

Numerical modeling of relativistic  
magnetic reconnection:  
Kinetic, two-fluid, and MHD simulations

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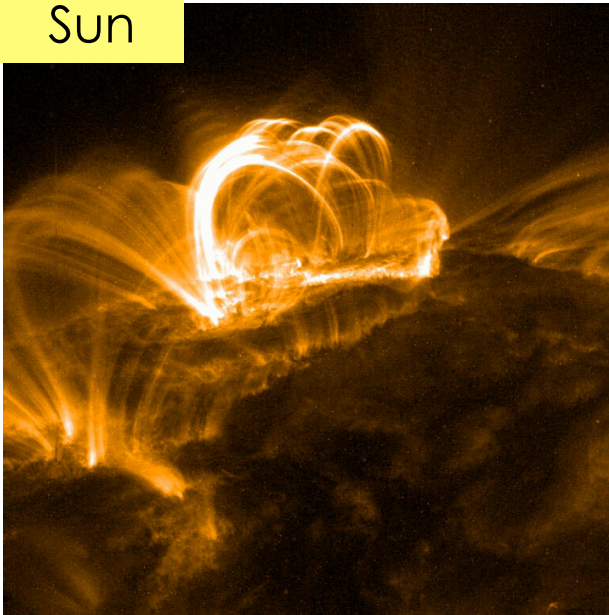
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M. Kuznetsova (NASA/GSFC), T. Miyoshi (Hiroshima U)

# Outline

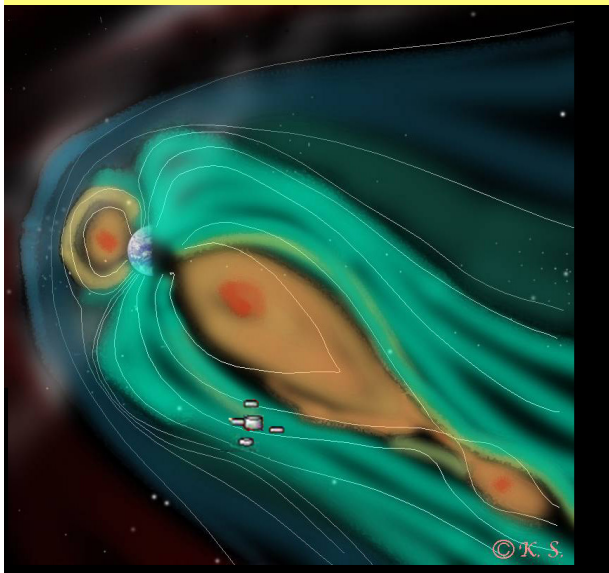
- 0. Introduction
- 1. Kinetic modeling
  - 2D reconnection
- 2. Fluid modeling
  - RRMHD & two-fluid simulations
  - New insight: high-speed fluid dynamics
- 3. Cross-code comparison
- 4. Summary

# Magnetic reconnection

Sun

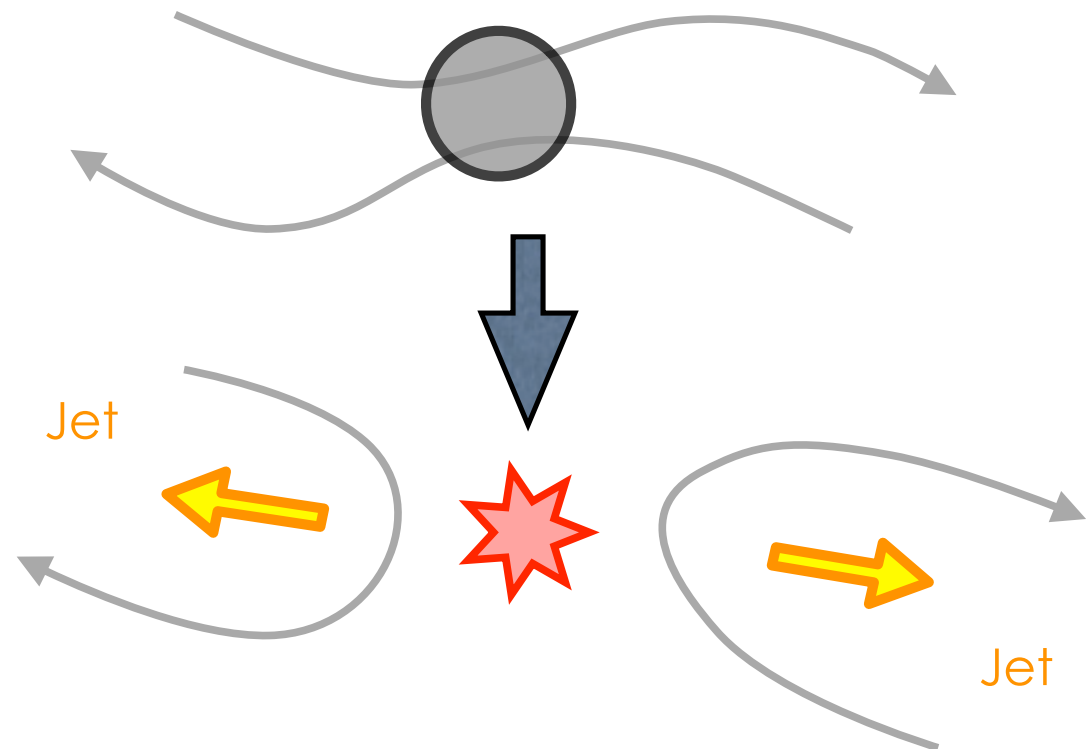


Earth's Magnetosphere



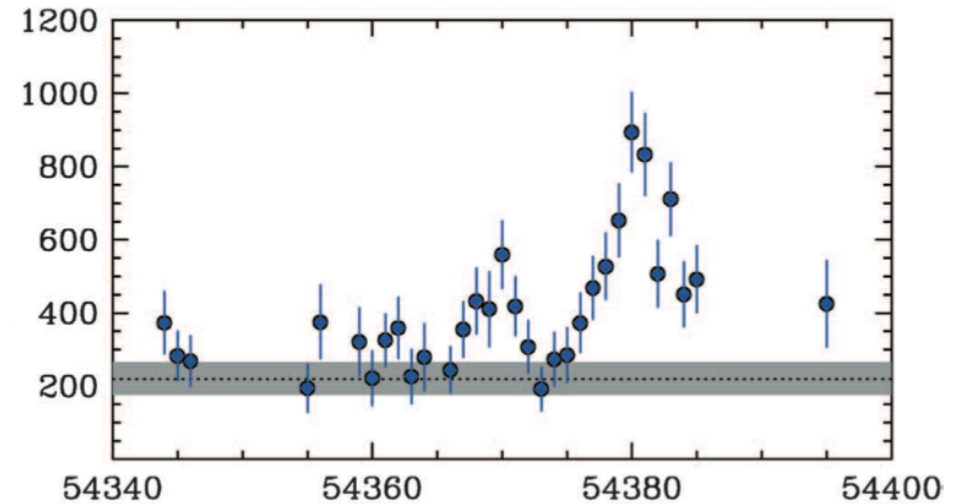
- Re-configuration of magnetic topology
- Release of magnetic energy to plasma energy
- Violation of the ideal condition is necessary

$$\mathbf{E} + \mathbf{v} \times \mathbf{B} \neq 0$$



# Magnetic reconnection in high-energy settings

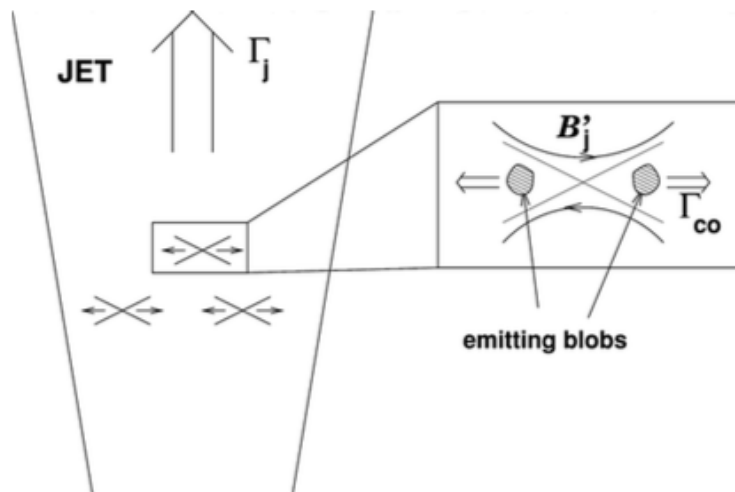
- Magnetically dominated settings
- **Special relativity**
  - + radiation, pair creation ...



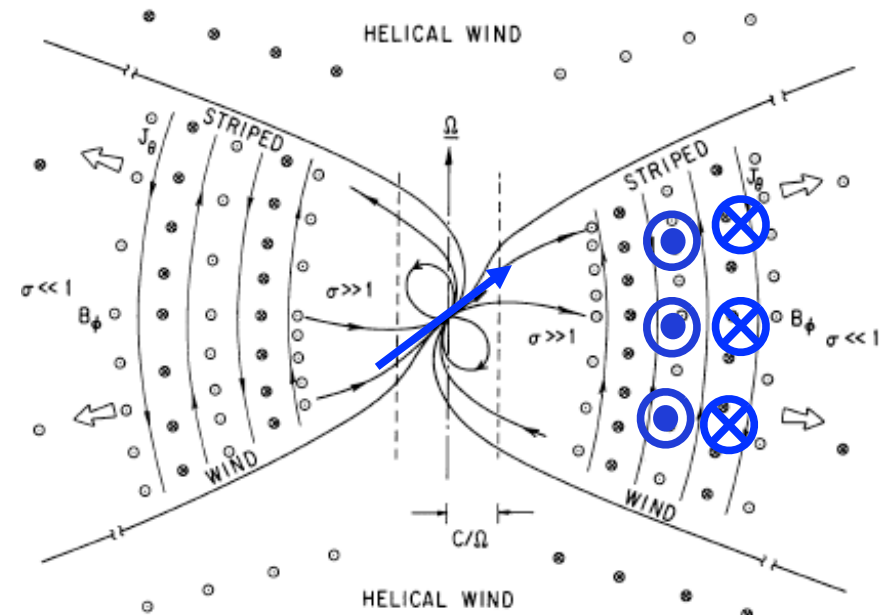
Gamma-ray flares

Tavani 2011

## Jet model



Giannios+ 2009



Striped wind

Coroniti 1990



# Current status of relativistic reconnection research (2015Q2)

- Theories have been discussed over two decades
- Many works came out after the Crab flare (2011)

## MHD theories

Blackman & Field 1994

Lyutikov & Uzdensky 2003

Lyubarsky 2005

Tenbarge+ 2010

Comisso & Asenjo 2014

- Basic properties are under debate

## MHD simulations

Watanabe & Yokoyama 2006  
**Zenitani+ 2010, 11**  
Zanotti & Dumbser 2011  
Takahashi+ 2011  
Takamoto 2013  
**(Zenitani+ 2015)**

