

Stellar dynamo: new insights from the Kepler mission

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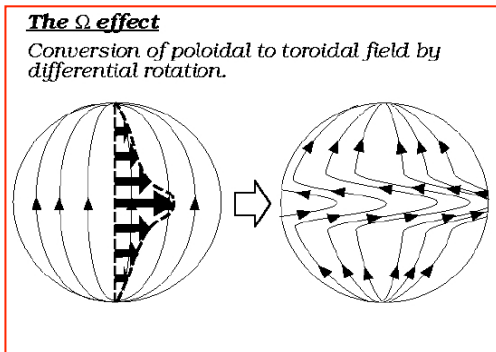
outline

- Review of MF-dynamo in stellar context
- Ground based data
- Dynamo in radiative zone
- The *Kepler* mission
- An explicit example: KIC 8429280

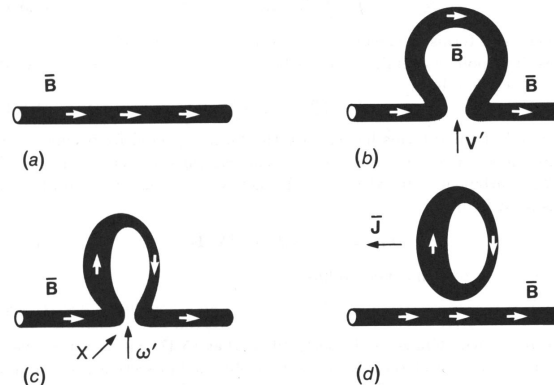
Stellar dynamo models

- Dynamo in convective zone (convective instability)
- Dynamo in the overshoot region – (buoyancy and/or Tayler instab.)
- Dynamo in radiative zone (quasi-interchange instability)
- Dynamo in compact objects (neutron-finger instability)

Ω -effect



α -effect



Mean-field dynamo in a nutshell

$$\frac{\partial \vec{B}}{\partial t} = \nabla \times \left(\vec{u} \times \vec{B} + \vec{\mathcal{E}} - \eta_T \nabla \times \vec{B} \right)$$

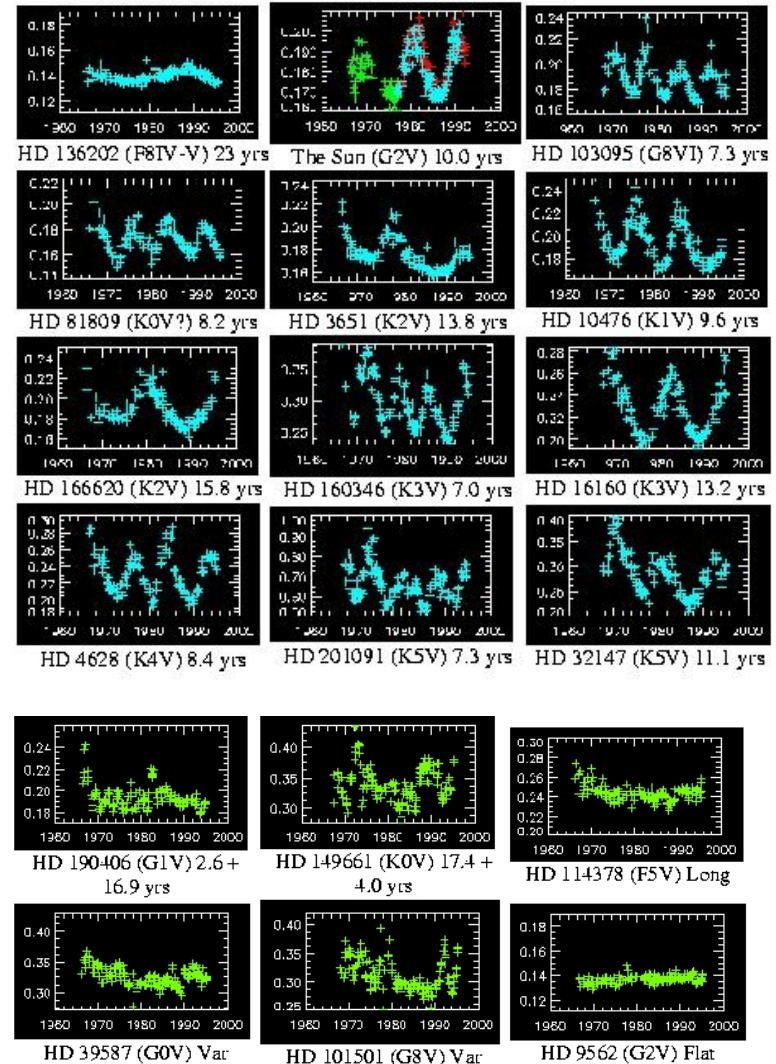
$$\vec{\mathcal{E}} \equiv \langle \vec{u} \times \vec{b} \rangle = \alpha \vec{B} - \eta_T \nabla \times \vec{B} + \dots$$

$$\alpha = \frac{\tau}{3} \langle \vec{u} \cdot \nabla \times \vec{u} \rangle \quad \text{Kinetic helicity – homogeneous turbulence}$$

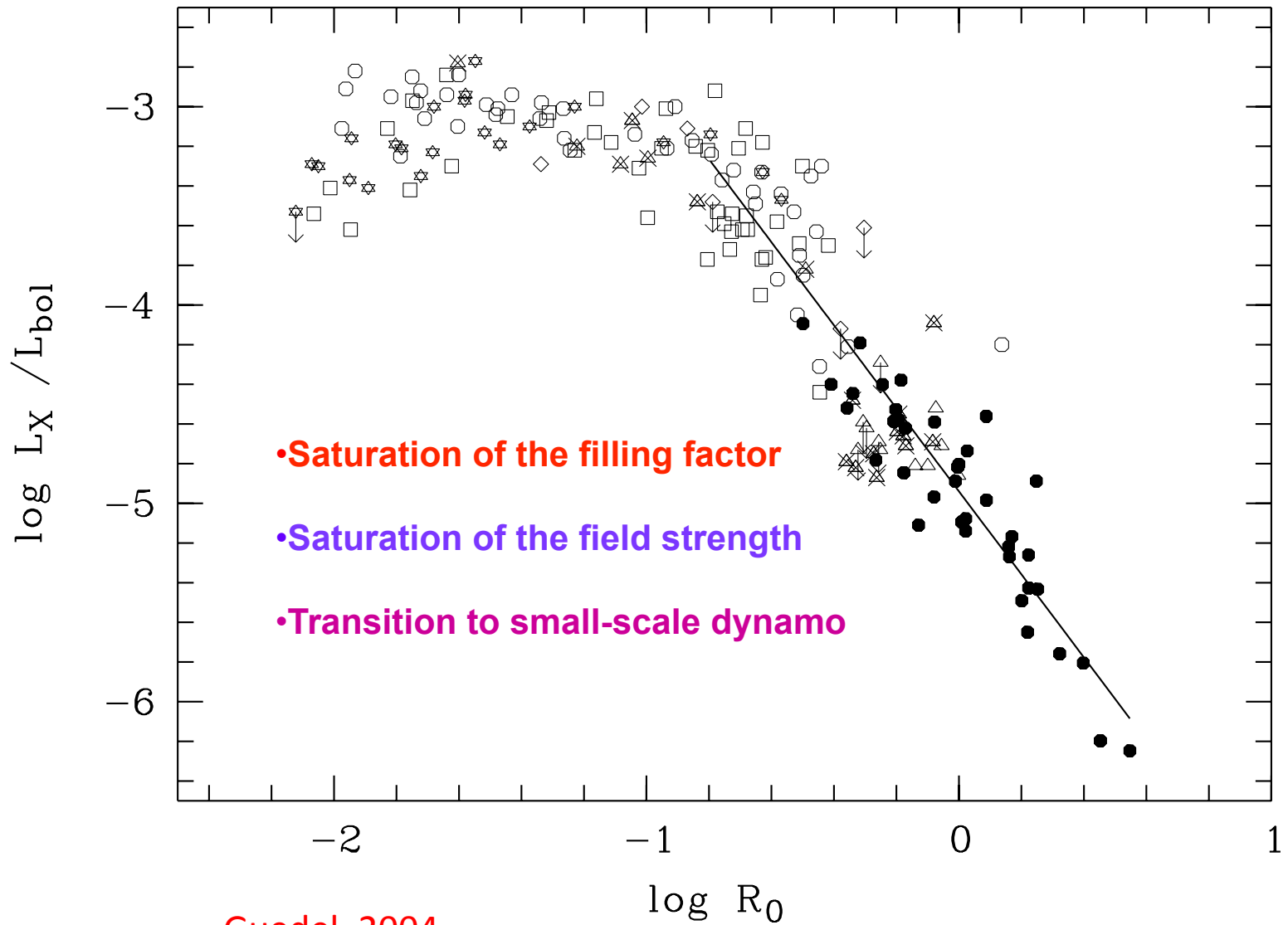
$$\alpha = \frac{\tau}{\rho} \langle \vec{b} \cdot \nabla \times \vec{b} \rangle \quad \text{Magnetic cross-helicity}$$

Magnetic activity in stars

- Late-type stars of solar type also exhibit magnetic activity
- Can be detected by Ca II HK emission profiles
- Mount Wilson survey shows a wide variety of behaviour
- Activity and modulation increases with rotation rate (decreases with Rossby no. Ro)



Activity-rotation relationship



Guedel, 2004

Stellar differential rotation

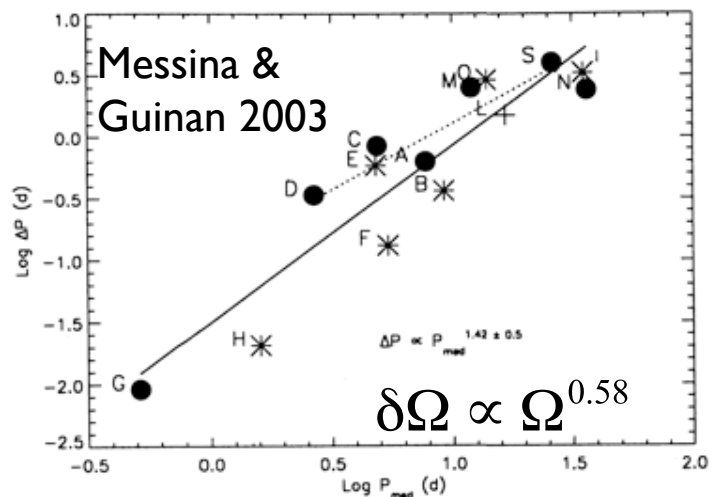
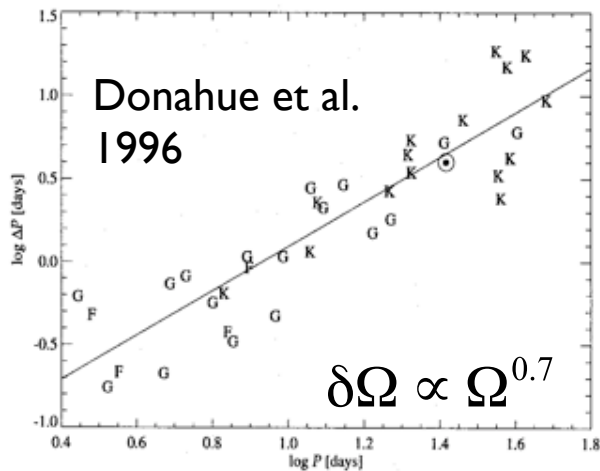
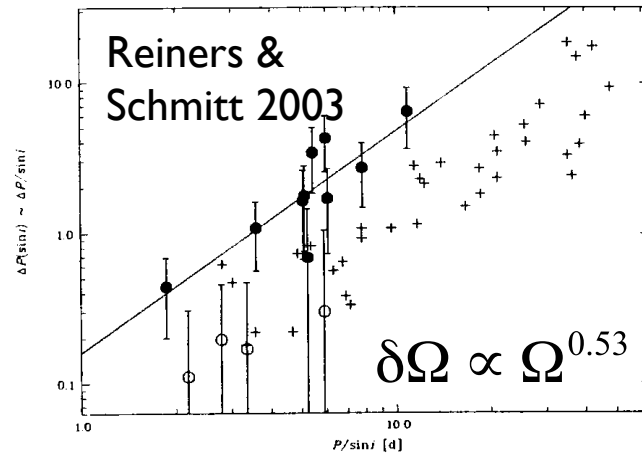
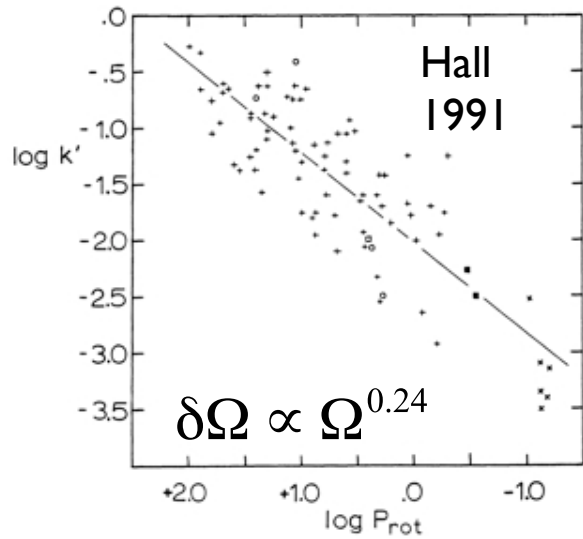


FIG. 3.—Range of observed rotation periods vs. $\log \langle P \rangle$. Least-squares fit of these data yields $\Delta P \propto \langle P \rangle^{1.3 \pm 0.1}$ (correlation coefficient $r = 0.90$).

