectra of velocity

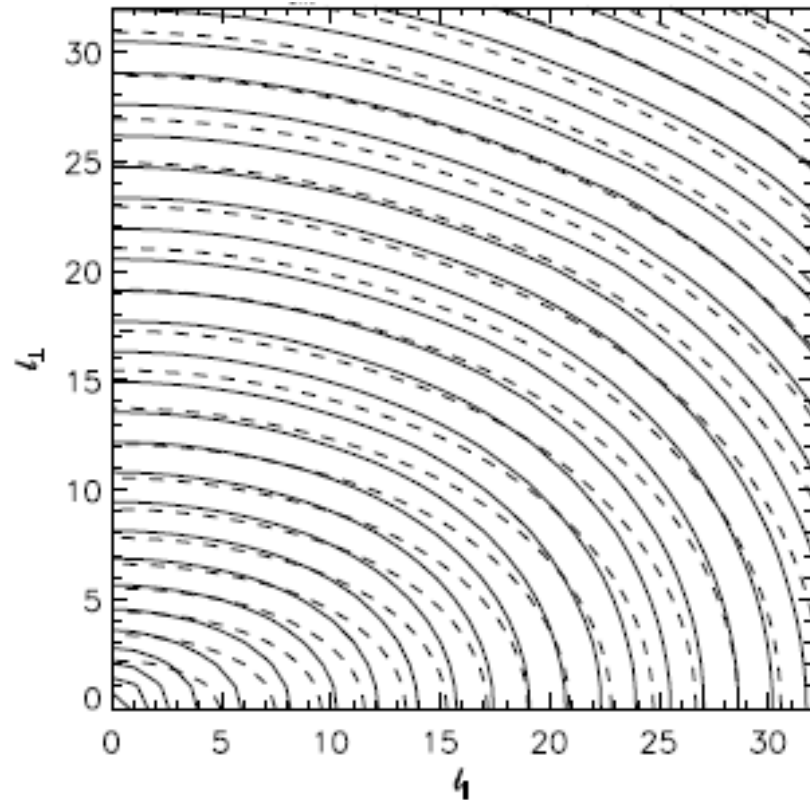


firehose

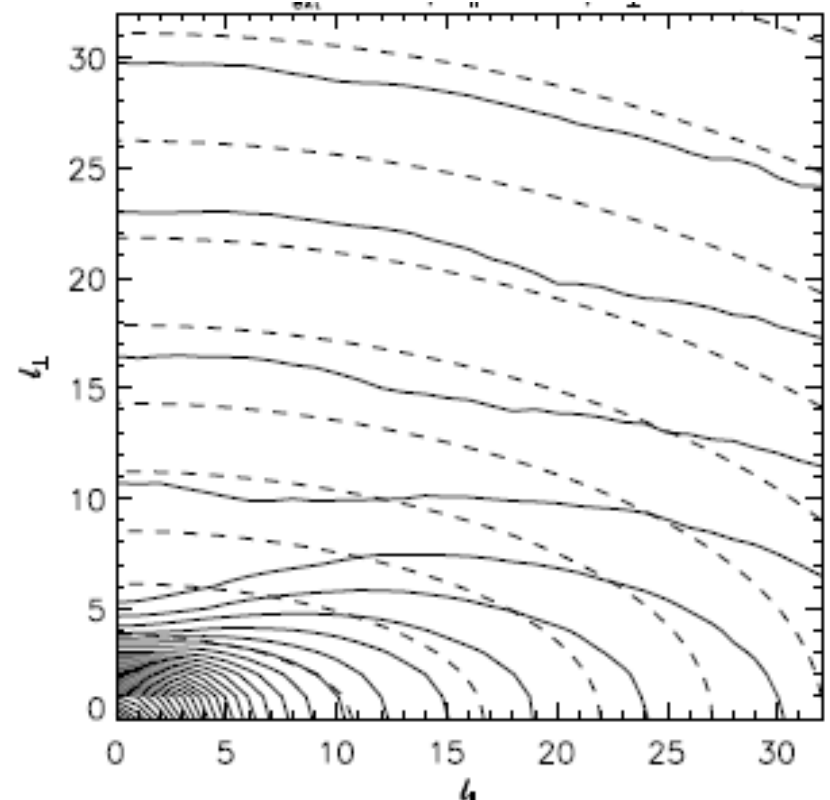


mirror

## 2nd order structure function



firehose



mirror

**Saturation of instability is fast!**

$$\tau_{\text{sat}} \sim 0.1 \tau_{\text{dyn}} (\ll \tau_{\text{alf}})$$

**CGL-MHD turbulent dynamo (can be) is faster than MHD turbulent dynamo (do not miss Santos-Lima's talk)**

**Caveat: double-isothermal closure**

**External/internal processes could sustain pressure anisotropy (cosmic rays, anisotropic heat conduction, etc.)**



# The Intracluster medium

... best application

## The ICM and the cluster total mass

Usually, the ICM is believed to be in quasi-equilibrium :