- Ideal for global modeling

## Two-fluid simulations

**Zenitani+ 2009**

- Meso-scale evolution

## Kinetic (PIC) simulations

**Zenitani & Hoshino 2001-2008**

Jaroschek+ 2004-2009

Liu+ 2011

Cerutti+ 2012-2014

Kagan+ 2013

Sironi & Spitkovsky 2014

Melzani+ 2014

Guo+ 2014-2015

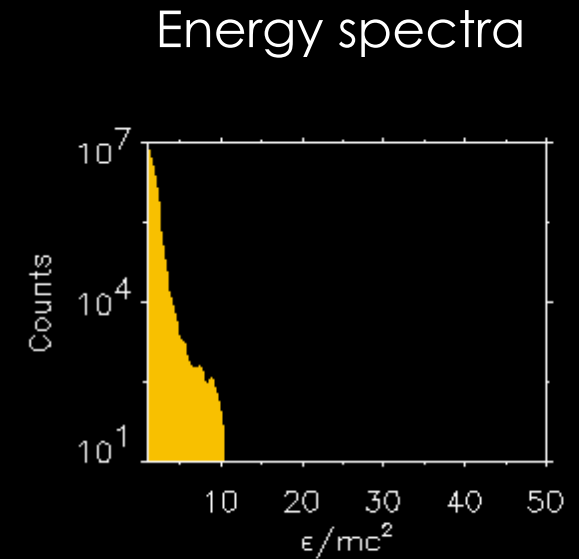
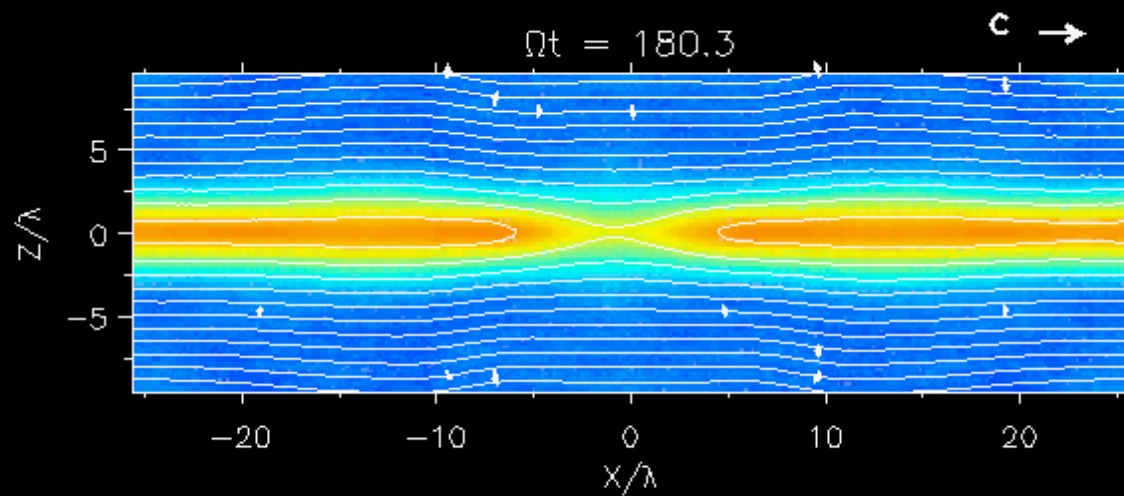
**Zenitani in prep.**

- Fast evolution
- Particle acceleration

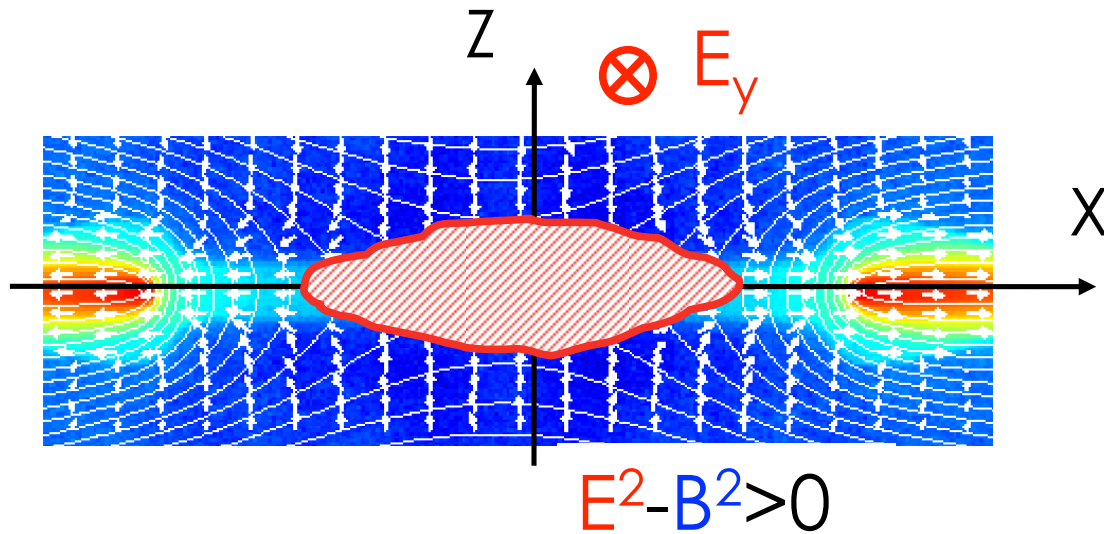
# 1. Kinetic modeling

# 2D Particle-In-Cell (PIC) simulation

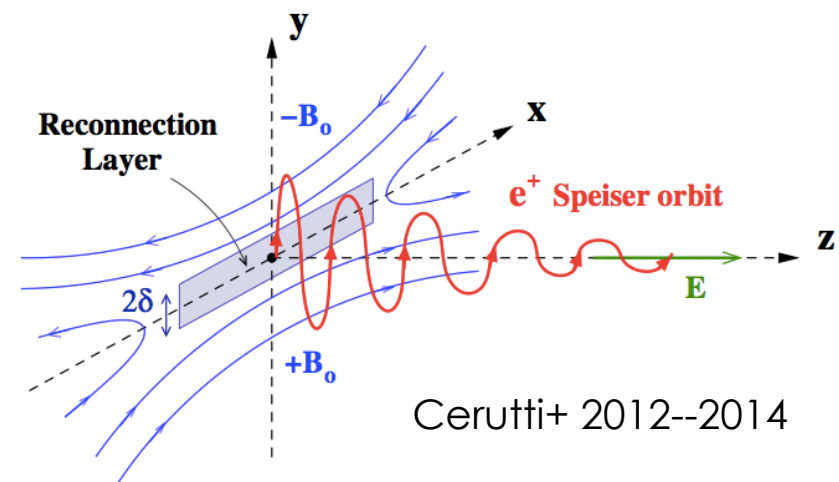
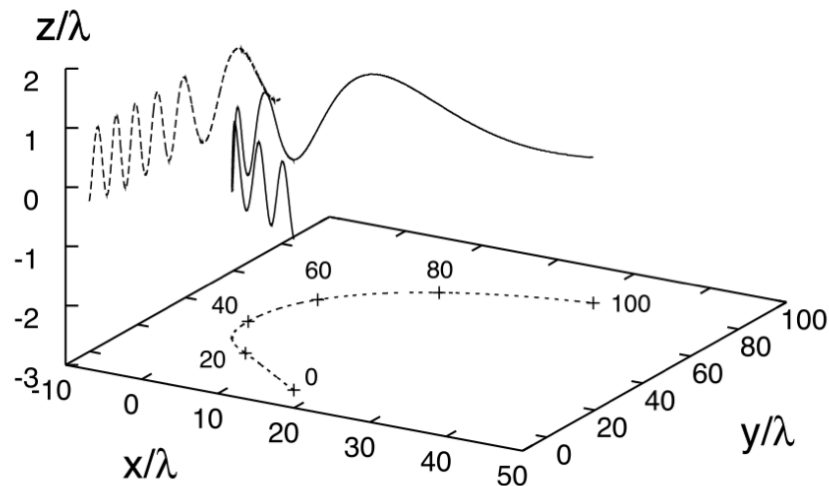
- Fast reconnection and **particle acceleration** occurs
- Online version: <http://th.nao.ac.jp/MEMBER/zenitani/files/reconnection.mov>



# DC particle acceleration

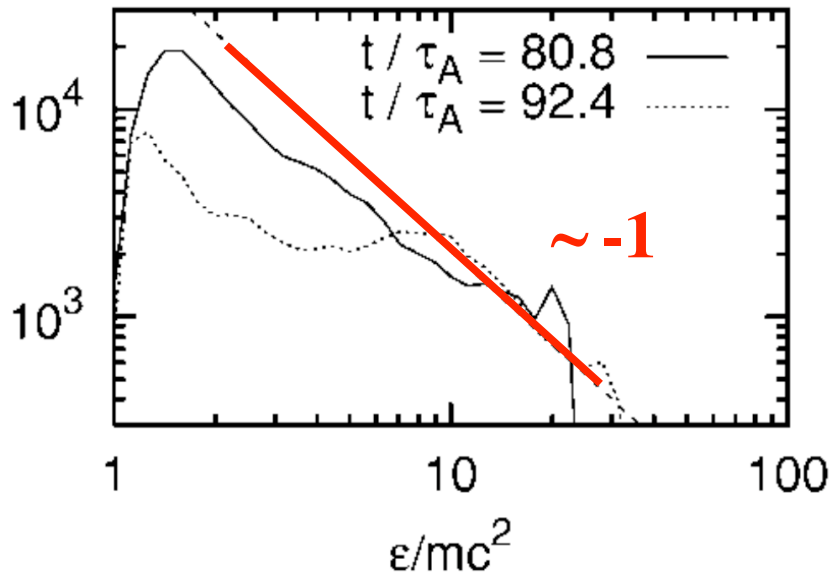


Speiser 1965, Michel 1968,  
Zenitani & Hoshino 2001, 2007,  
Uzdensky+ 2011, Cerutti+ 2012