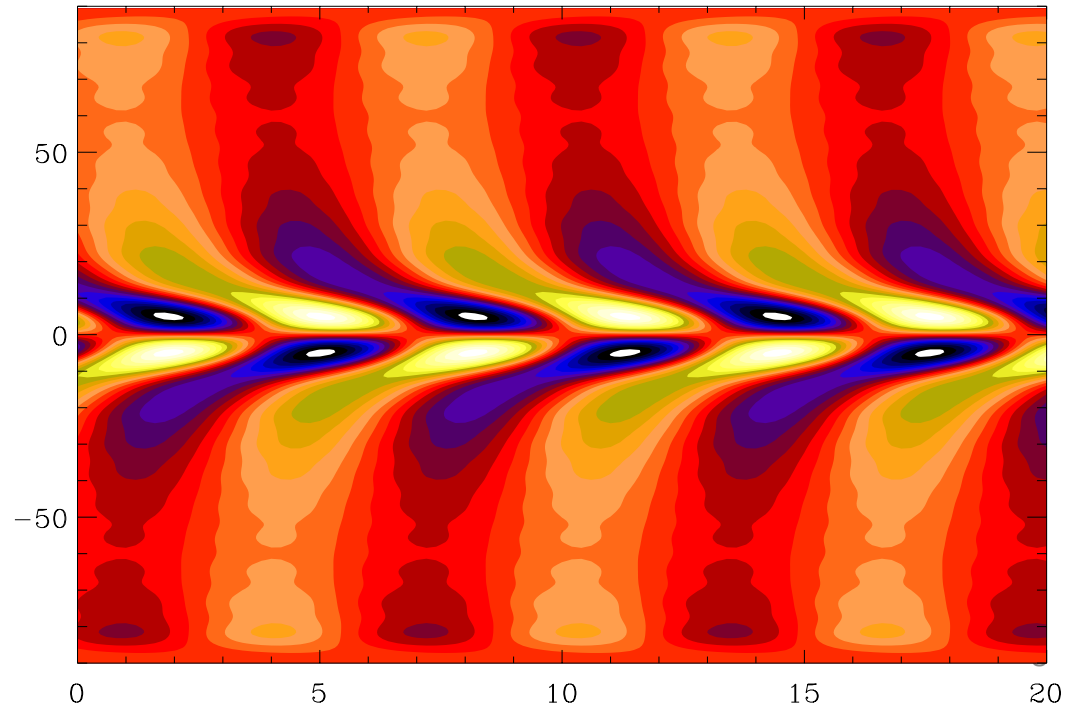
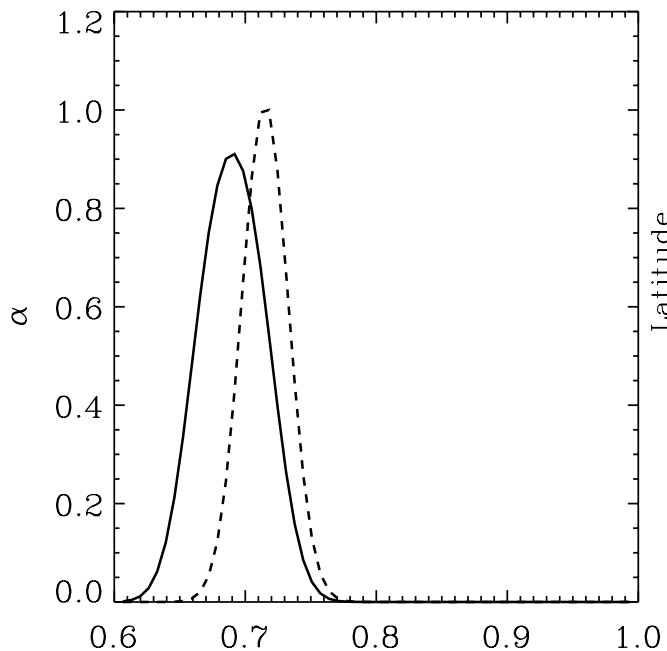
Dynamo in radiative zone

- Based on the Tayler instability: (Spruit 1999, Spruit 2000, Braithwaite 2006)

$$\alpha = \frac{\tau}{\rho} \langle \vec{b} \cdot \nabla \times \vec{b} \rangle$$

- The key question is how to close the dynamo loop (Mathis, Brun, Zahn, 2010)

- Or, how to produce a “magnetic” alpha-effect (see Ruediger, Kitchatinov, Elstner, arXiv-1107.2548)

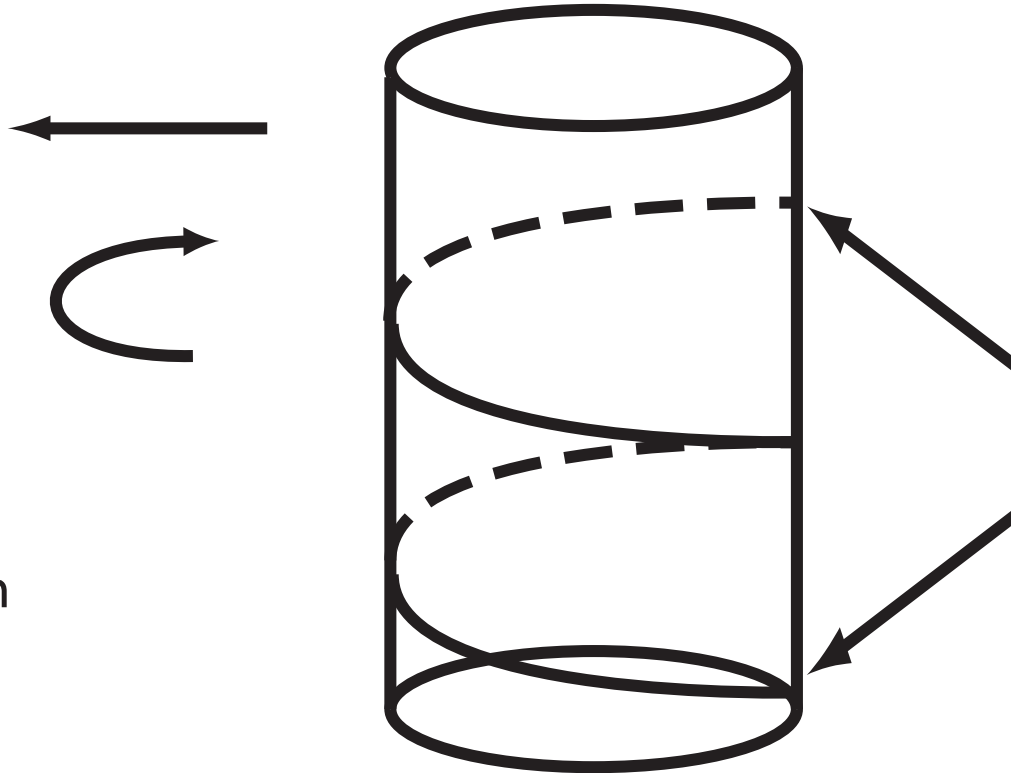


Consider an idealized geometry: static MHD column model

pressure
+
curvature

=

pressure - driven
instability



Twist > a few
rotations
=
current - driven
instability

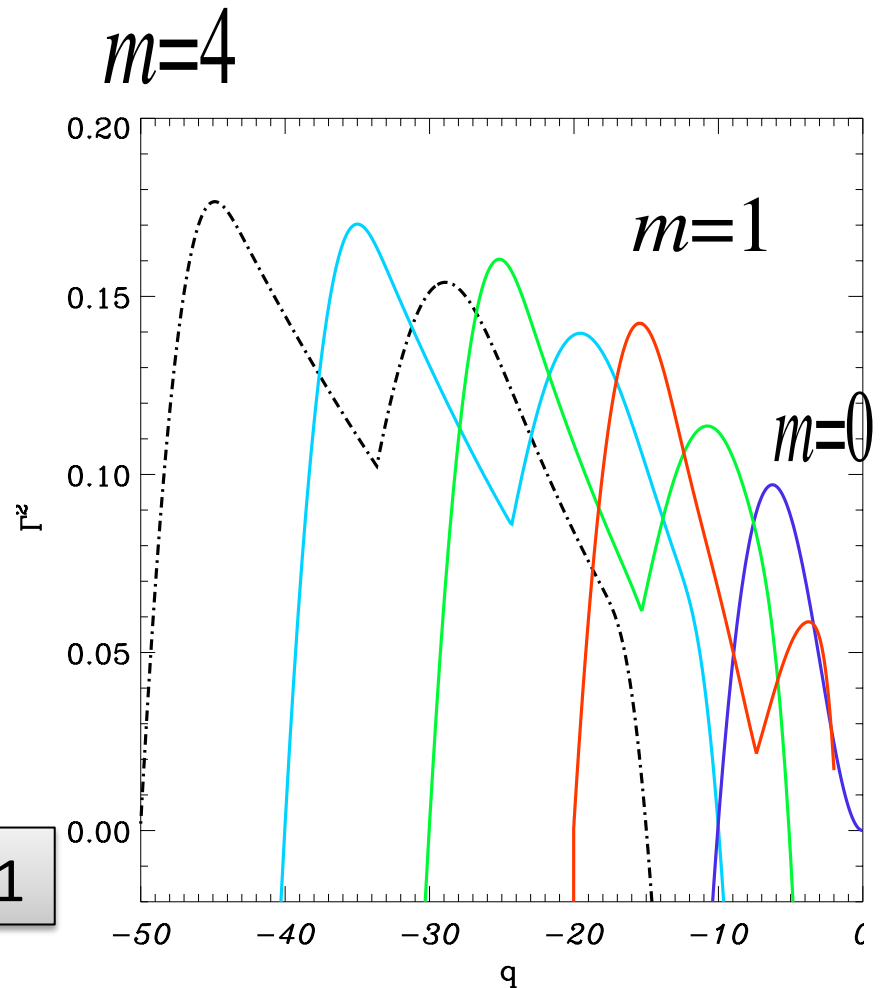
$$\omega_A = \frac{1}{\sqrt{4\pi\rho}} \left(k_z B_z + \frac{m}{s} B_\varphi \right) \approx 0$$