$$\nabla P = -\rho \nabla \Phi$$

$$M(r) = -3.68 \times 10^{13} T(r) r \left( \frac{d \log \rho_{gas}}{d \log r} + \frac{d \log T}{d \log r} \right)$$

Sarazin (1988)

## Density profile

For an isothermal plasma (isotropic), the emission is free-free:

Cavaliere & Fusco-Femiano (1978)

$$\Sigma(r) = \Sigma_0 \left( 1 + \frac{r^2}{r_c^2} \right)^{-3\beta+1/2} \longrightarrow n_e(r) = n_0 \left( 1 + \frac{r^2}{r_c^2} \right)^{-3\beta/2}$$

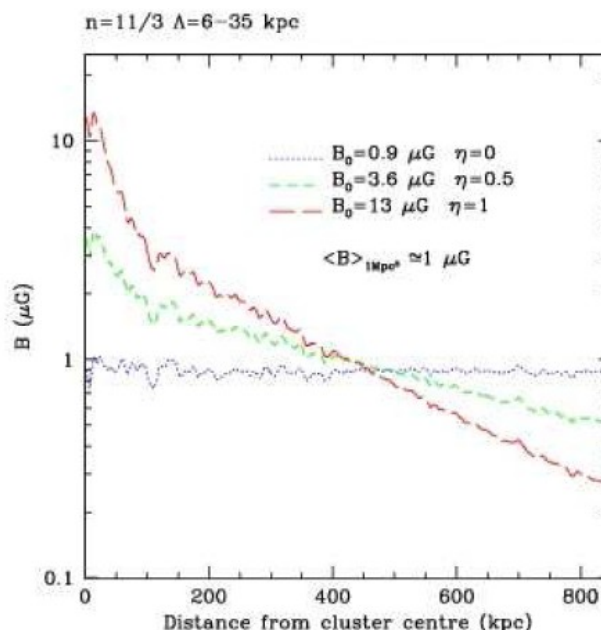
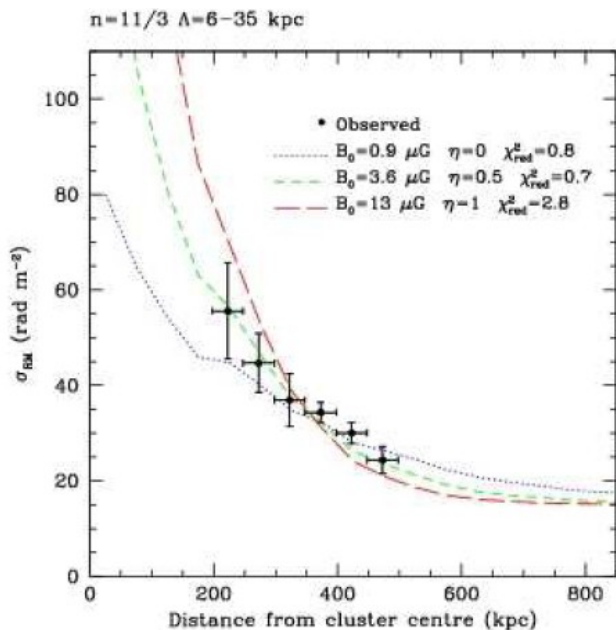
Vikhlinin et al. (2006)

Relaxed clusters present cusps at central region, so the  $\beta$  model is not the best option

# Faraday Rotation in the ICM

$$\Psi_{obs} = \Psi_{in} + \lambda^2 RM$$

$$RM \cong 812 \int_0^{L(kpc)} n_e(cm^{-3}) B_{||}(\mu G) dl \quad (rad / m^2)$$



Guidetti et al. 2008

$$n(r) = n_0 \left( 1 + \frac{r^2}{r_c^2} \right)^{-\frac{3}{2}\beta}$$

+

$$B(r) \propto n(r)^\eta$$

## Turbulence in the ICM

$$K \approx \frac{U_g}{2}$$

$$\sigma \approx 700 - 1000 \text{ km/s}$$

$$T \approx 10^{7-8} \text{ K}$$

$$c_s \approx 300 - 1000 \text{ km/s}$$

Subsonic (or mildly supersonic)