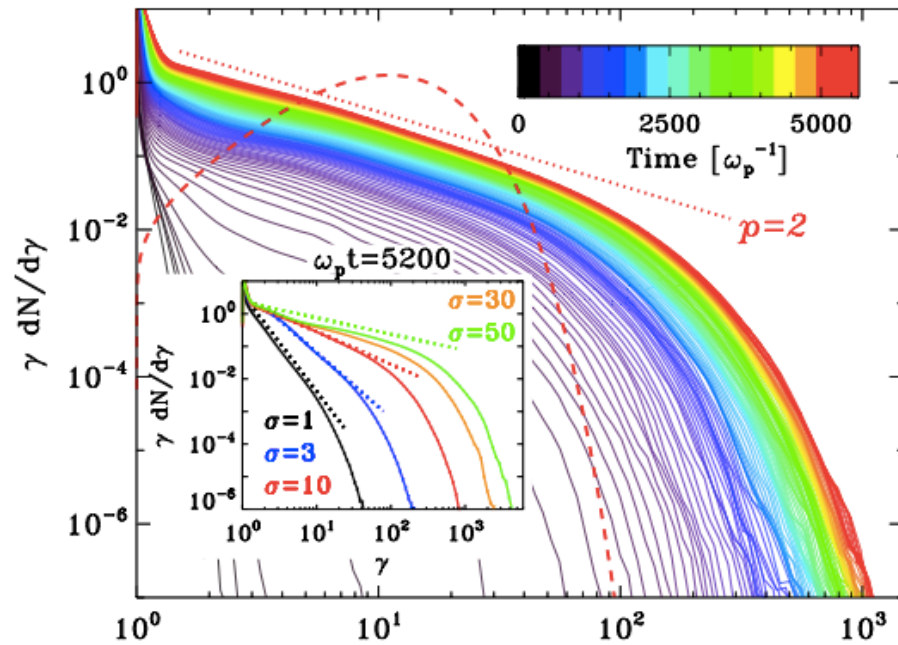


Cerutti+ 2012--2014

# Hard-energy spectra

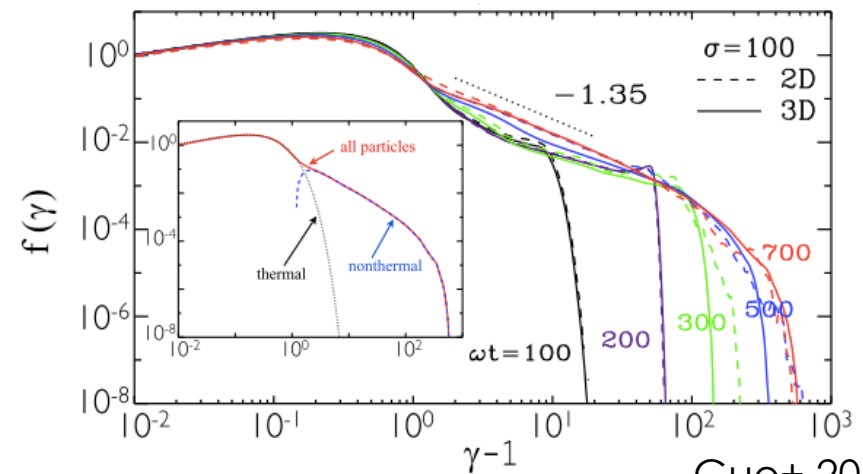


Zenitani & Hoshino 2001



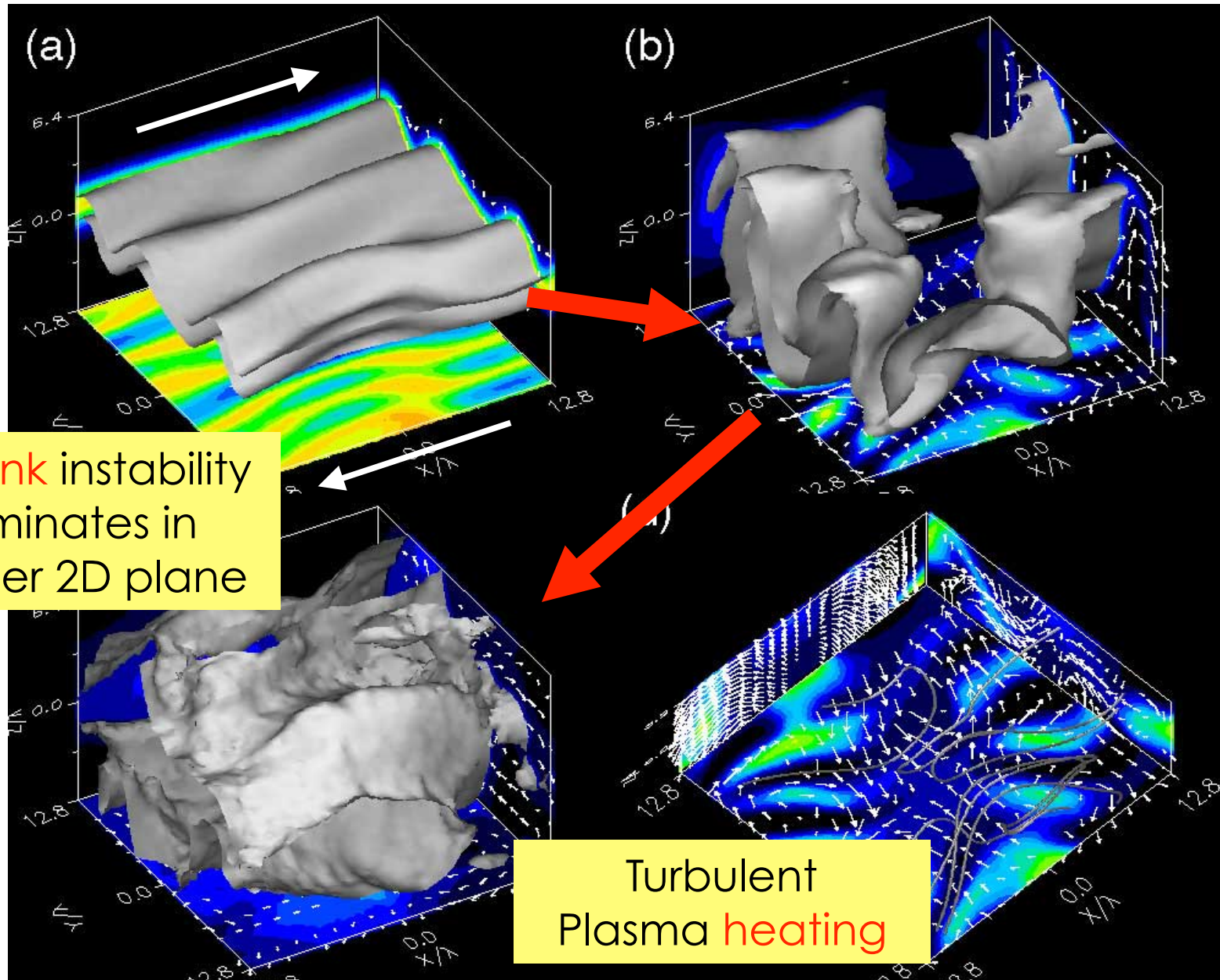
Sironi & Spitkovsky 2014

- Power-law index in earlier works  
 $s \sim -1$  (near acc. region),  $-2 \sim -3$  (global)
- Fermi process? Upstream magnetization may control the index (Guo+ 2014)



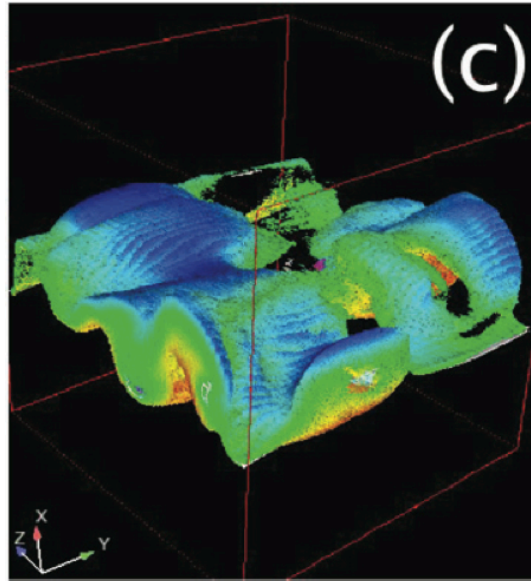
Guo+ 2014

# 3D reconnection: Onset problem

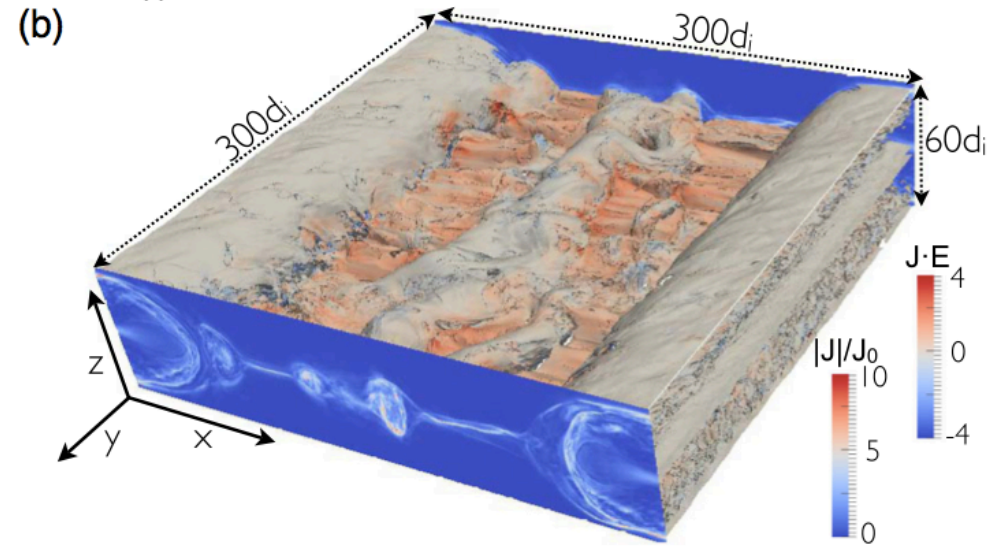




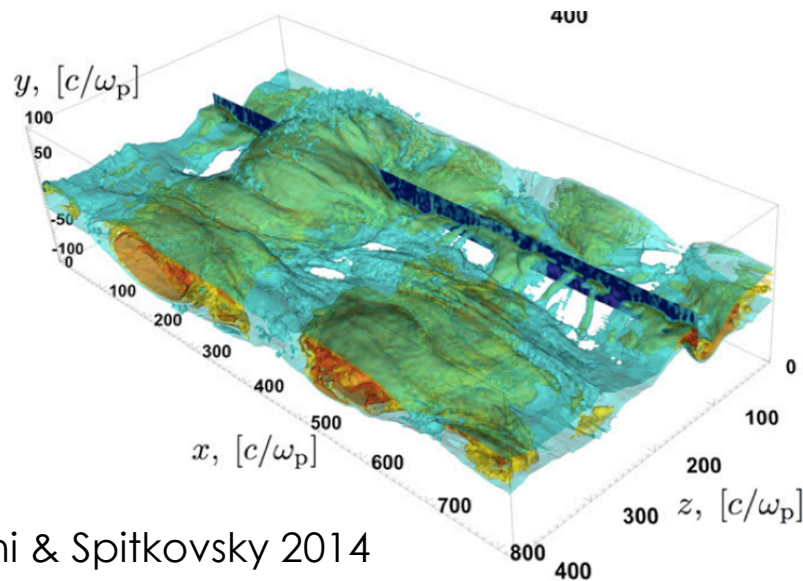
# 3D large-scale evolution: RX appears to win



Liu+ 2011



Guo+ 2014



Sironi & Spitkovsky 2014

- **Kink**-mode often saturates
- **Reconnection** outruns **kink**, and then particle acceleration turns on
- 3D energy spectra is similar to 2D