Quasi – interchange instability: Friedberg, 1970 – Goedbloed, 1971

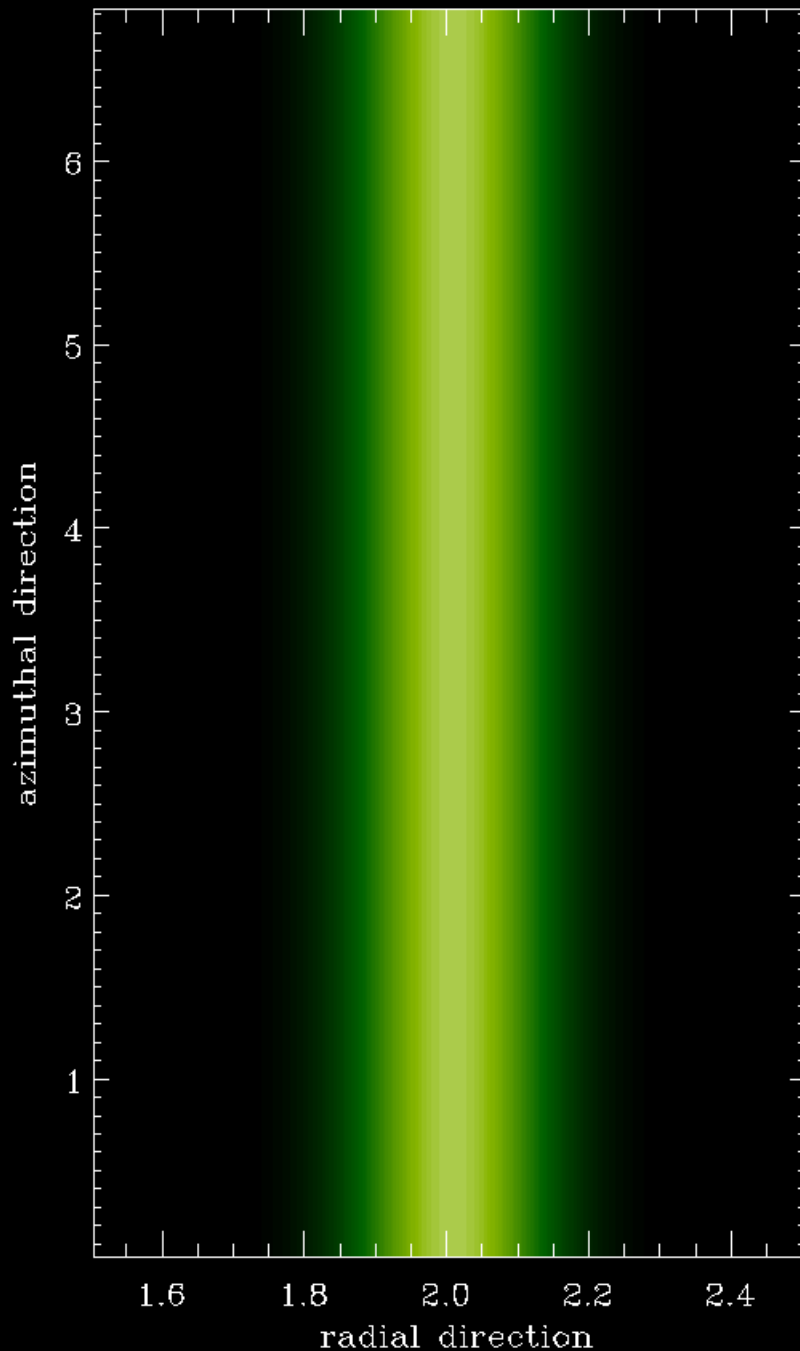
$$\epsilon = \frac{B_z}{B_\varphi} = 0.1$$

- $m \rightarrow -m$ and $B_z \rightarrow -B_z$ symmetry!
- $m > 1$ in general if B_z is not zero!
- Does this trend saturate? Note the resonant character.

Bonanno and Urpin, A&A 2008,2011



time= 0.0000000



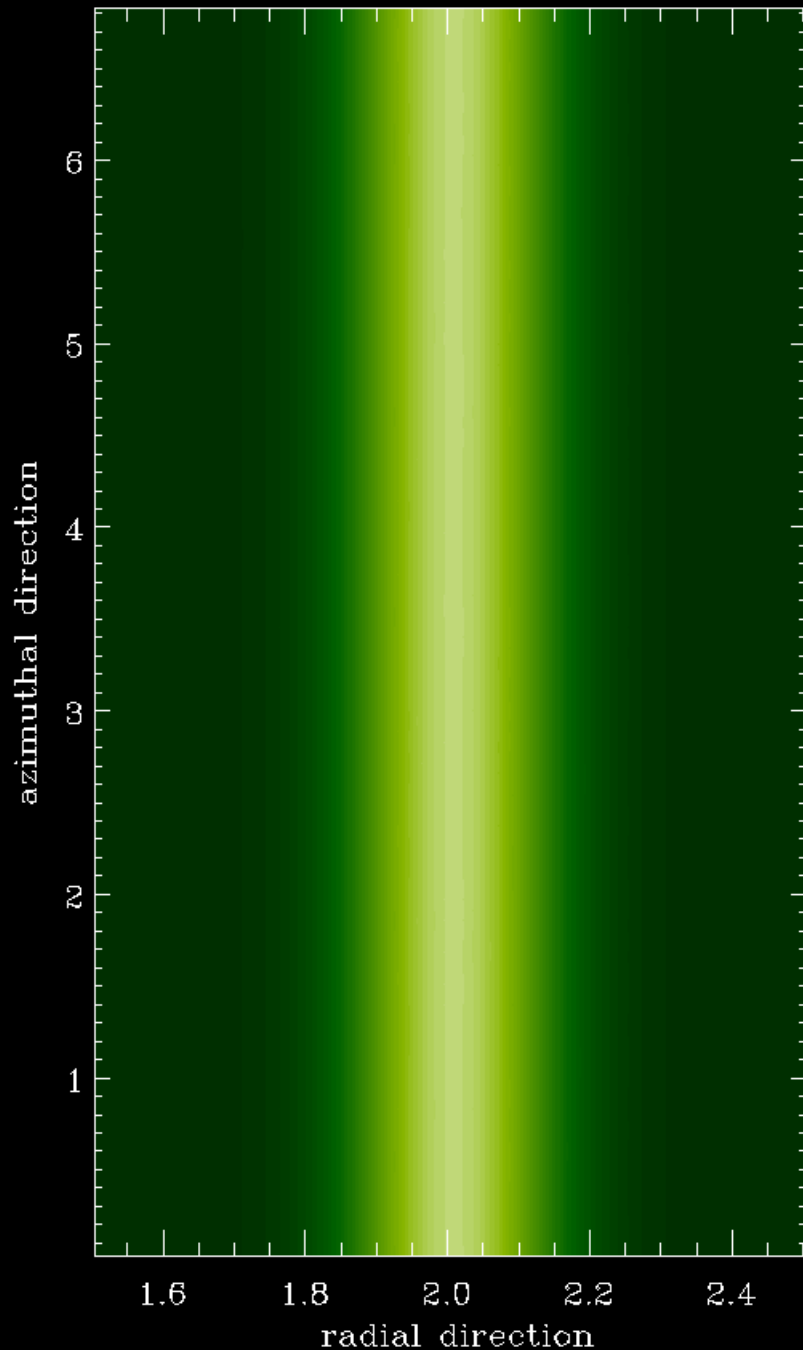
$$B_{\phi} = b_0 \frac{s}{s_0} \exp \frac{-(s - s_0)^2}{\sigma}$$

Balance this basic state with either gradient of pressure, or external force (gravitational potential).

$$\epsilon = 0$$

In this case a mode with $m=1$ dominates the non-linear evolution.

time= 0.12821970

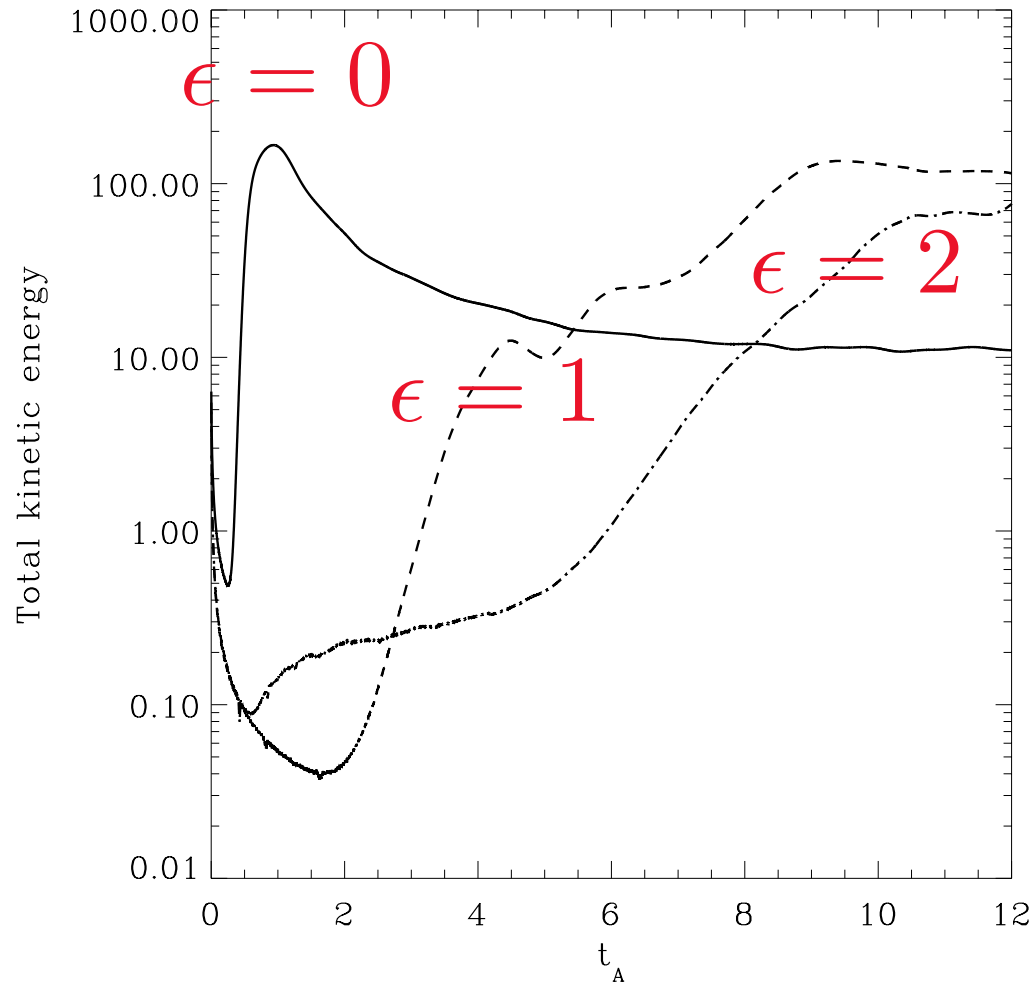


$$B_\phi = b_0 \frac{s}{s_0} \exp \frac{-(s - s_0)^2}{\sigma}$$

$$\epsilon = 2$$

In this case a mode with $m=6$ dominates the non-linear evolution. Similar selection occurs for the vertical wavenumber!

Kinetic energy evolution



$\epsilon = 2 \rightarrow m = 6$
 $\epsilon = 1 \rightarrow m = 3$
 $\epsilon = 0 \rightarrow m = 1$

Dynamo in PNS stars!

▪ **strong instabilities driven by lepton number gradients and temperature gradients**

$$t \sim 40 \text{ s}$$

$$\Omega \cong 1000 \text{ rad/sec}$$

(This is ten times as fast as young pulsar accompanied with SNR (spin period $\sim 10\text{msec}$))

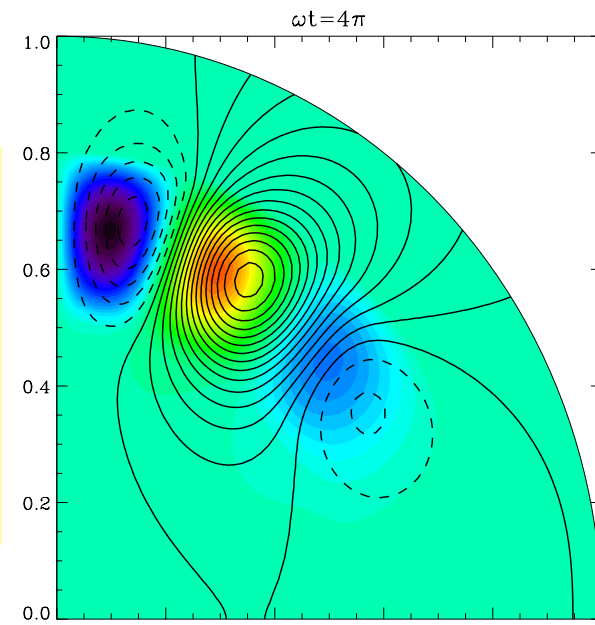
▪ **The features of pulsar suggested by observation**

Magnetic field of young pulsar $B \cong 10^{12-13} \text{ G}$

➔ PNS are accompanied with magnetic fields

- Possibility of dynamo action (Bonanno & Urpin 2005,2006)
- Strong fields are generated with $B_p/B_{\phi} = O(1)$
- Possibility of explaining magnetars magnetic fields
- Now consistent with observations (Halpern and Gottlieb, ApJ2010, PSR J1852+0040, *anti-magnetar*)

(Typical PNS - MF)