**Injection scales ~ few hundreds of kiloparsecs**

Total energy ~  $10^{63}$  ergs

Energy density ~  $10^{-11}$  erg/cm<sup>3</sup>

**KHMD models**

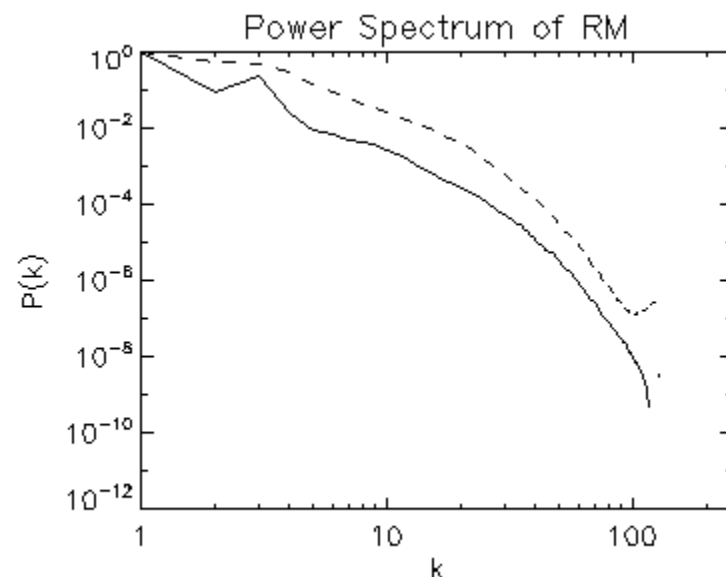
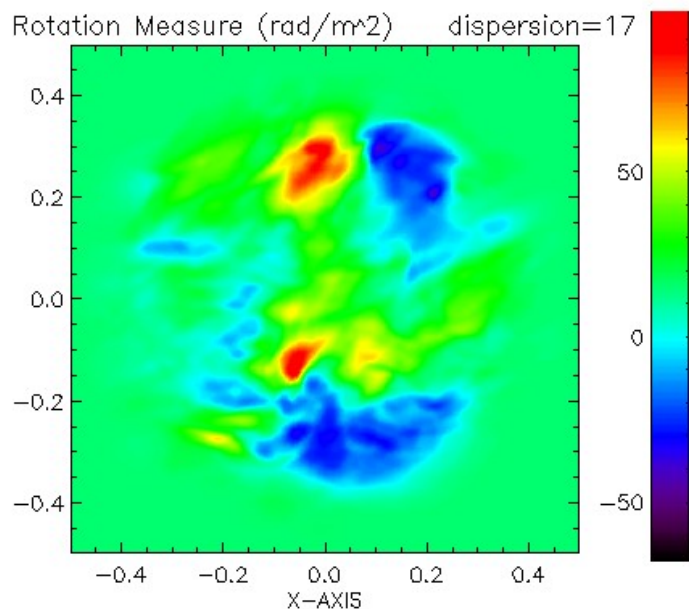
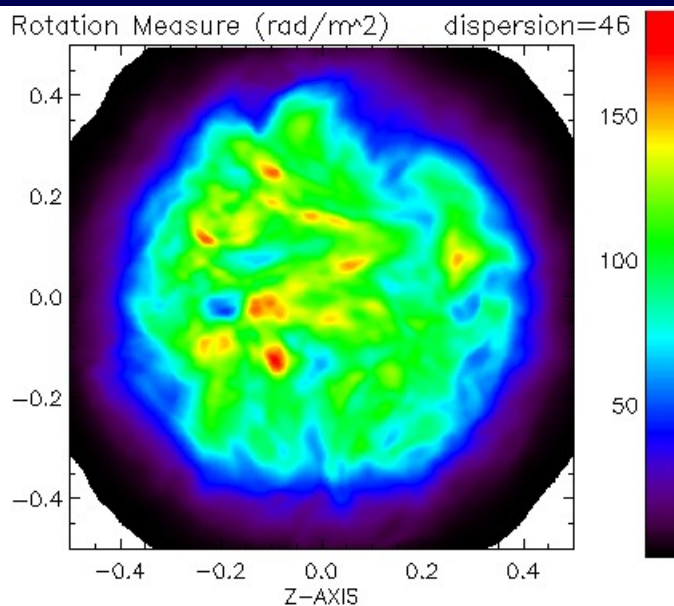
**Probing magnetic fields**