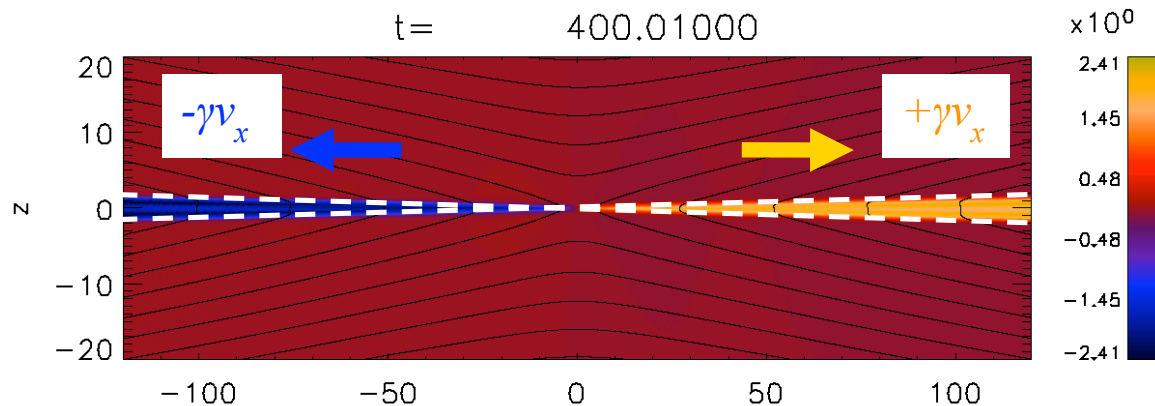
## 2. Fluid modeling

# Relativistic Petschek (PK) reconnection

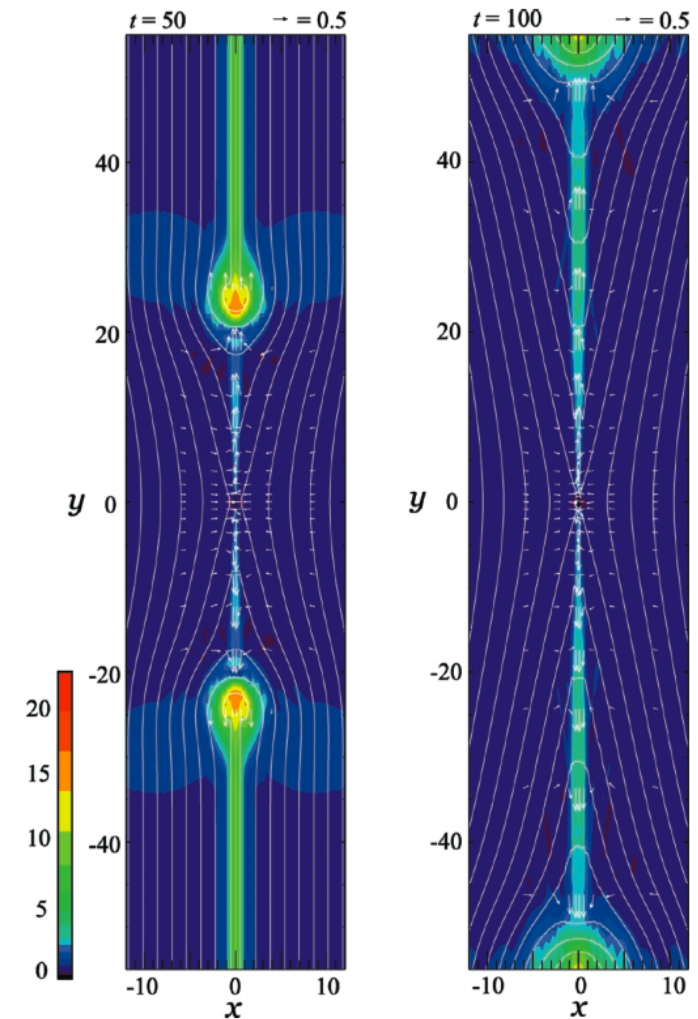
- Relativistic resistive MHD (RRMHD) eqs.  
(Watanabe & Yokoyama 2006, Komissarov 2007)

$$\begin{aligned}
 (\rho U^\mu)_{,\mu} &= 0, & (T_{\text{gas}}^{\mu\nu} + T_{\text{em}}^{\mu\nu})_{,\mu} &= 0 \\
 F_{,\mu}^{\mu\nu} &= -J^\nu, & F_{,\mu}^{*\mu\nu} &= 0 \\
 F^{\mu\nu} u_\nu &= \eta \left( J^\mu + (J^\nu u_\nu) u^\mu \right)
 \end{aligned}$$

- Alternative: relativistic two-fluid eqs.  
(Zenitani+ 2009a,b, Barkov+ 2014)



Zenitani+ 2009a



Watanabe & Yokoyama 2006

# Relativistic PK reconnection - Alfvénic outflow

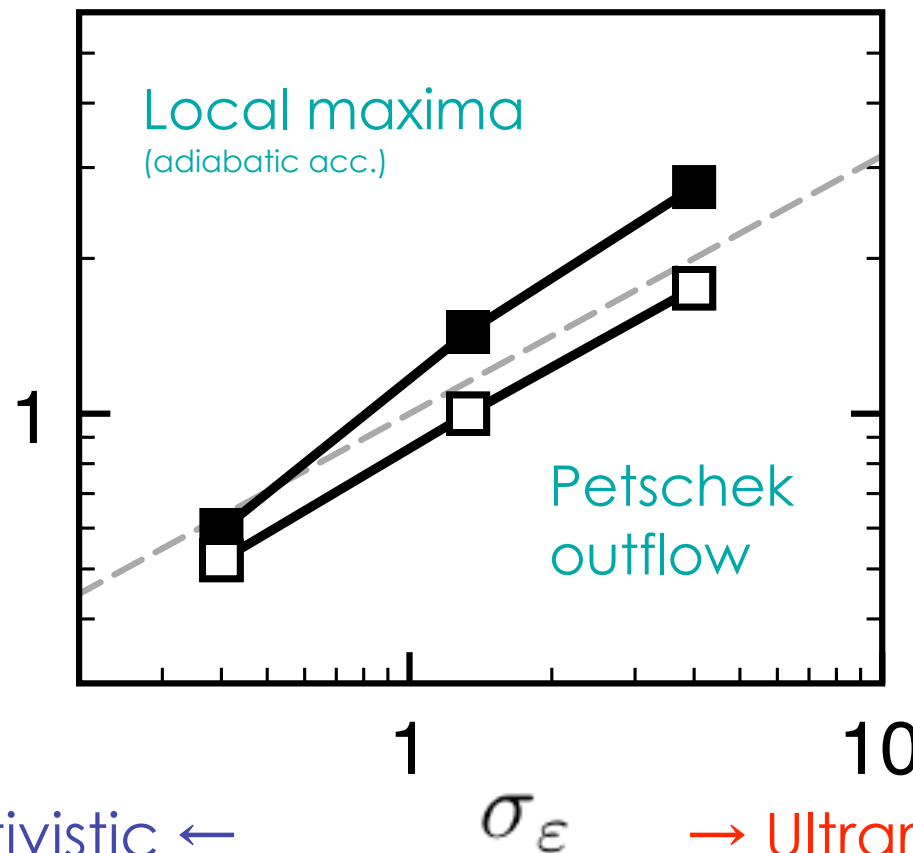
- Magnetization parameter

$$\sigma_\varepsilon = \frac{B_0^2}{4\pi\gamma^2 w} \left( \approx \frac{8}{5} \frac{\mathcal{E}_{EM}}{\mathcal{E}_{fluid}} \right)$$

- Relativistic Alfvén speed

$$\gamma_{jet} v_{jet} \approx \gamma_{ACA} = \sqrt{\sigma_\varepsilon}$$

$$U_x = \gamma V_x$$

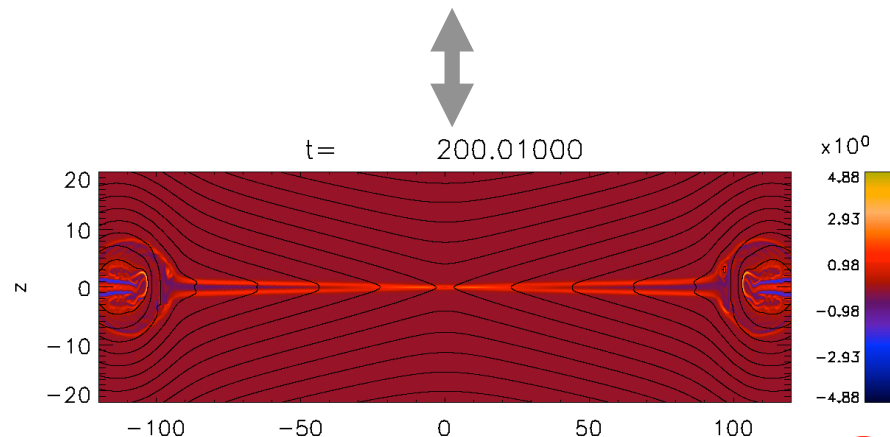
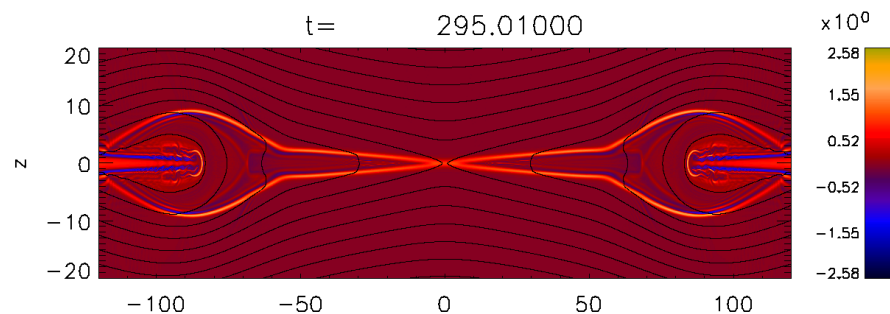


Zenitani+ 2010

# Relativistic PK reconnection - a paradox

- Narrower opening angle (Lyubarsky 2005)
- Speed is limited by Alfvén speed

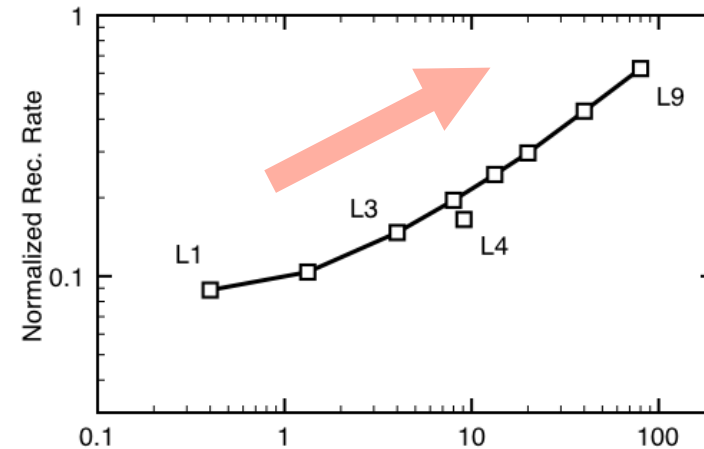
Semi-relativistic ( $\sigma=0.4$ )



Relativistic ( $\sigma=4$ )