The *Kepler* Mission

1.4m primary mirror

Earth-trailing orbit

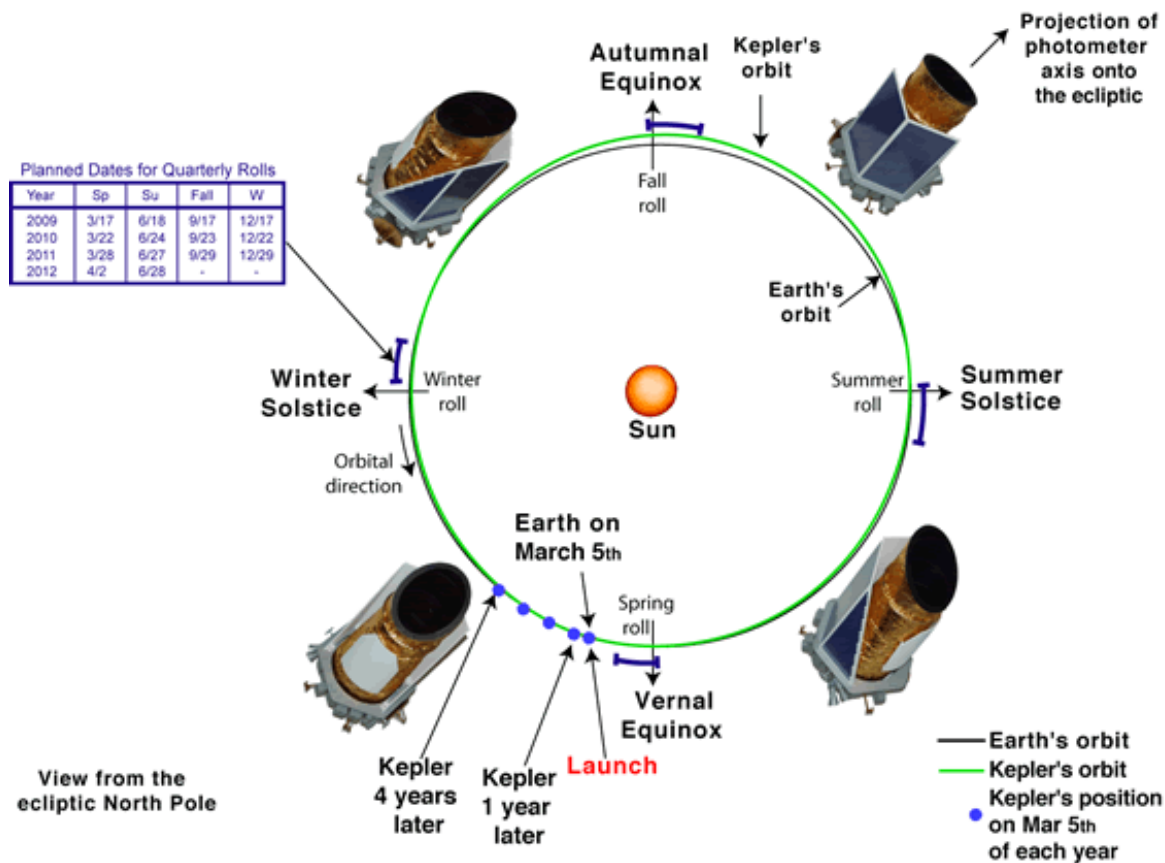
Mission lifetime of at least 3.5 years continuously viewing the same region of sky.

Vast (0.9 m across) broadband (4300-8900 Å) optical CCD array

105 square degrees of sky in Cygnus-Lyra region.

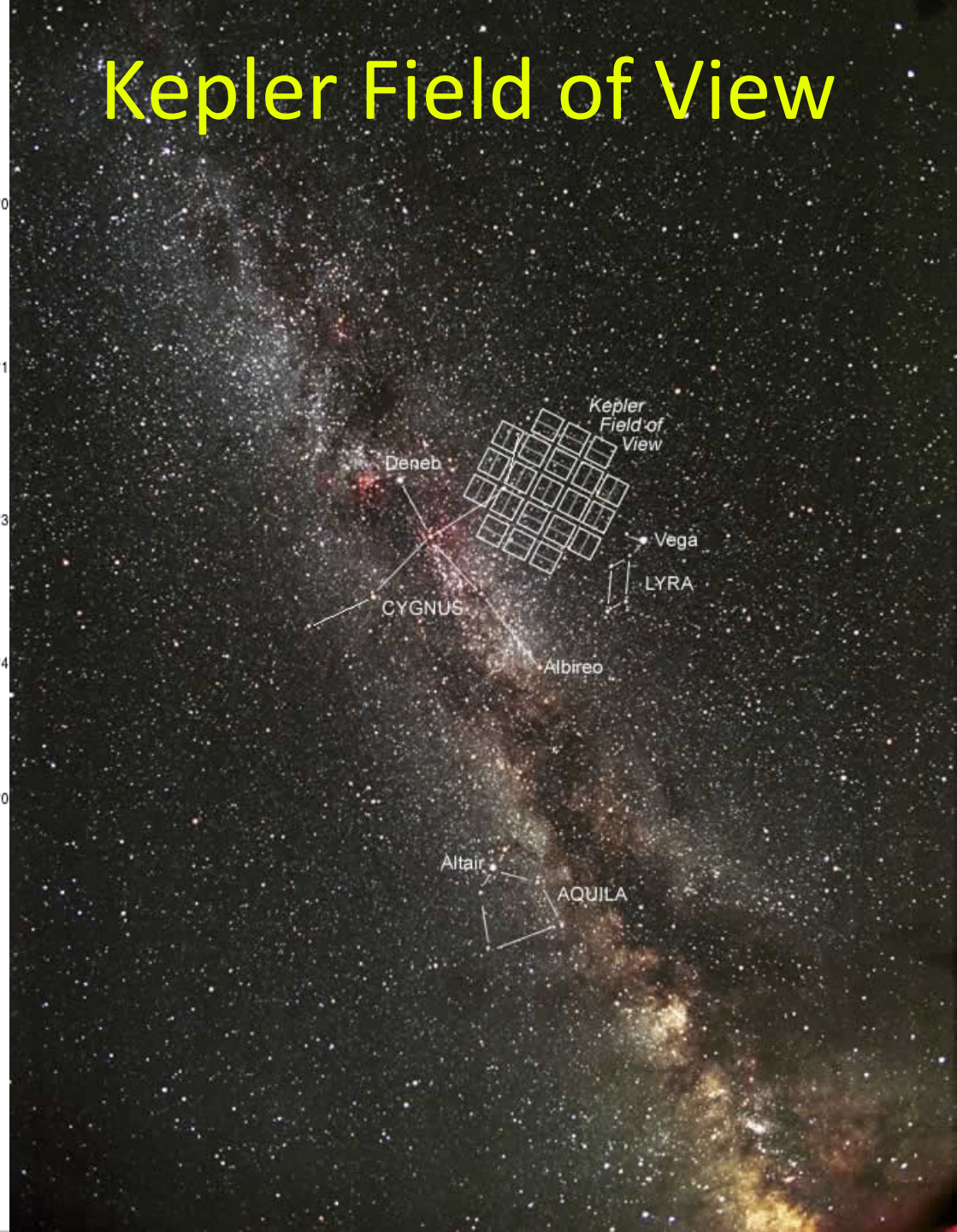
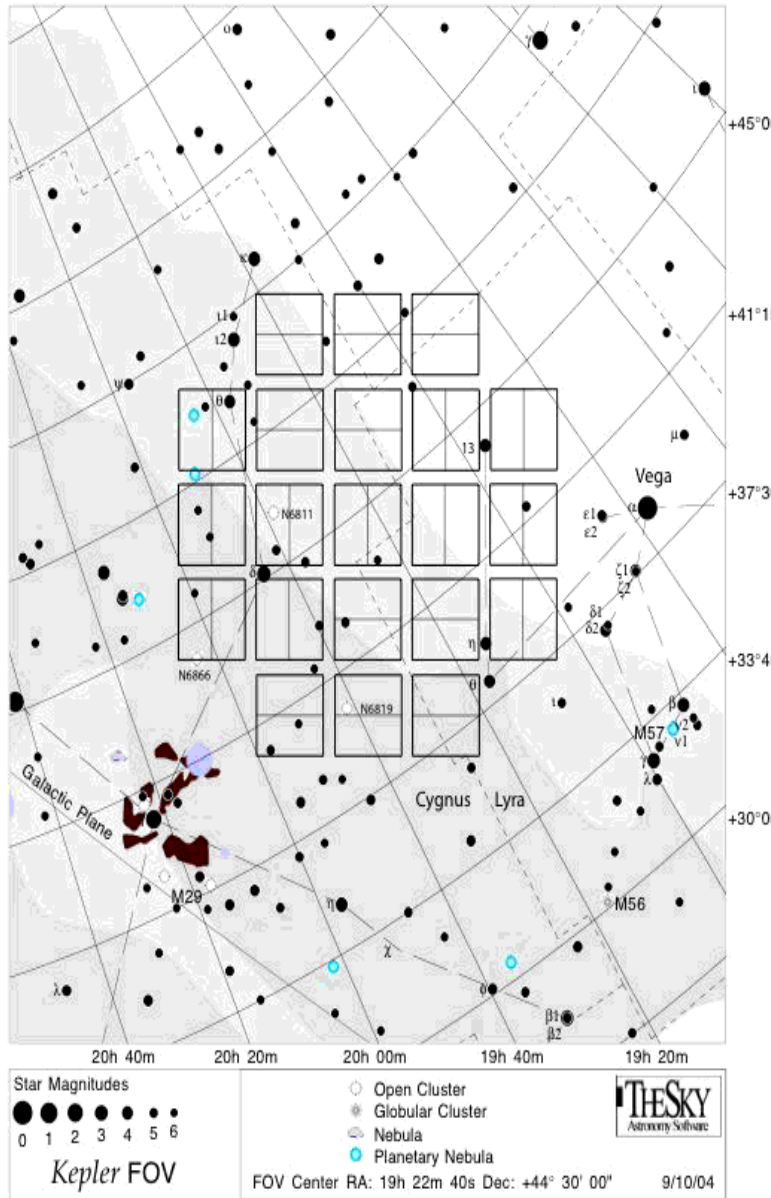
Long (30 min) and short (1 min) data cadence derived by summing 6 sec images.

Primary goal is detecting Earth-like planets through transit observations.



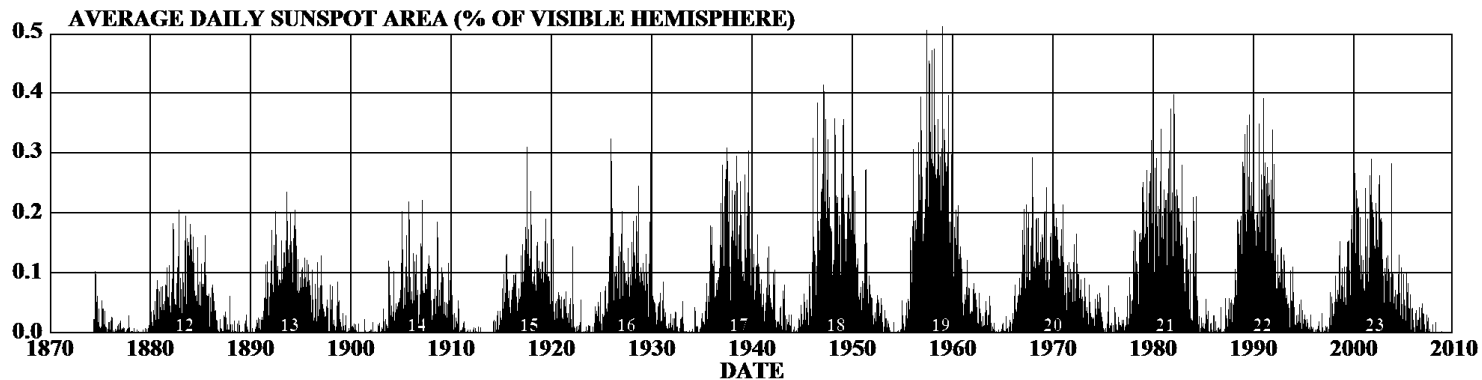
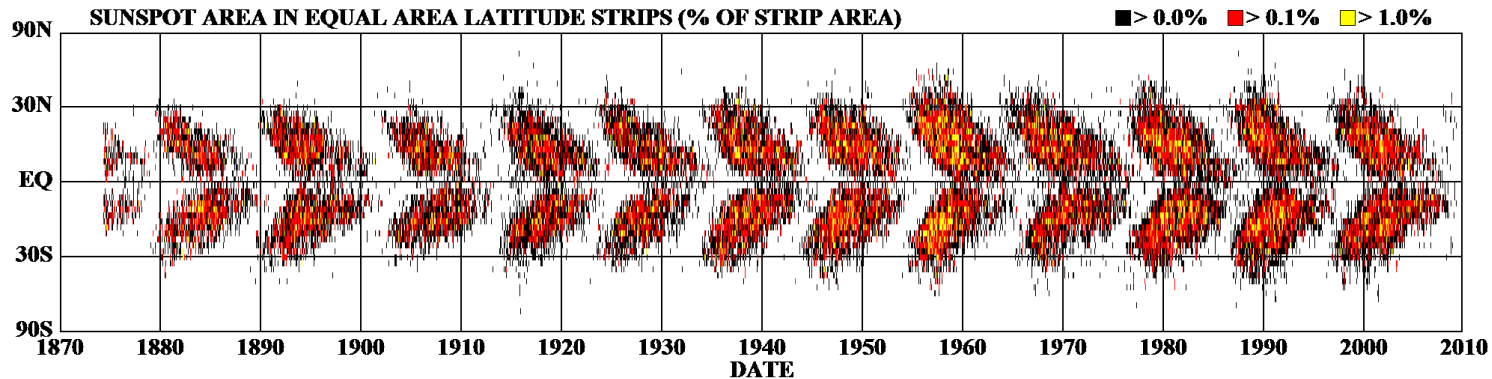
Source: NASA *Kepler* website