... or turbulent modes



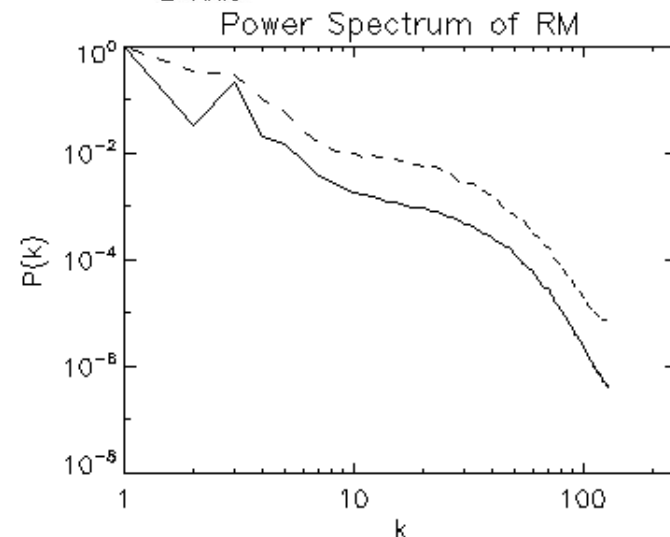
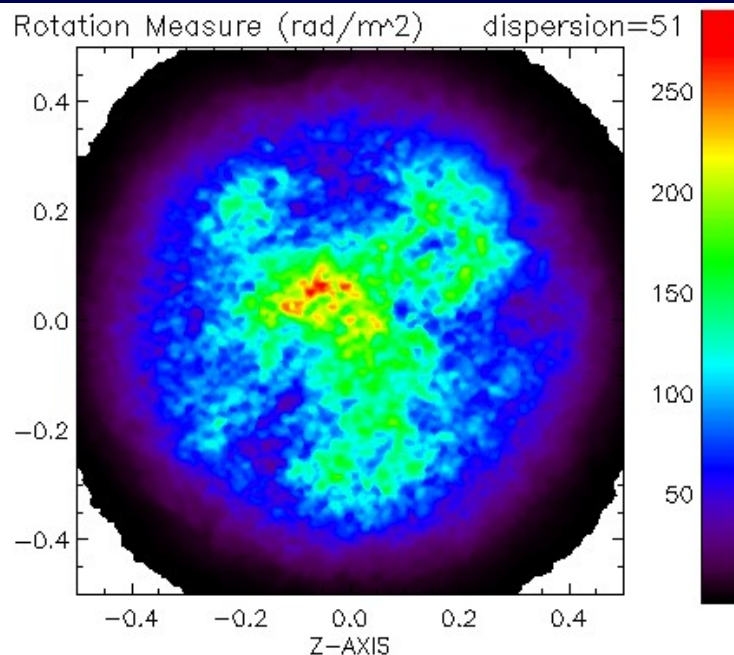
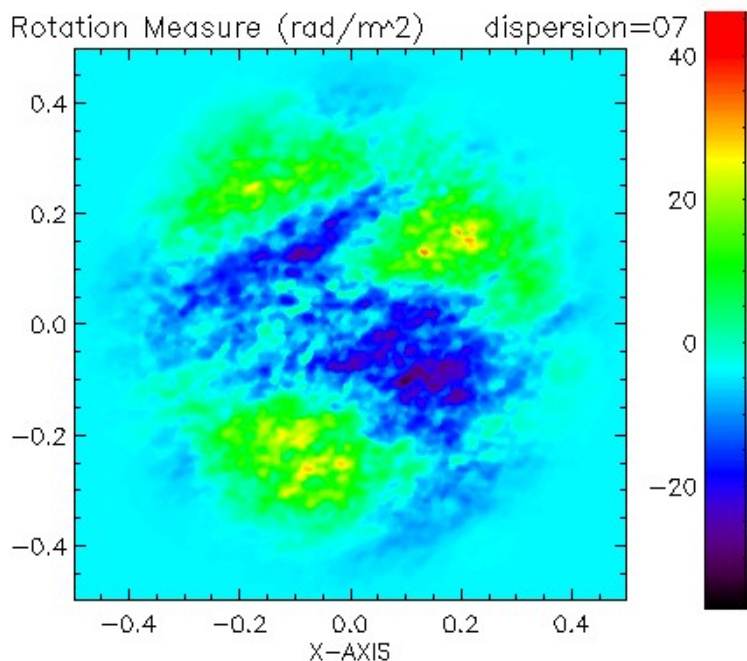
# MHD