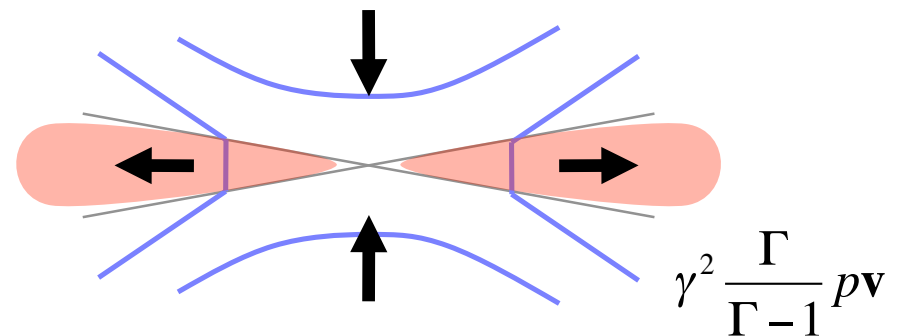


- Reconnection rate (flux transfer speed) goes high

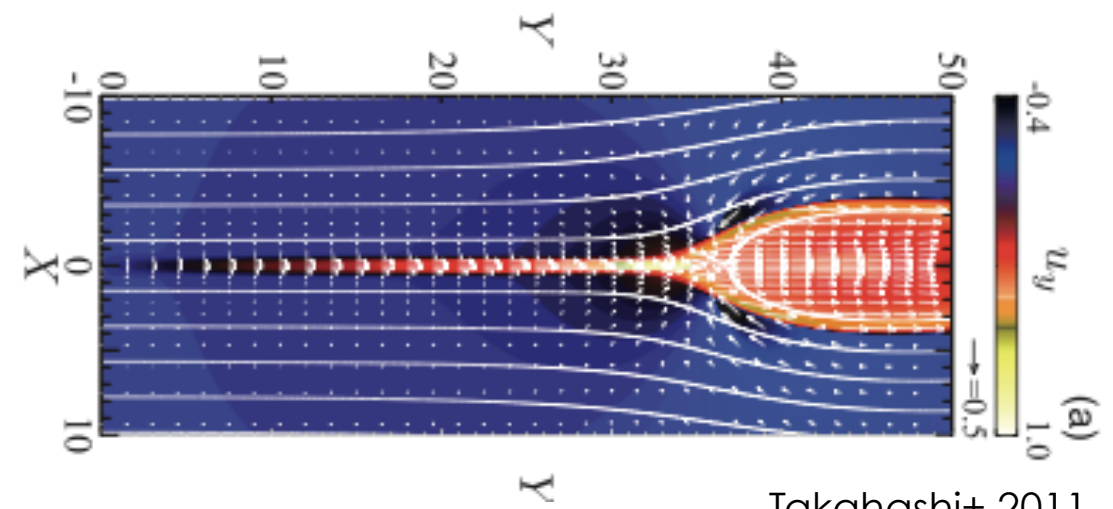
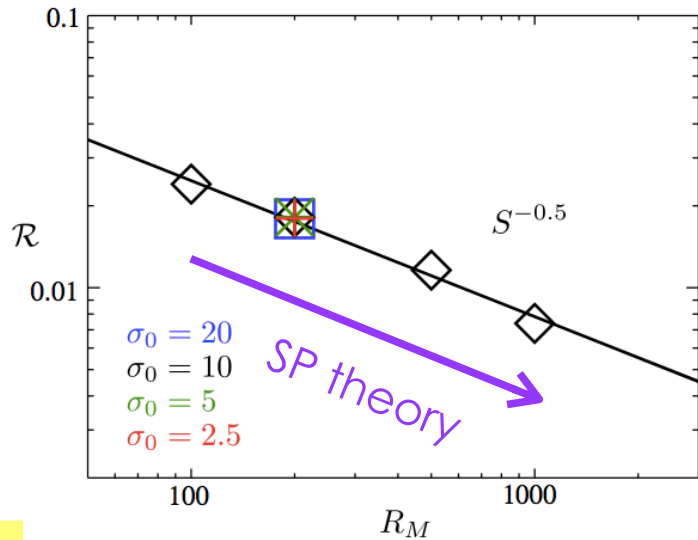


Nonrelativistic  $\leftarrow \sigma_\epsilon \rightarrow$  Ultrarelativistic

- Heat-dominated flow sustains fast energy throughput

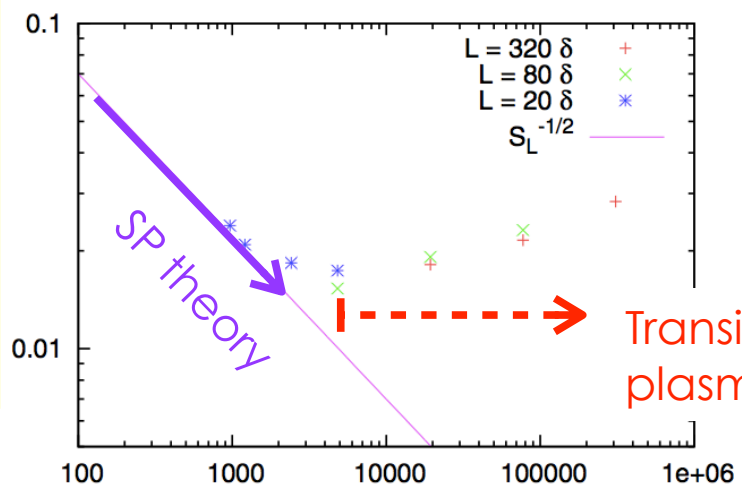


# Relativistic Sweet-Parker reconnection

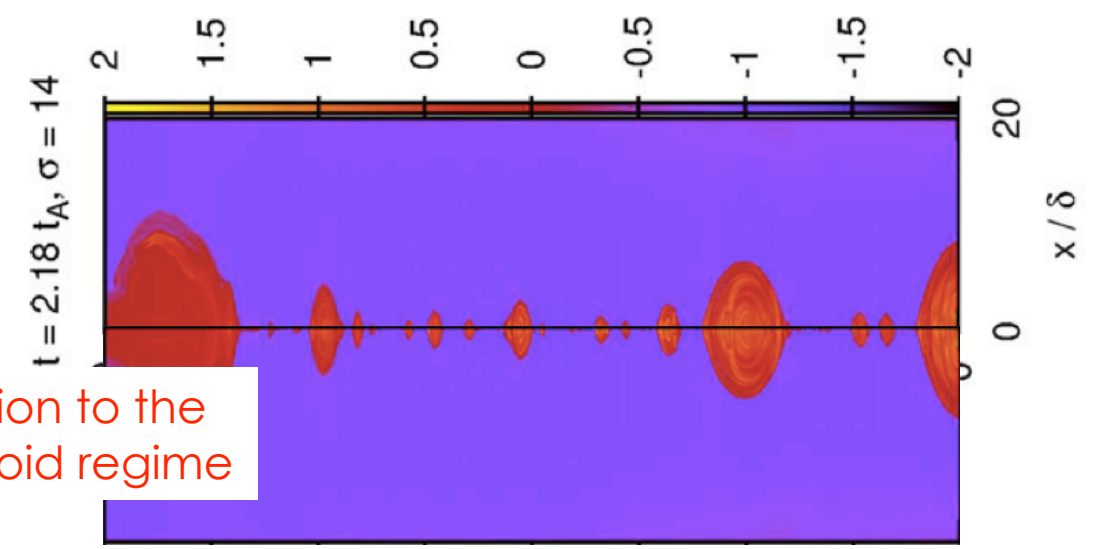


Takahashi+ 2011

Reconnection rate



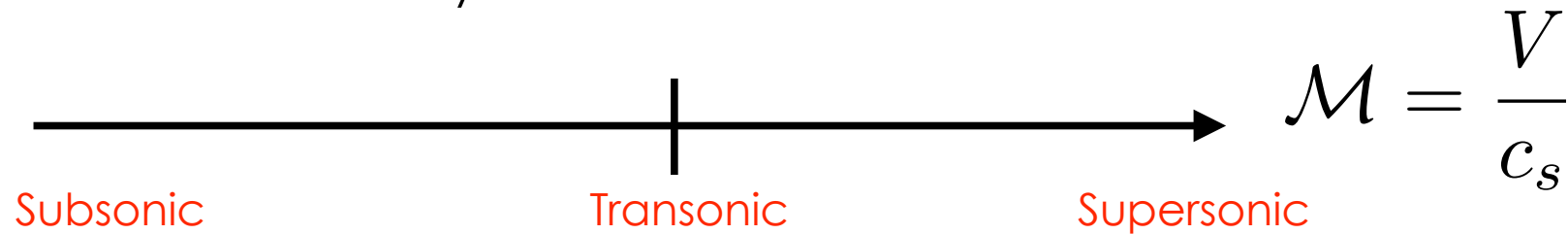
Lundquist number  
(Normalized system length)



Takamoto 2013

# New insight: High-speed fluid dynamics

- Branches of fluid dynamics

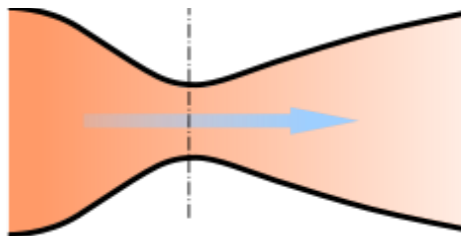
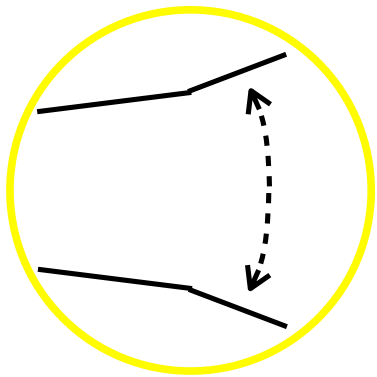
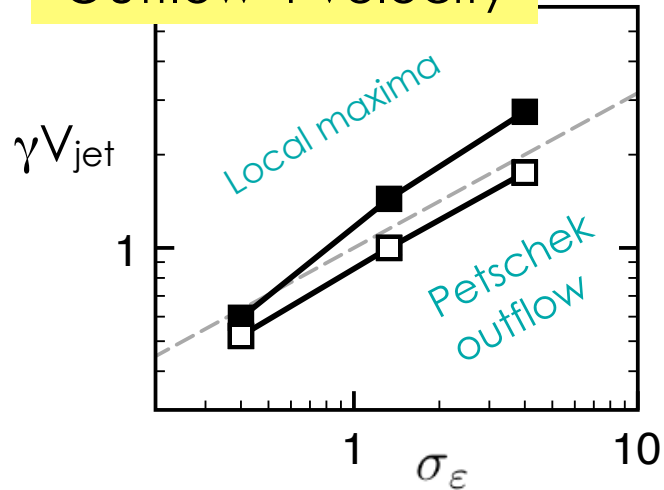


- Incompressible fluids
  - High-speed fluid dynamics
  - Compressible fluid dynamics
    - Adiabatic effects
    - Shocks
    - Shock=Shock interaction
- Relativistic reconnection is usually in the high-speed regime

$$c_s \leq \frac{c}{\sqrt{3}} \quad c_A = c \sqrt{\frac{\sigma_\varepsilon}{1 + \sigma_\varepsilon}} \rightarrow c \quad \sigma_\varepsilon > \frac{1}{2}$$