Kepler Field of View



Solar butterfly diagram

DAILY SUNSPOT AREA AVERAGED OVER INDIVIDUAL SOLAR ROTATIONS

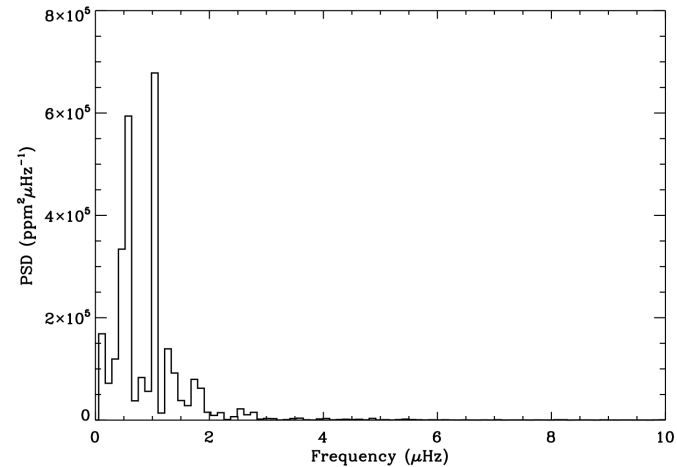
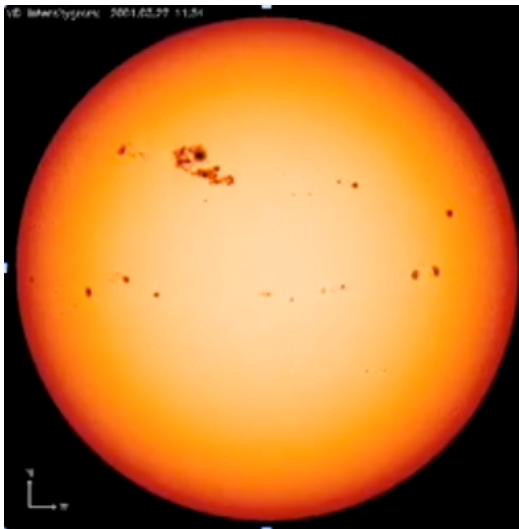
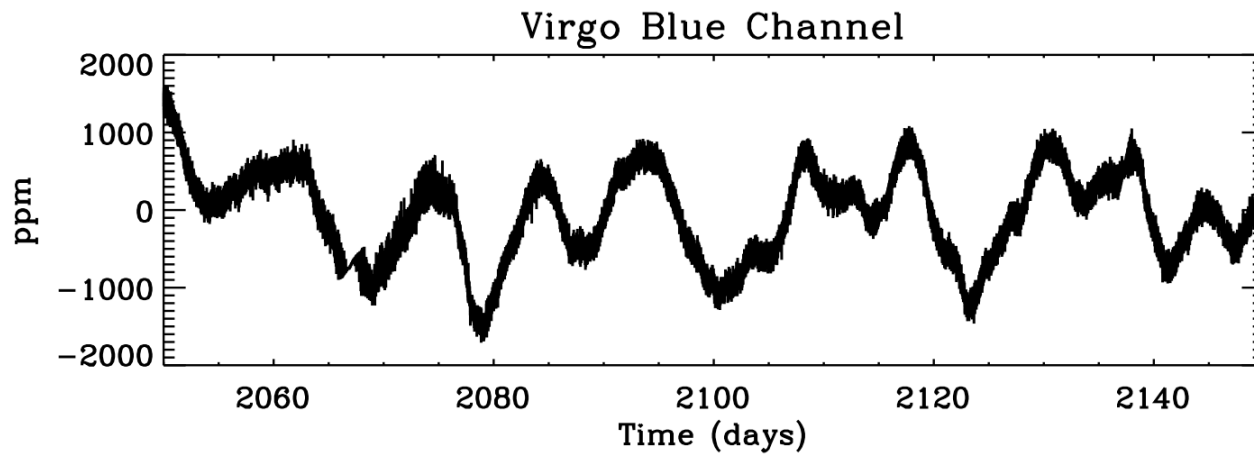


<http://solarscience.msfc.nasa.gov/>

HATHAWAY/NASA/MSFC 2009/05

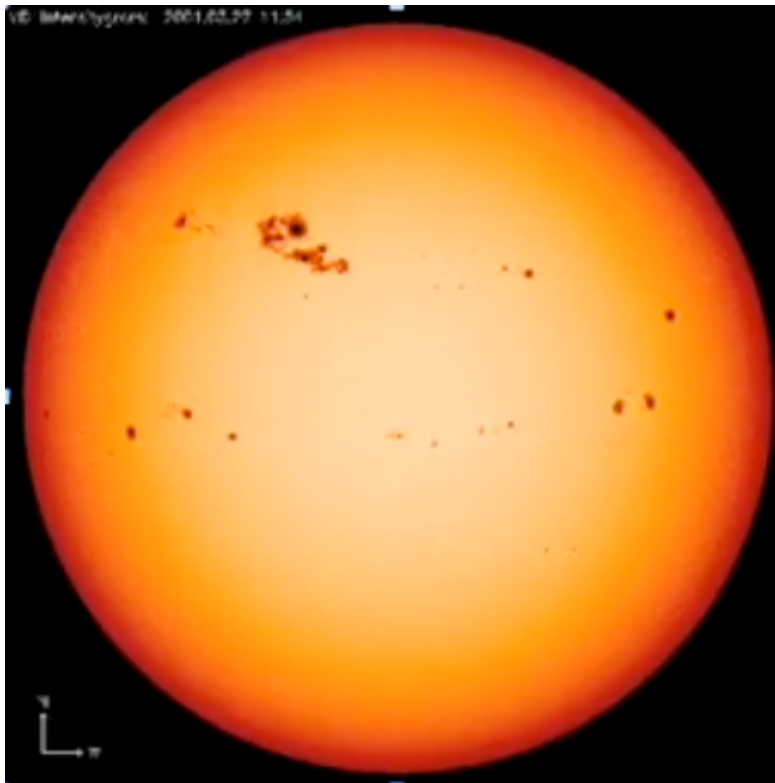
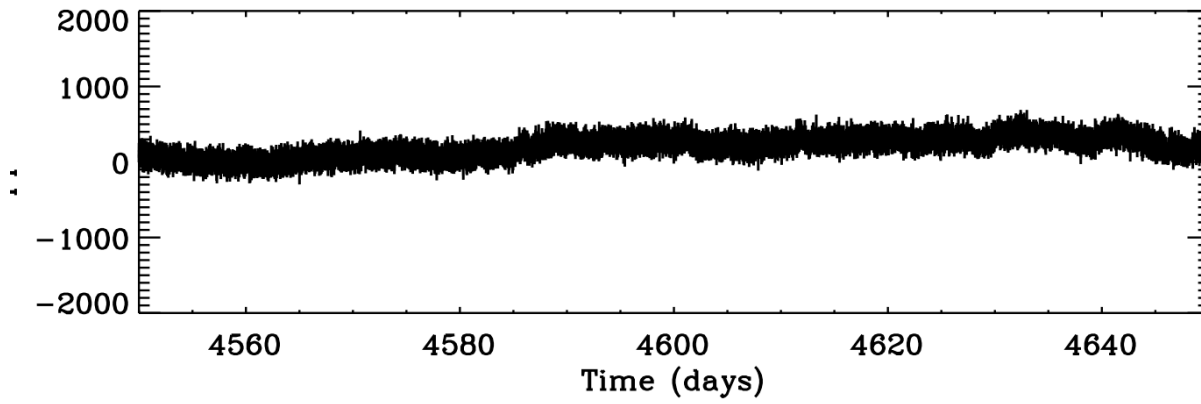
Sunspots appear in two bands on either side of the equator that drift toward the equator as the cycle progresses.

Can we retrieve this information in other stars from LC-data?