- $B \sim 0.1 \mu\text{G}$
- $L \sim 1\text{Mpc}$
- $n \sim 0.01\text{cm}^{-3}$
- **MHD is smooth**



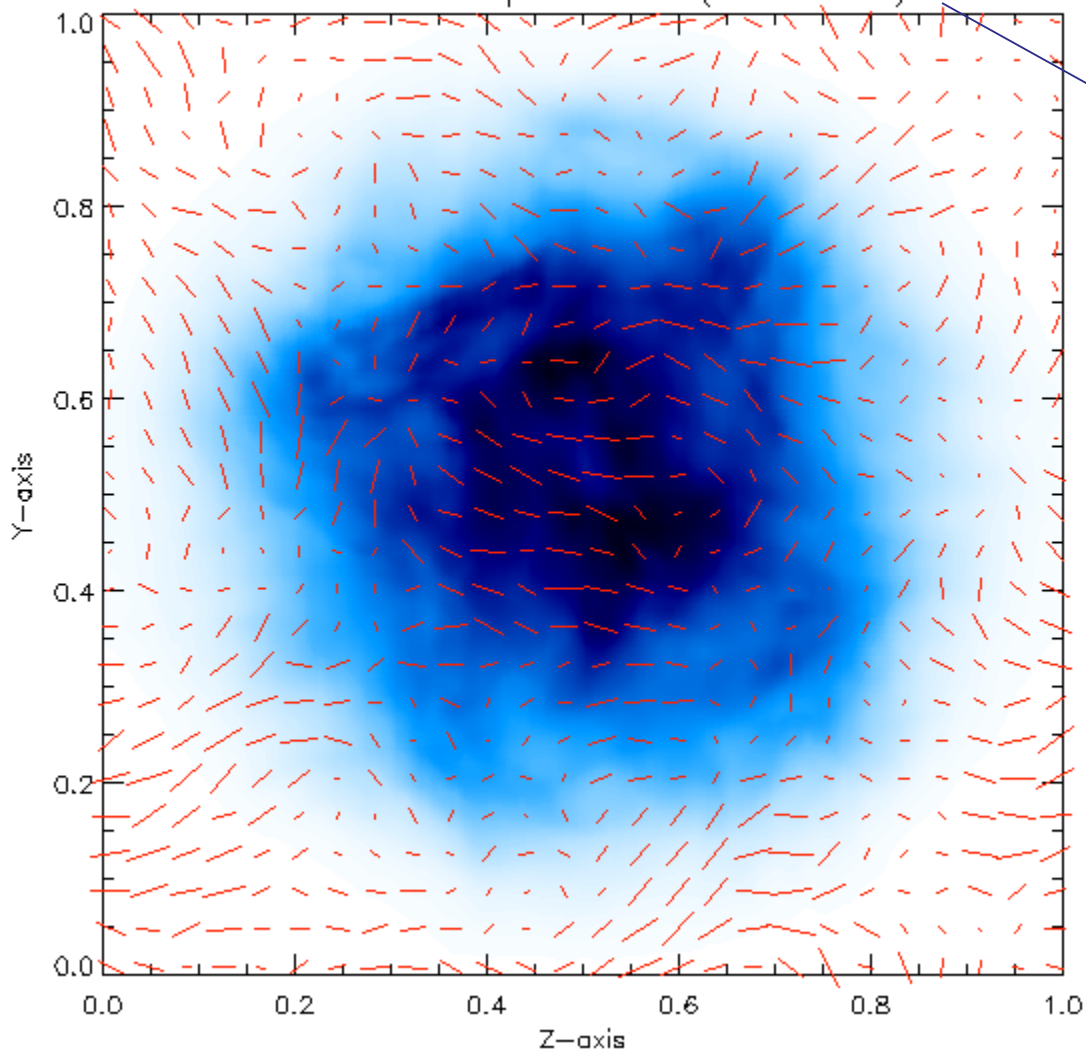
### CGL-MHD

- Compared to the MHD case, power in small scale is increased;
- In the mirror case, RM intensity does not change much;
- In Firehose unstable scenario, RM decreases  $\sim 30 - 70 \%$