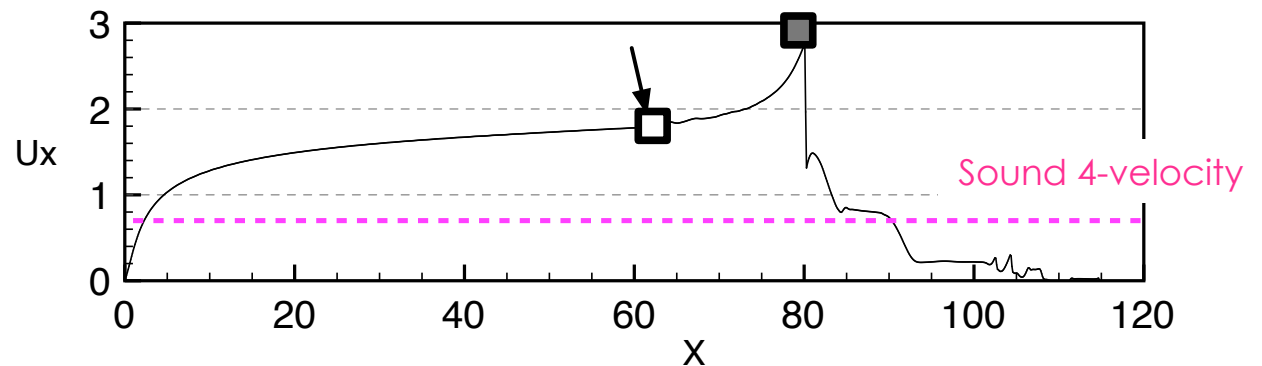
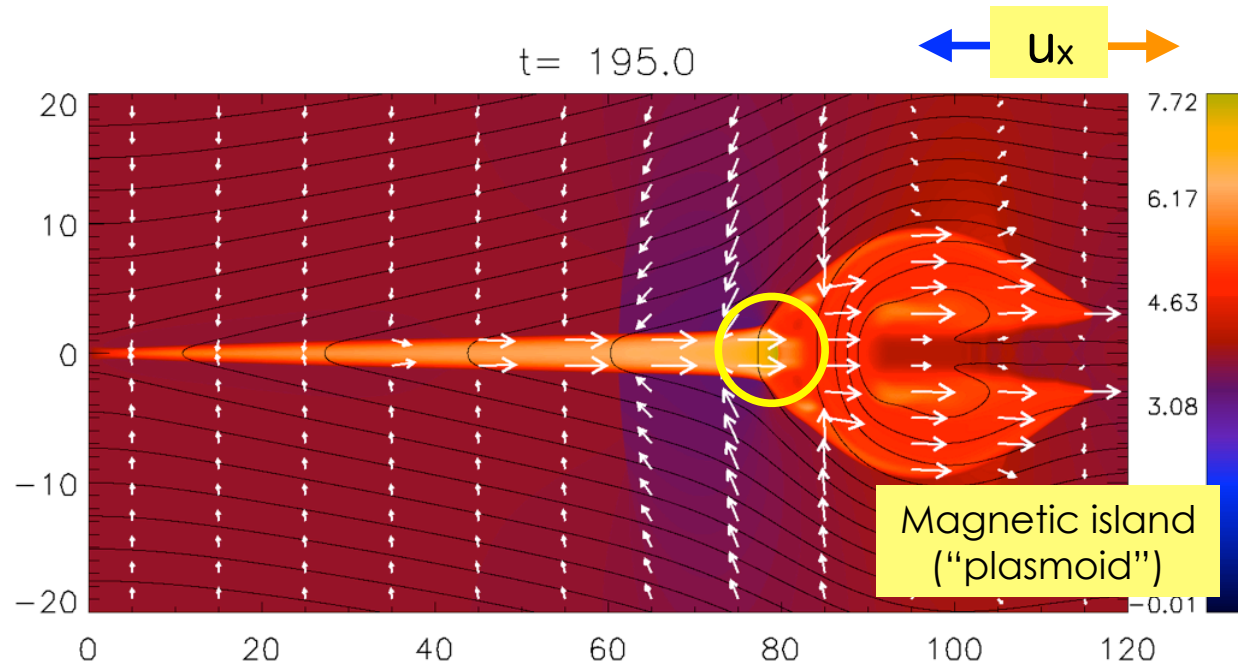
# High-speed fluid effects (1/3): Adiabatic acceleration

## Outflow 4-velocity



Laval nozzle

- Proposed by Shimizu & Ugai 2000
- Super-Alfvénic flow was also reported by Zanotti & Dumbser 2011

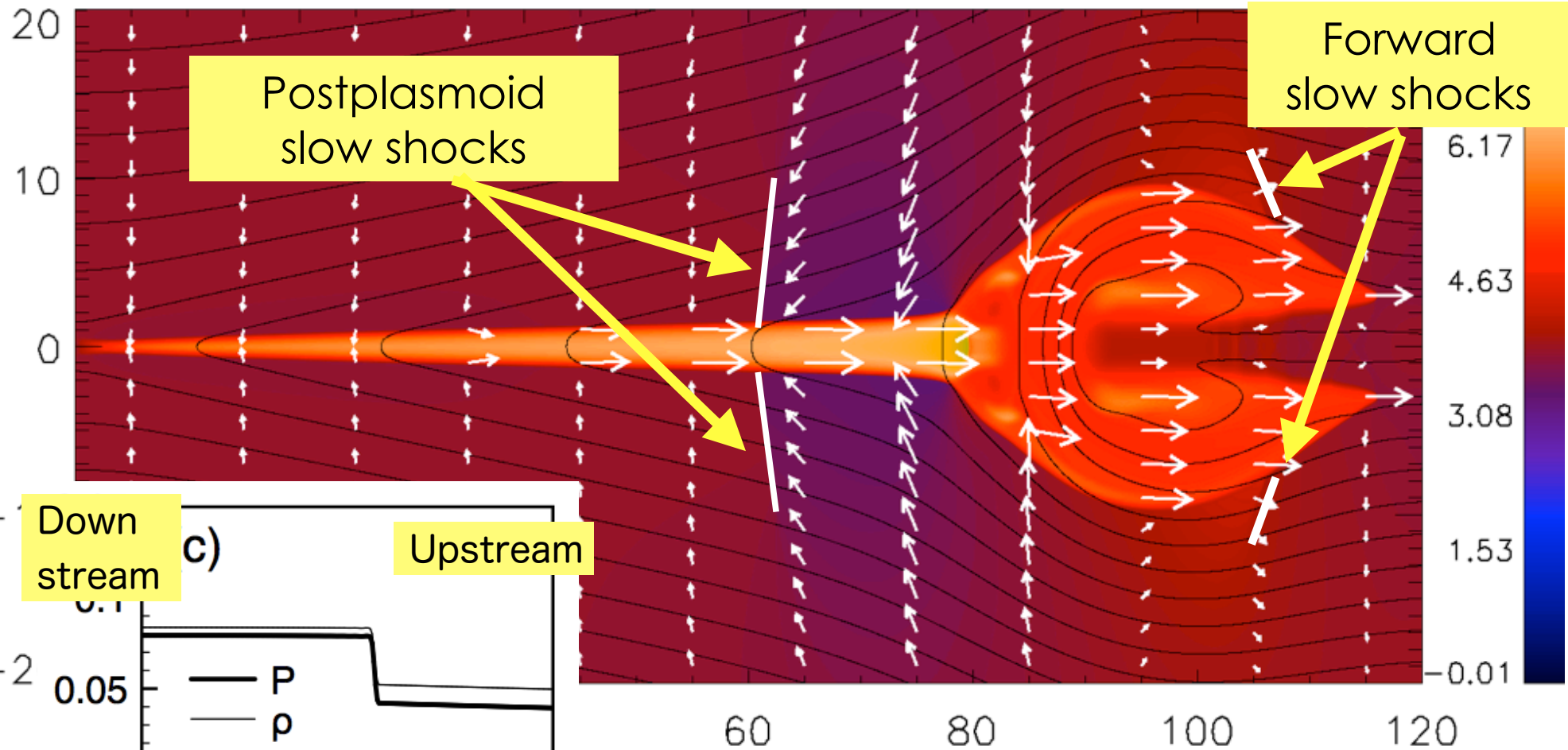




# High-speed fluid effects (2/3): normal shocks

t = 195.0

$u_x$



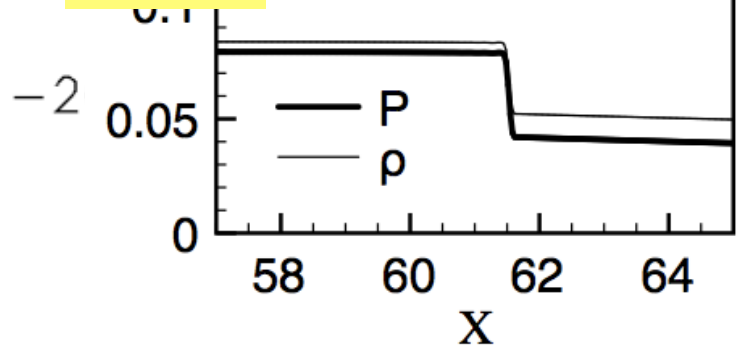
Postplasmoid  
slow shocks

Forward  
slow shocks

Down  
stream

Upstream

c)



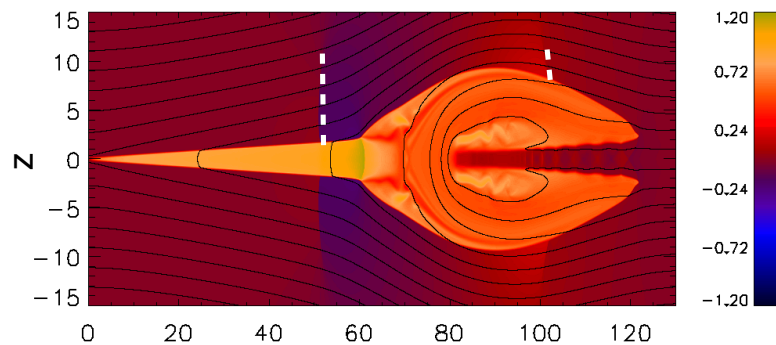
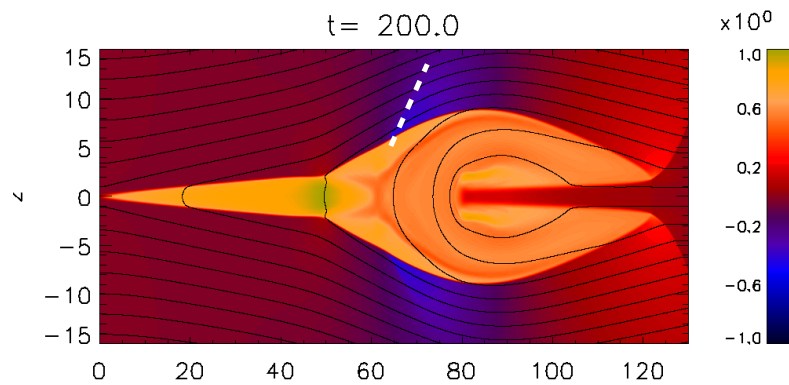
# Normal shock (Recompression shock)

- Magnetic island = Airfoil

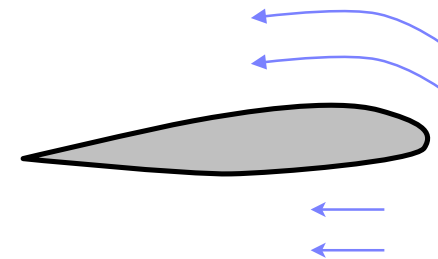
$$v_{jet} \approx c_A$$



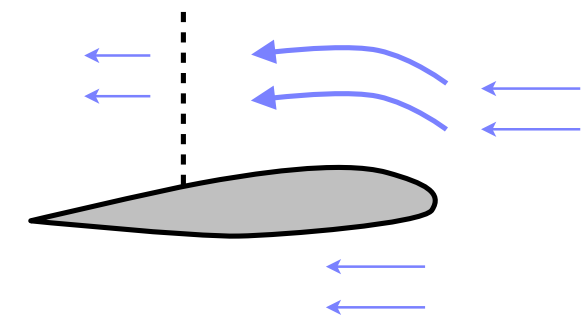
$t = 200.0$



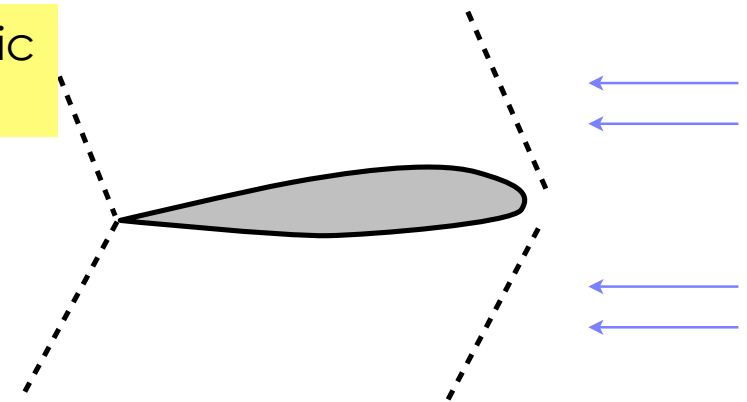
Subsonic  
( $V \ll c_s$ )