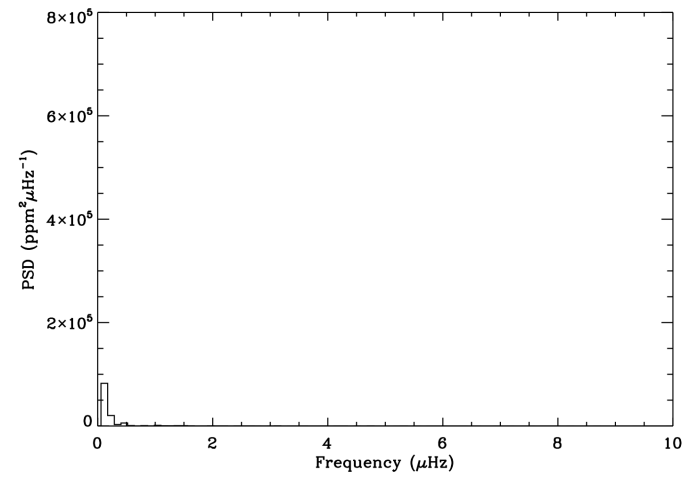


Solar Activity Maximum

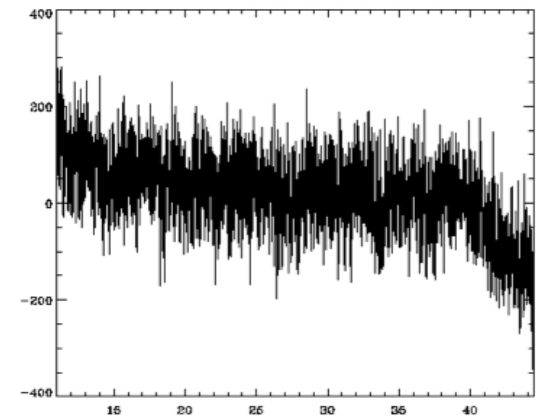
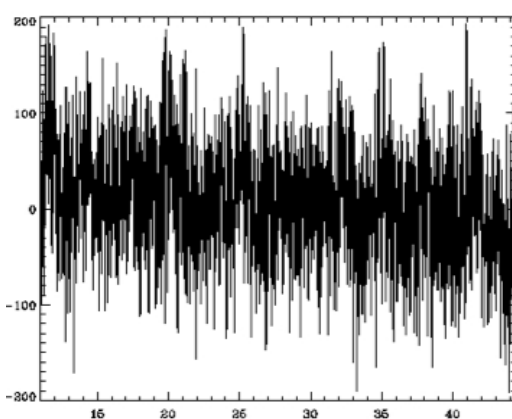
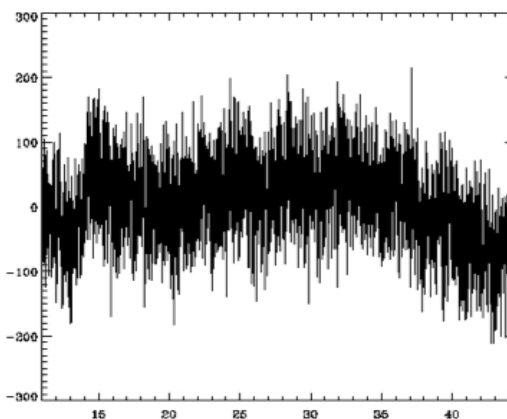
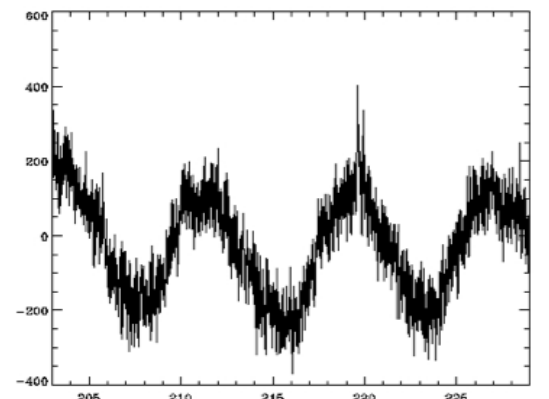
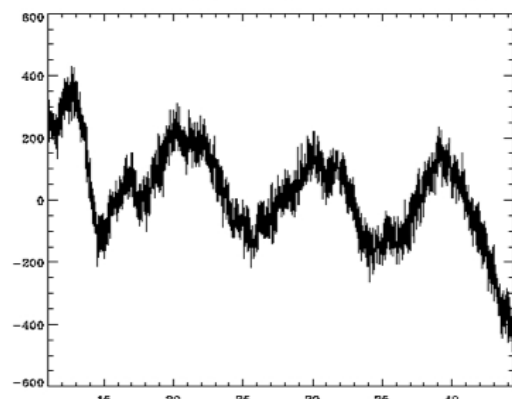
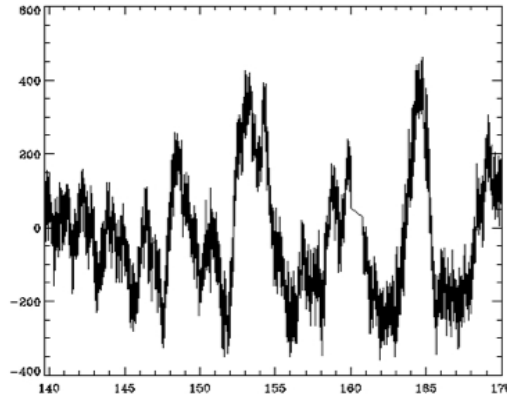
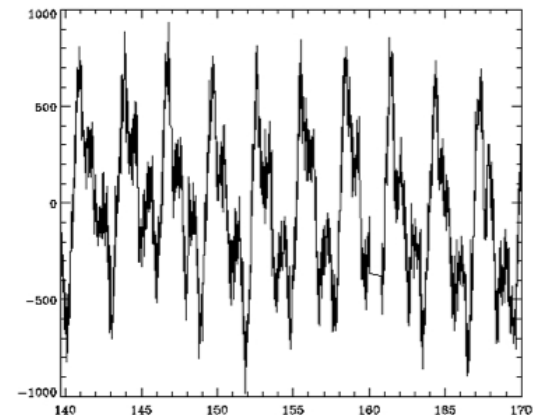
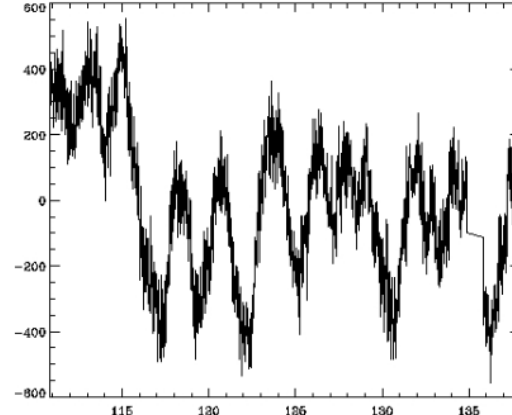
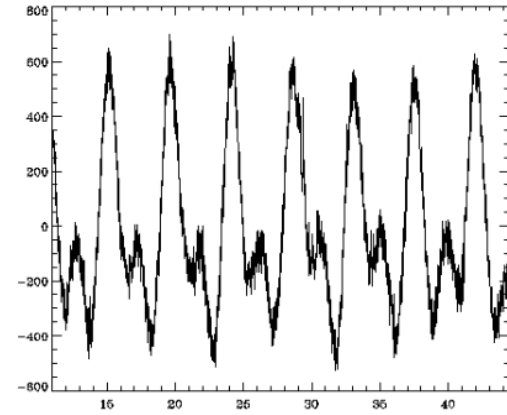
Courtesy of R.A. Garcia, KASC PE11



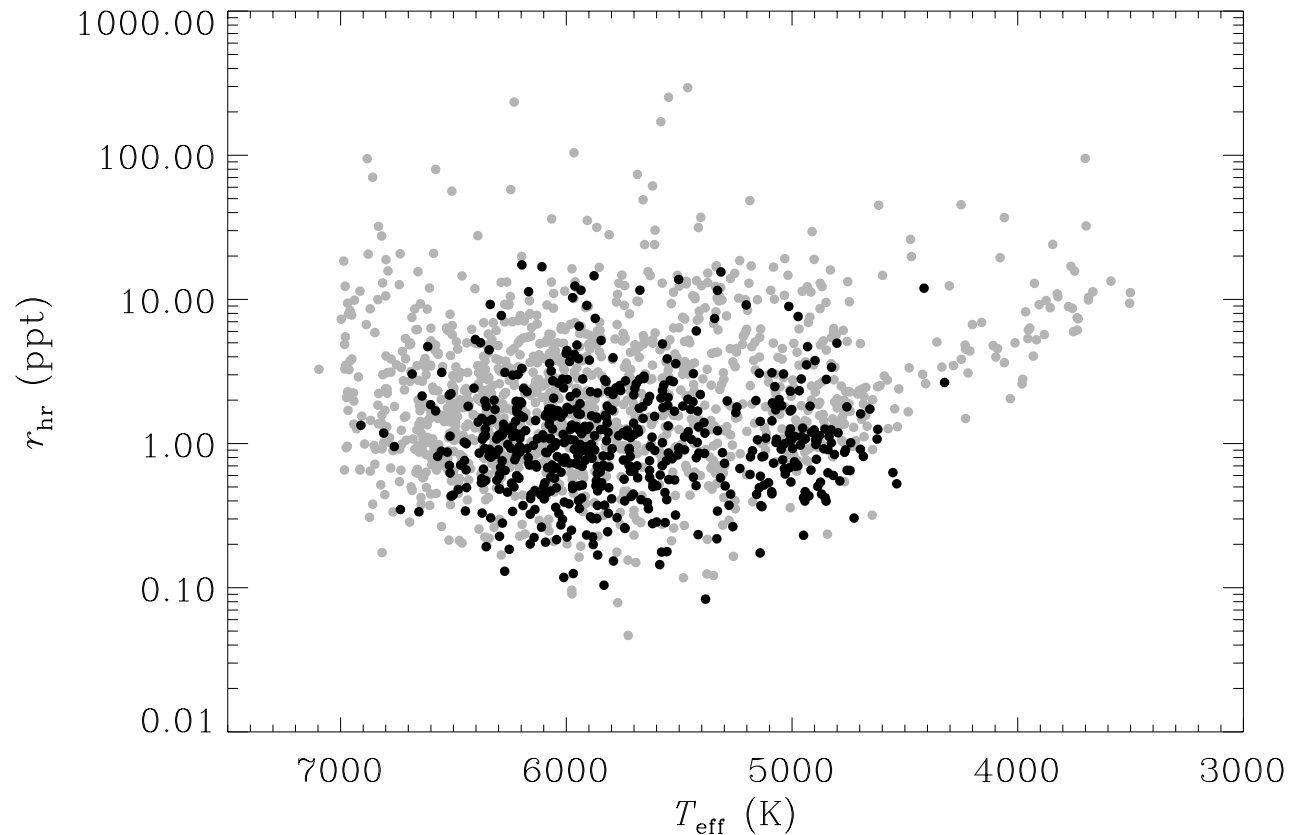
Solar Activity Minimum



Example of *Kepler* light curves (solar-like S)



Magnetic field and pulsations: activity suppresses acoustic oscillations!



Chaplin, Bedding, Bonanno et al., ApJL, 2011

The case of KIC8428280



Stellar Parameters:

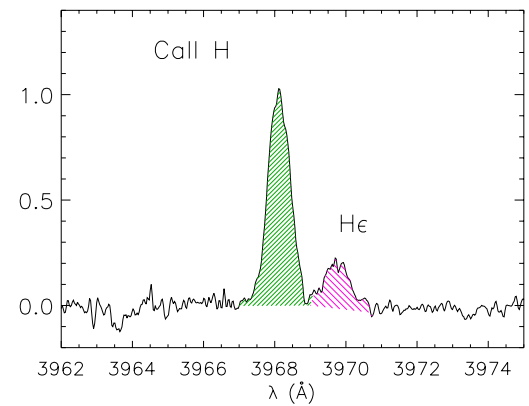
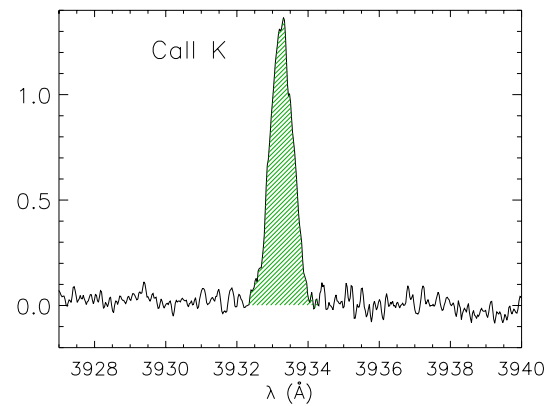
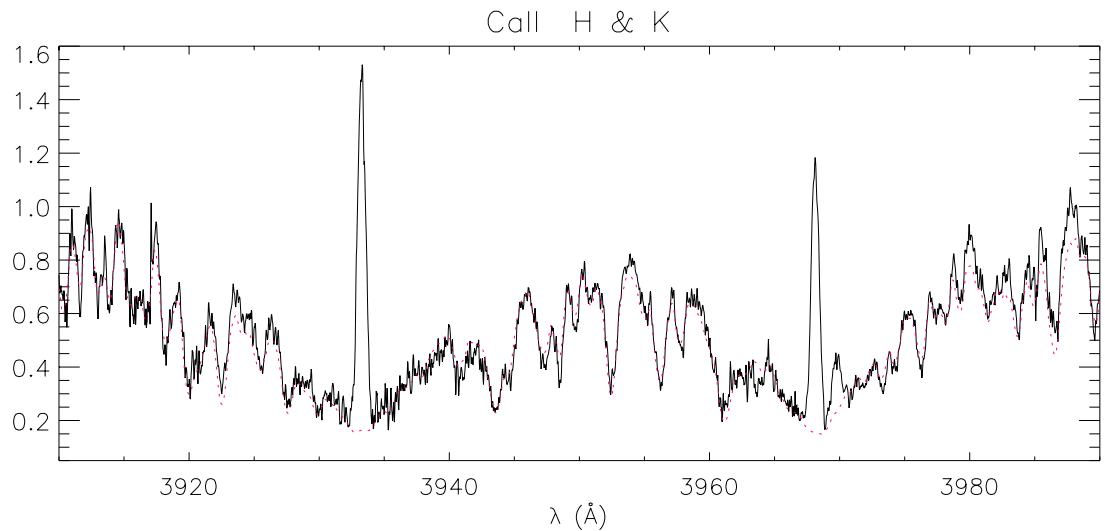
Spectral Type: K2V