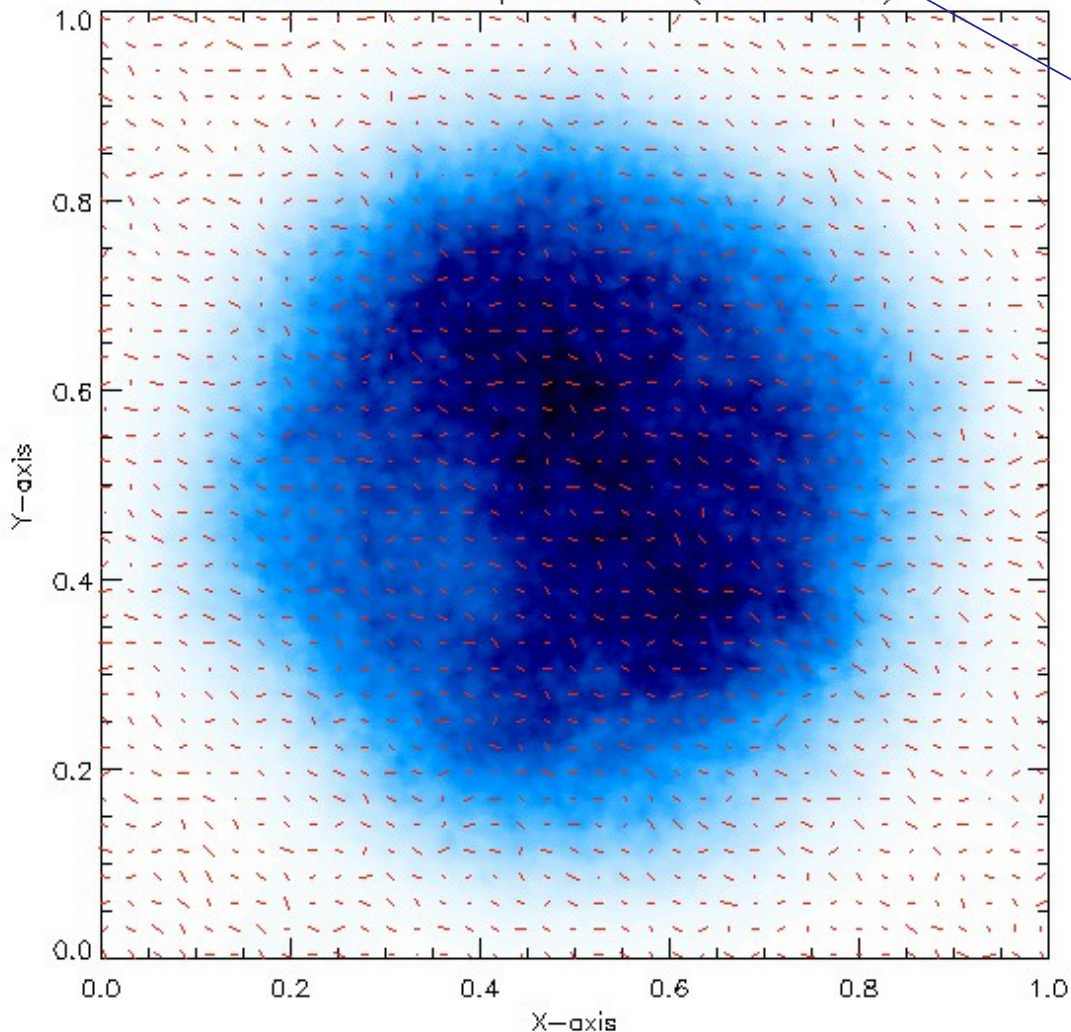
## MHD

Polarization Map LOS=X (Pmax=55%)



- Polarization degree is slightly reduced
- due to the turbulence mostly  
(Falceta-Gonçalves et al. 2008)

## CGL-MHD

Polarization Map LOS=Z ( $P_{\max}=33\%$ )

- Polarization degree is reduced in the Firehose unstable regime
- Cause is the decrease of the decorrelation length due to the instabilities

## Conclusions

**Some kinetic effects taken into account may change the dynamics of the plasma;**

**Depending on the regime, fast increase of magnetic field may take place;**

**As well as acceleration (fluid motions);**

**These occur at smaller scales;**

**Result in modifications of statistics of RM and synchrotron polarization**

**May increase reconnection rate and particle acceleration (seed for 2<sup>nd</sup> order Fermi)**