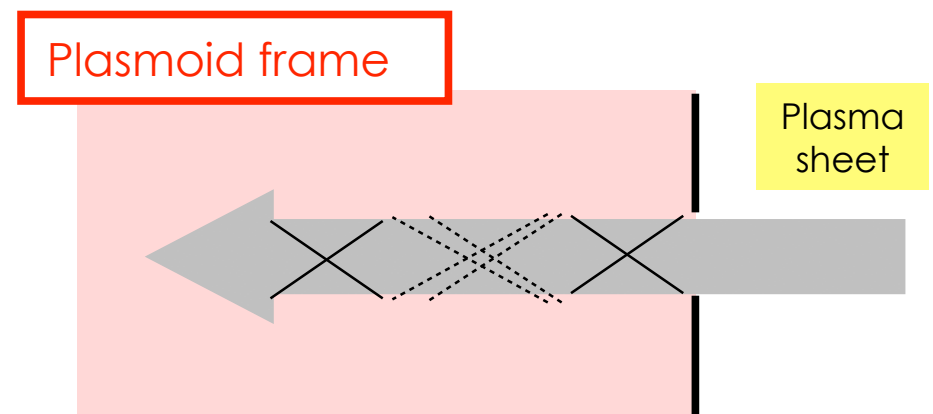
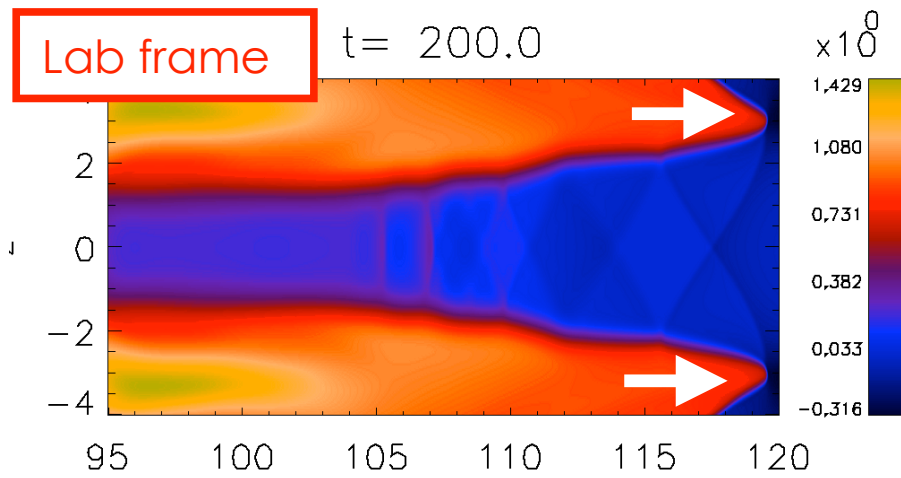
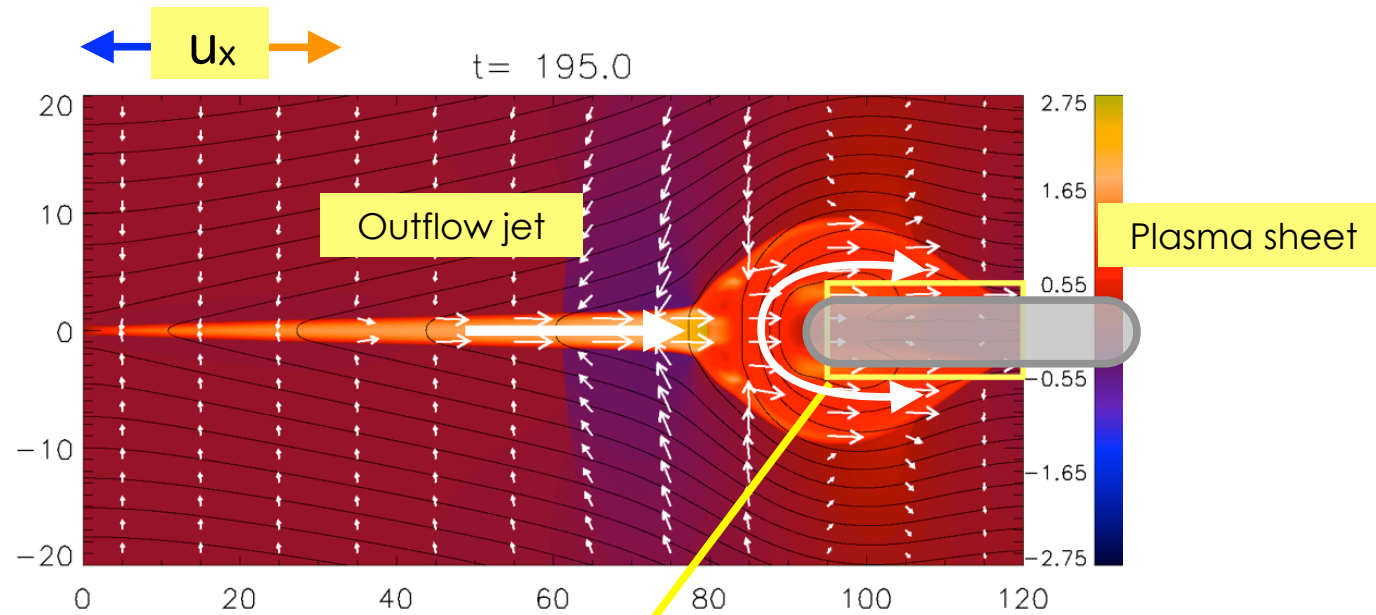
Transonic  
( $0.8c_s < V$ )



Supersonic  
( $c_s < V$ )



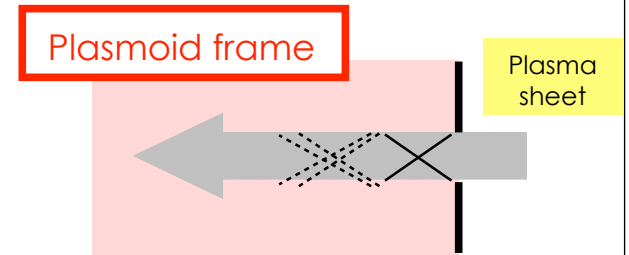
# Compressible effects (3/3): Shock diamond