$T_{\text{eff}} = 5055 \text{ K}$

$\log g = 4.41$

$\text{Fe}/\text{H} = -0.02$

$V_{\text{ sini}} = 38 \text{ km/s}$

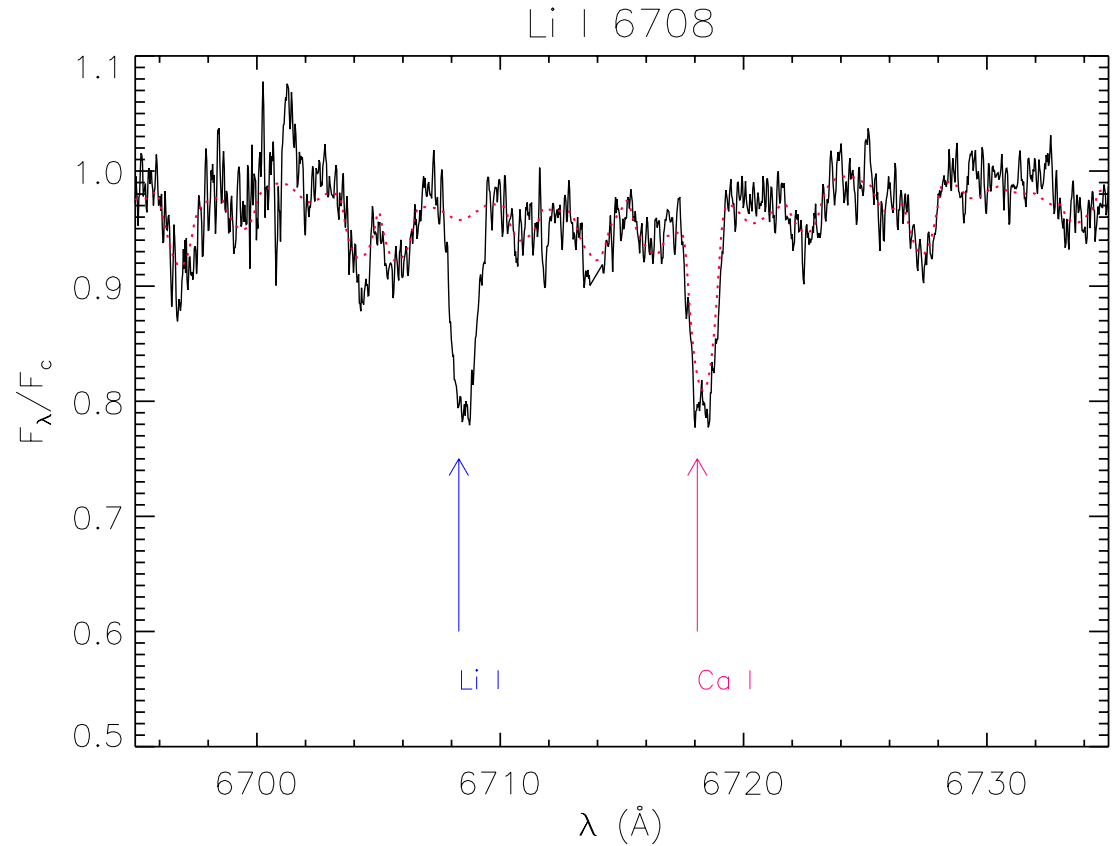


The case of KIC8428280

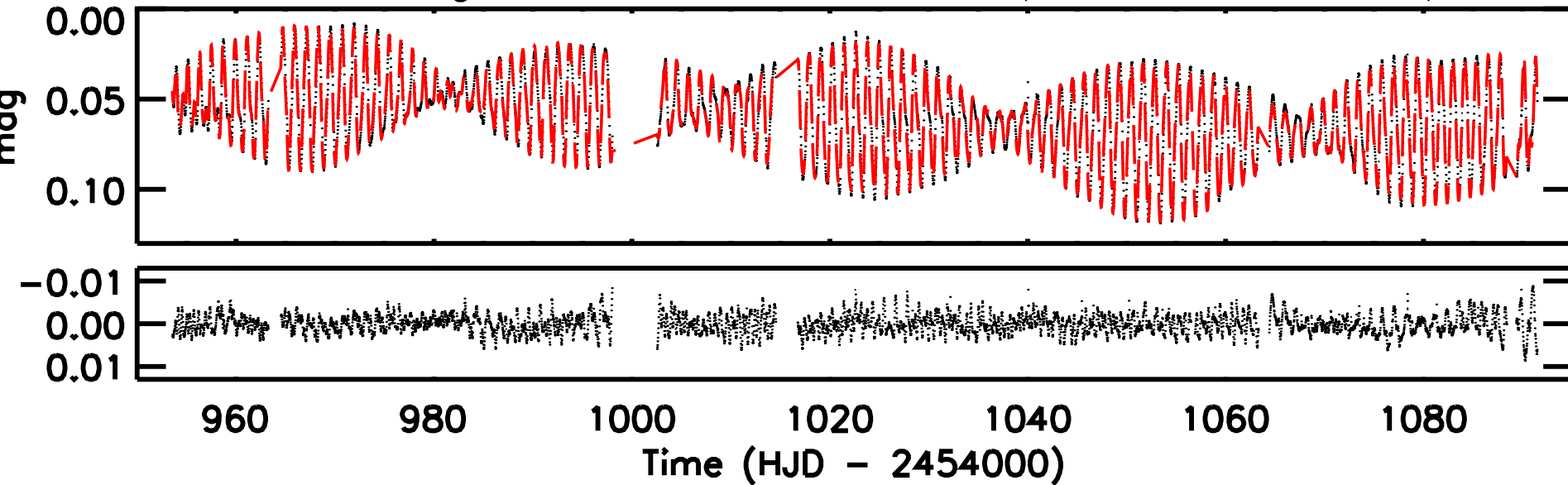


Stellar Parameters:

AGE: 50 Myrs,
Pleiads !

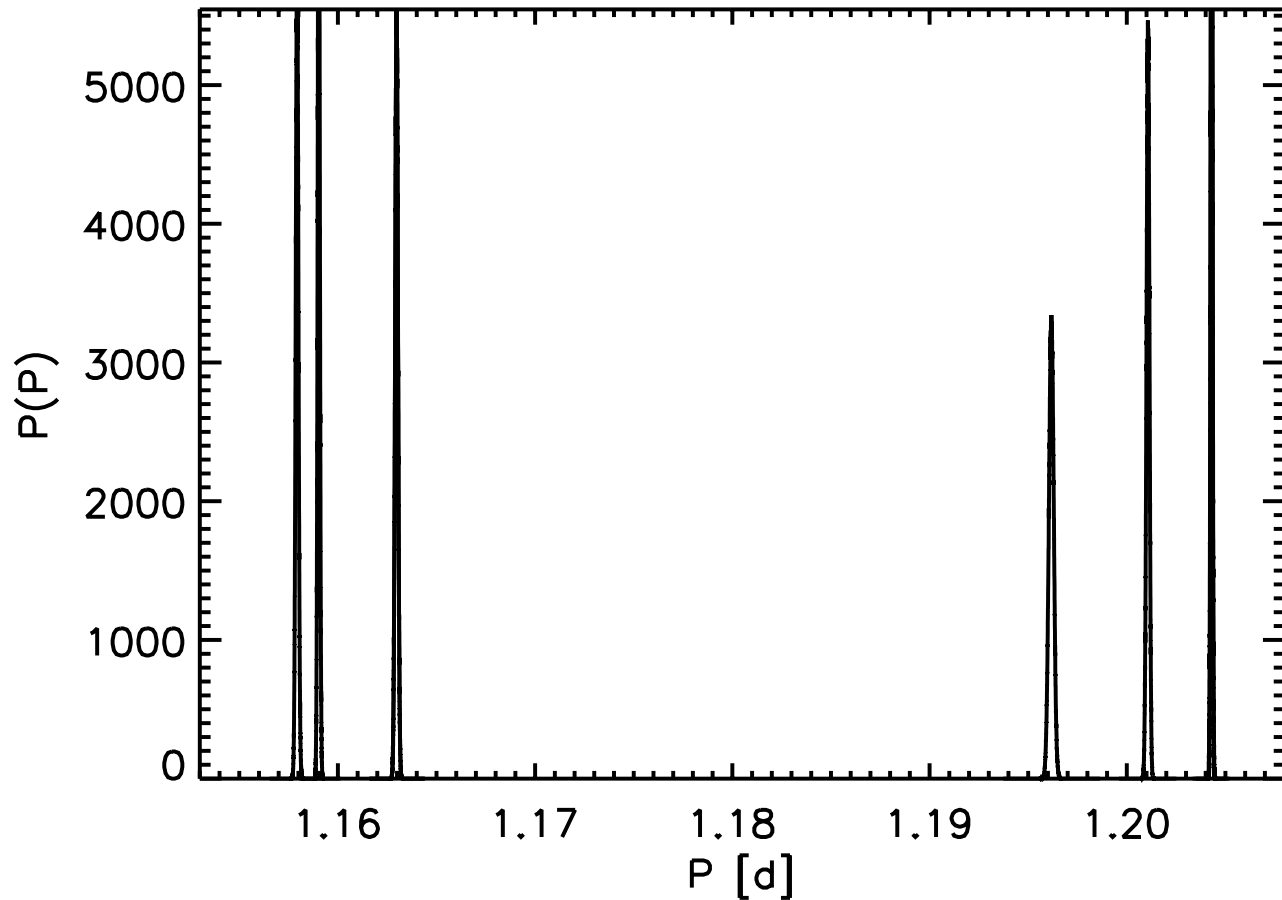


Kepler light curve: KIC 8429280 (bottom: residuals)

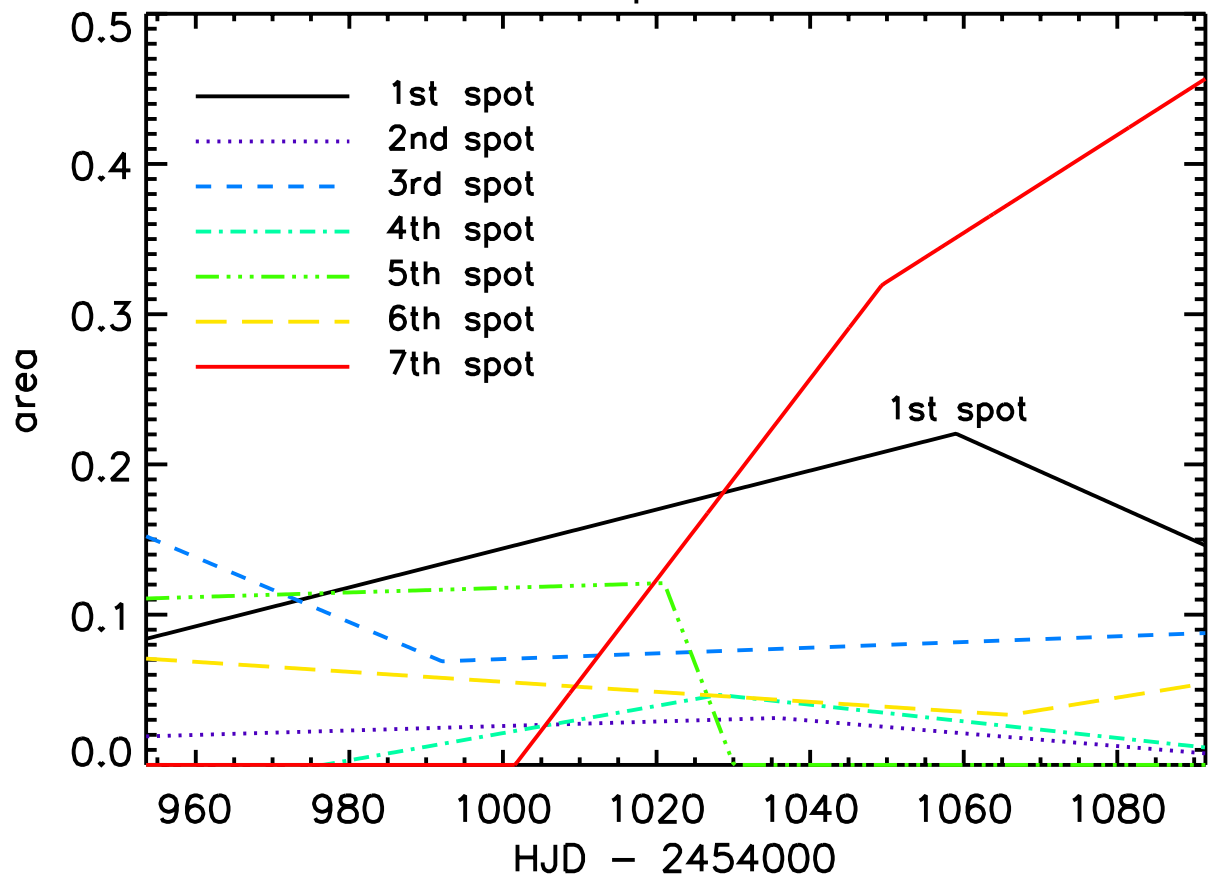


A Bayesian analysis of the 138 days lightcurve in terms of circular spots revealed at least seven slowly evolving features. There are two possible darkspots solutions (if one dismisses a 3rd solution with very dark spots). The latitude dependence of angular velocity is prescribed by a \sin^2 law. A quadratic limb-darkening law with fixed coefficients has been applied. Spot area evolution is parameterized by a simple ansatz: area goes linearly with time. The evolution model allows for one sudden change in the slope of the area vs time relation.

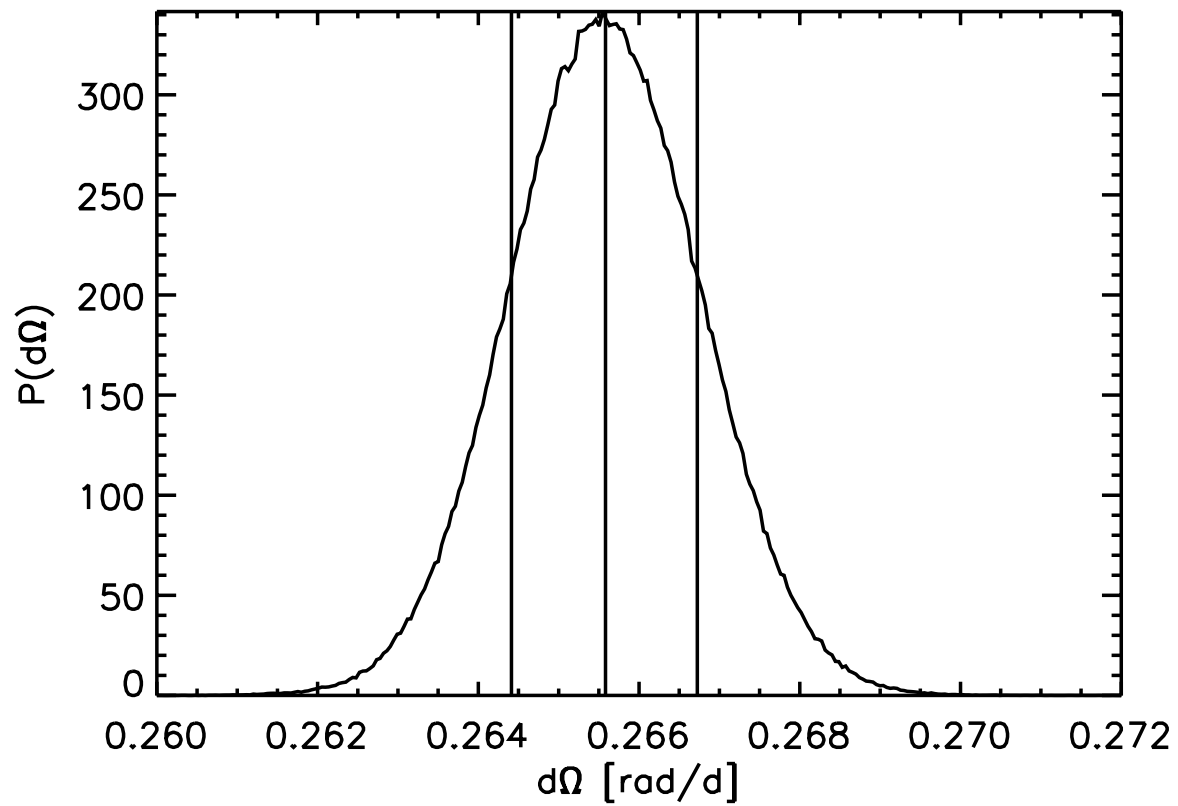
KIC8429280: spot periods



KIC8429280: spot area evolution



KIC8429280: differential rotation



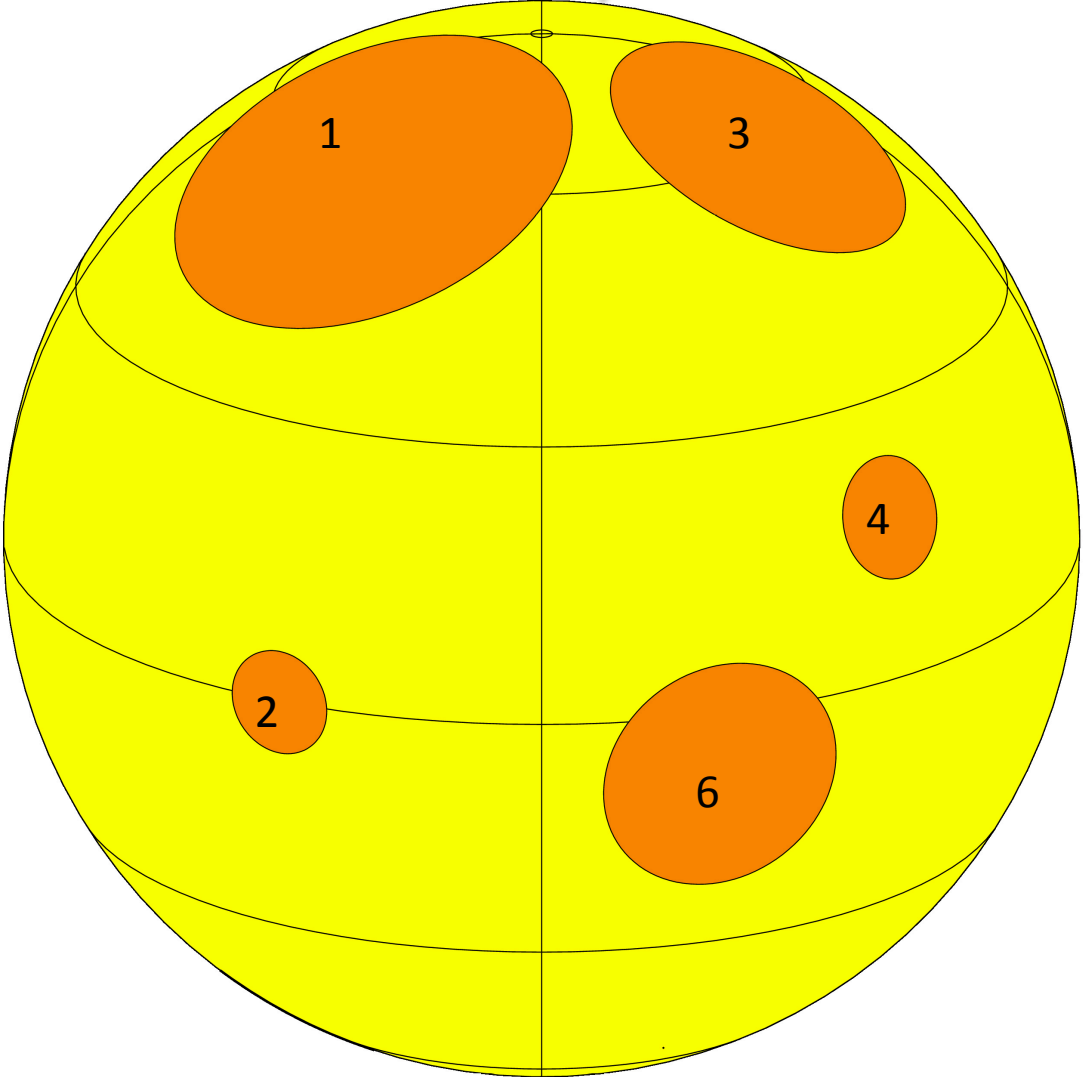
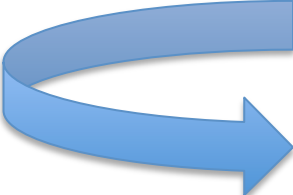
Posterior probability distributions for all parameters with mean and $\pm 1\sigma$ credibility intervals.

In both solutions inclination (69.5 ± 0.4 , 69.6 ± 0.4 deg) and spot contrast (0.57 ± 0.01 , 0.60 ± 0.02) are comparable.

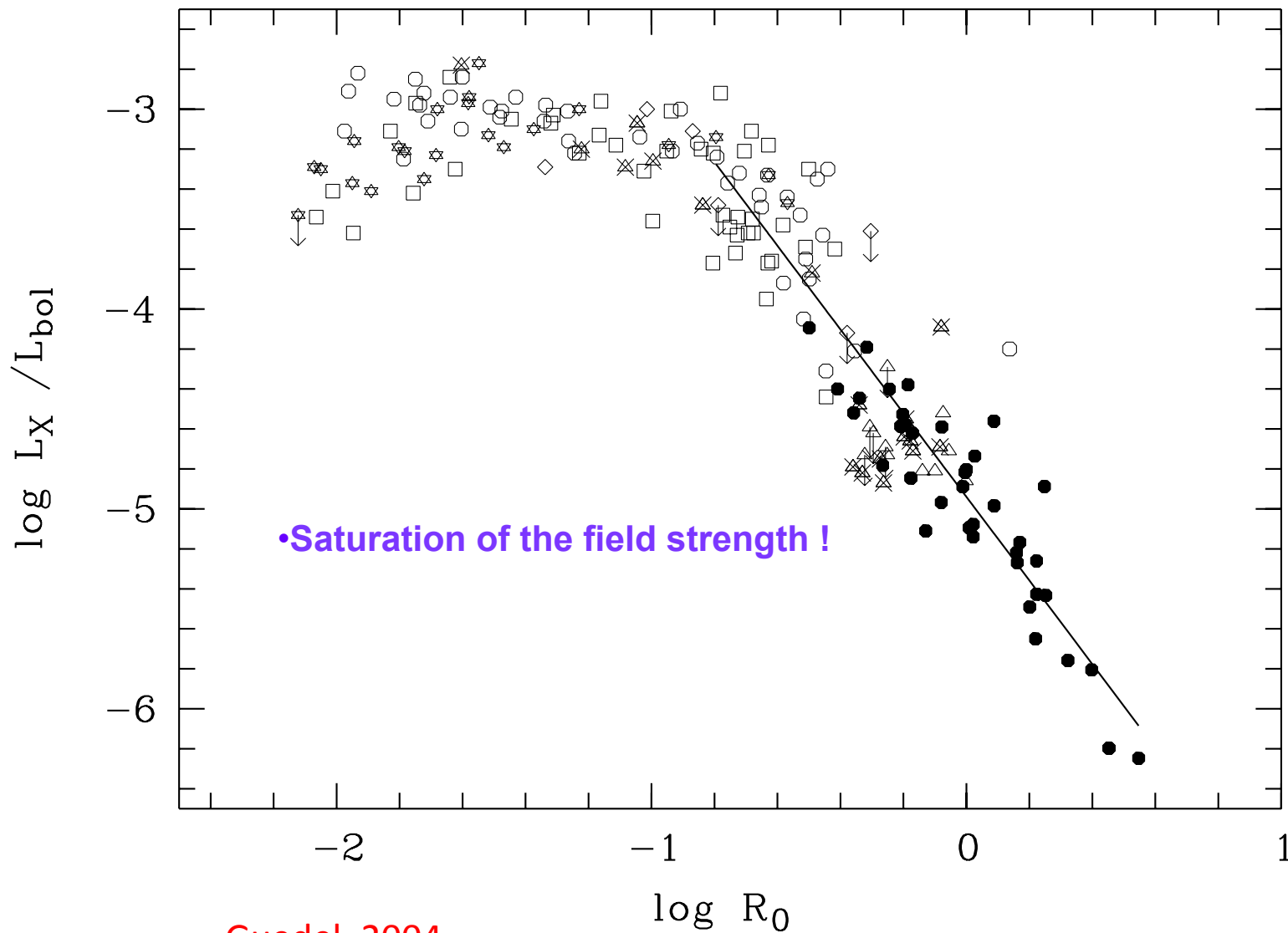
Two southern spots of the 1st solution changed the hemisphere in the 2nd solution.

For both solutions the solar-like differential rotation is surprisingly large: $0.2656 (+0.0012, 0.0011)$ and $0.2974 (+0.0032, 0.0016)$ rad/d, respectively.

The limit is on B not on the filling factor!



KIC8429280 lies in the saturated R_o



Guedel, 2004

Conclusions

- New *Kepler* data on fast rotating stars can explore the high Ro regime of dynamo action (small dynamo?) and obtain surface DR !!
- ESSENTIAL INGREDIENTS ARE GROUND-BASED OBSERVATIONS!
- Dynamo in radiative zone is a very exciting alternative to the standard dynamo based on kinetic-helicity alpha effect
- Much effort is still needed to understand ideal MHD

If dynamos do not work in such a simple case they will not work at all ! (A. Einstein)

Discussion

- Do we understand the triggering mechanism of MHD instabilities? (see also the talk of Shih-Ping Lai). How is turbulence related with basic MHD instability?
- Where is the location of the alpha effect? (CZ vs RZ dynamo)
- Do we expect answers from future/present missions or questions? (see SKA... remember the solar dynamo before and after helioseismology)?
- Role of reconnection on (small scale) dynamo?