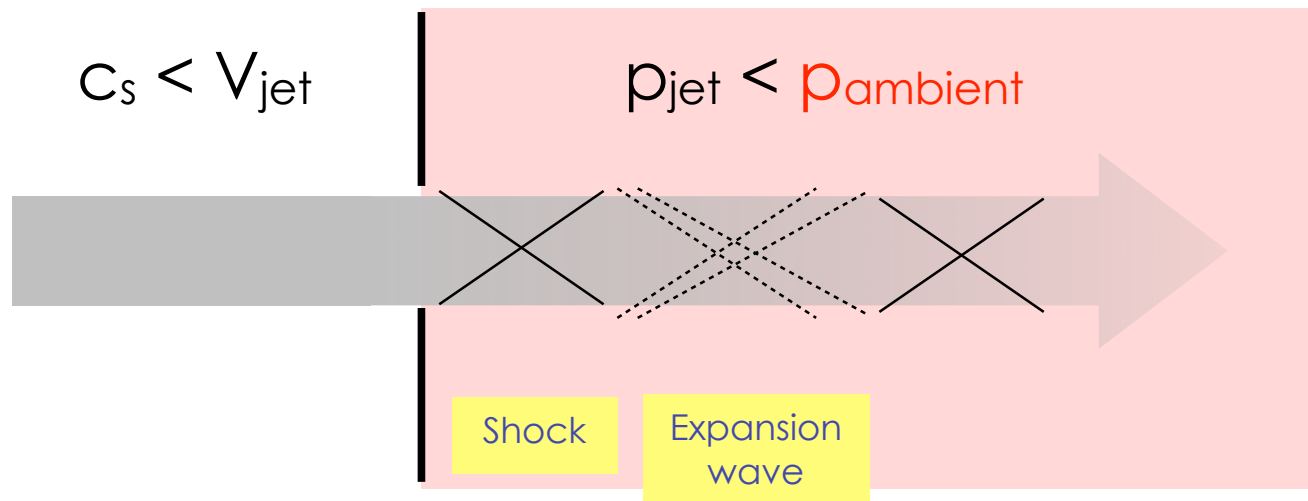
$U_x$

$v_{jet} \approx c_A > c_s$

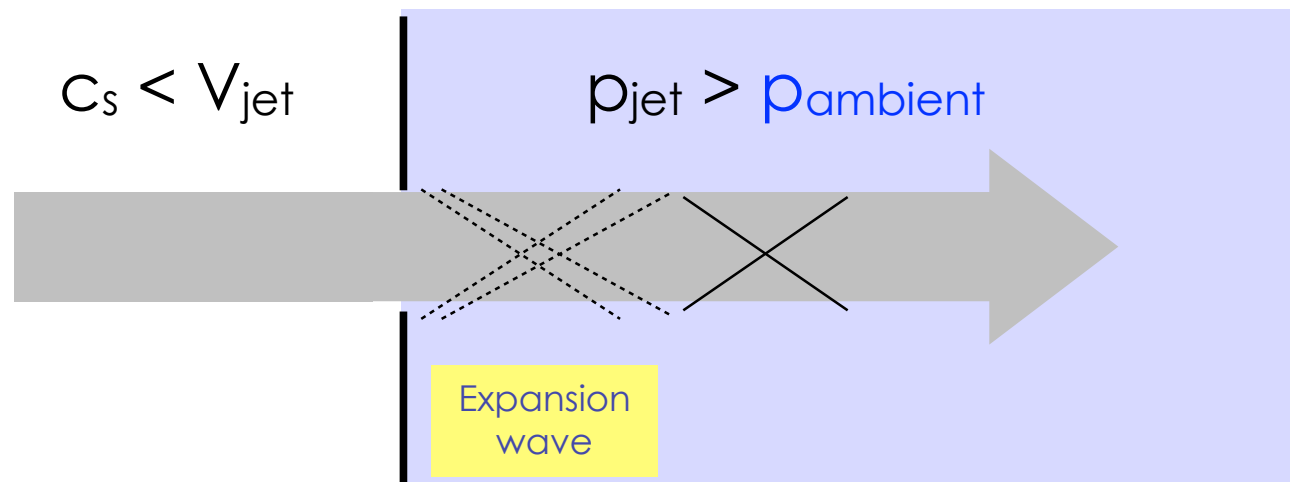
# Shock diamond



- (a) Over-expanded flow

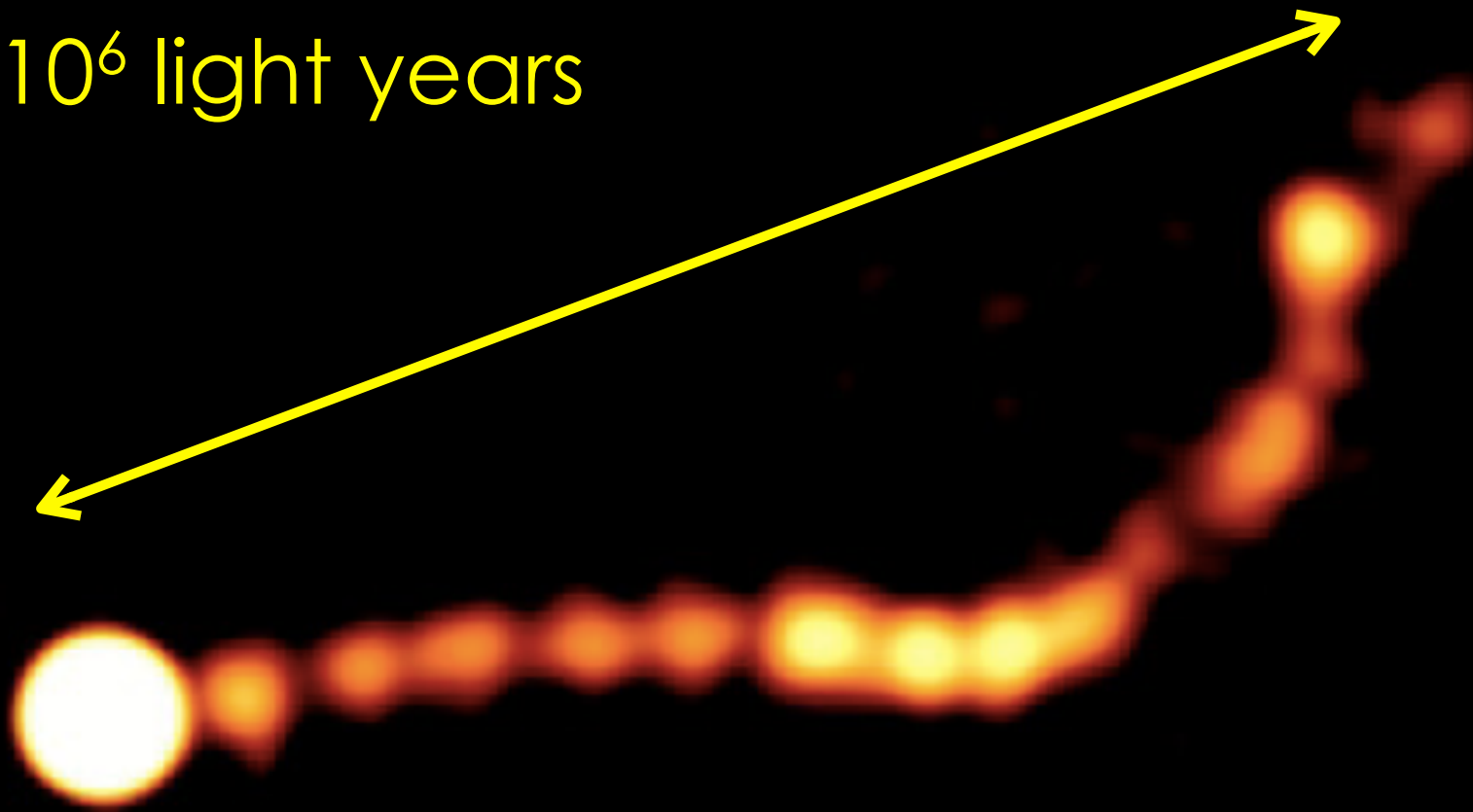


- (b) Under-expanded flow



# Shock diamonds in an extragalactic jet

$2 \times 10^6$  light years



PKS 0637-752 Godfrey+ 2012

# Shock diamonds in aeronautics

BBC



# Shock diamonds in video game

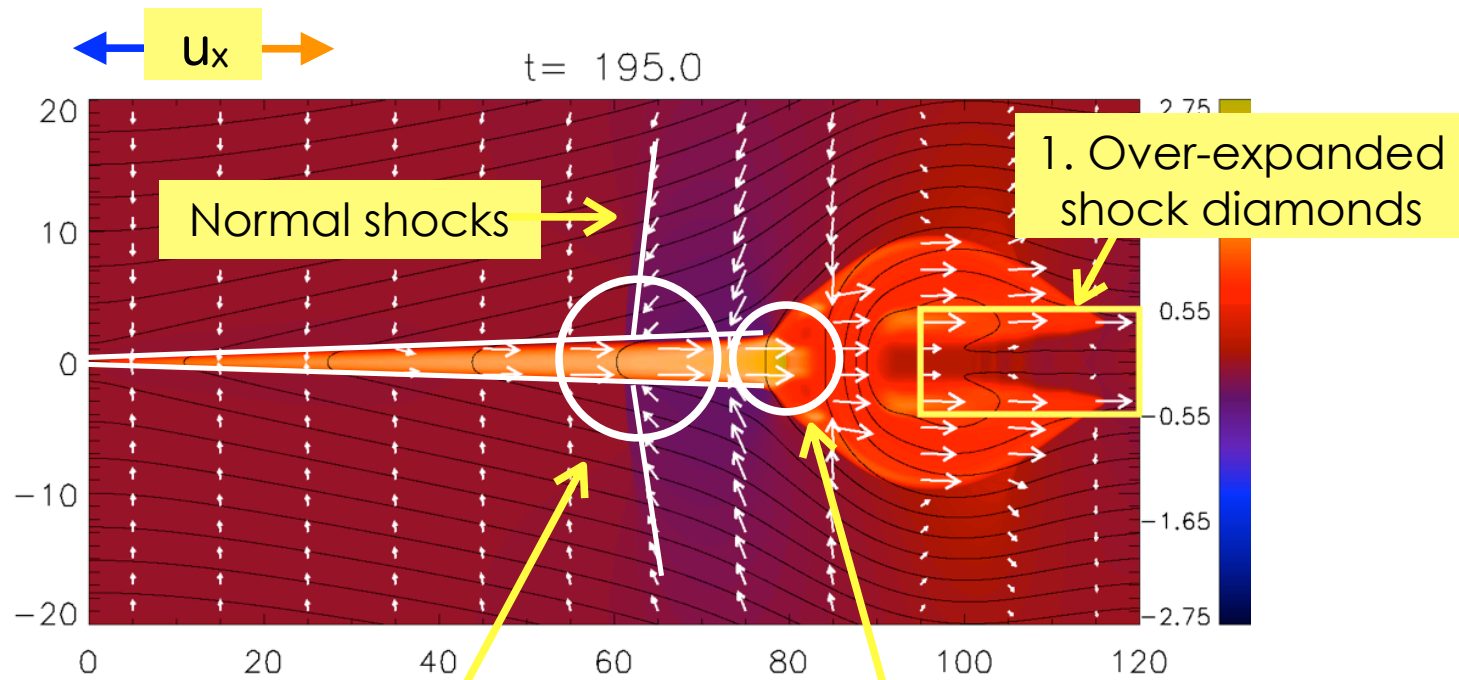


Microsoft Flight Simulator X

<https://www.youtube.com/watch?v=S8QGaiE4yWc>

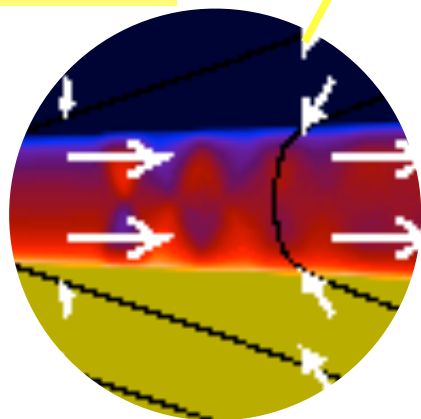


# Some more shock-diamonds

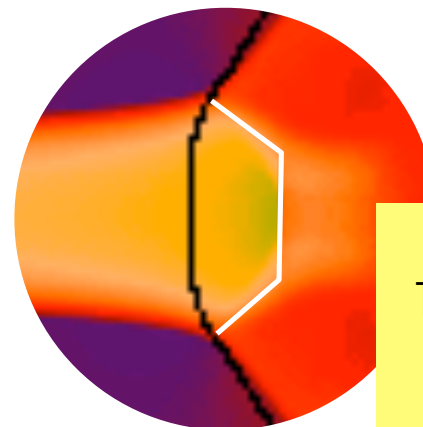
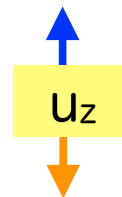


2. Under-expanded shock diamonds

$$\sigma_\epsilon > 3$$



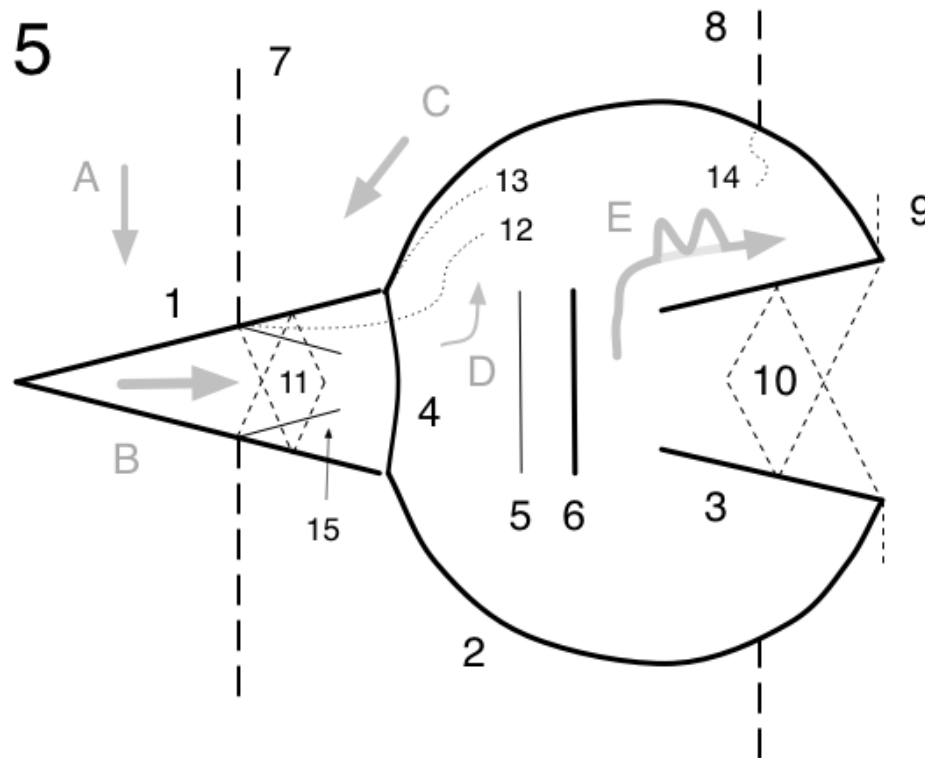
$\pm 1.5\%$



3. Mach disk  
This may evolve to over-expanded shock diamonds

# Structure of a reconnection-plasmoid system

2015



- High-speed effects were also missing in nonrelativistic reconnection industry
- They result in complex shock structure in a low- $\beta$  plasma

$$\beta = \frac{2}{\Gamma} \left( \frac{c_s}{c_A} \right)^2 \sim \left( \frac{c_s}{V} \right)^2 = \mathcal{M}^{-2}$$

1. Petschek slow shock (Petschek 1964)
2. outer shell = slow shock (Ugai 1995)
3. intermediate shock (Abe & Hoshino 2001) or slow shock (Saito et al. 1995)
4. fast shock (Forbes & Priest 1983)
5. looptop front (Ugai 1987)
6. tangential discontinuity
7. post-plasmoid vertical slow shock (Zenitani et al. 2010)
8. outer vertical slow shock (Zenitani & Miyoshi 2011)
9. fast-mode wave front (Saito et al. 1995)
10. overexpanded shock-diamonds (Zenitani et al. 2010)
11. underexpanded shock-diamonds (Zenitani 2015)
12. contact discontinuity (Zenitani & Miyoshi 2011, 2015)
13. contact discontinuity (Zenitani 2015)
14. contact discontinuity (Zenitani 2015)
15. slow expansion wave front (Zenitani 2015)

- A. reconnection inflow
- B. outflow jet
- C. post-plasmoid reverse flow
- D. internal flow
- E. flapping jet (KH instability)

Zenitani & Miyoshi 2011  
Zenitani 2015a

preliminary

# 3. Cross-code comparison

# Relativistic kinetic Ohm's law

- MHD simulation relies on pre-defined Ohm's law
- What about self-consistent PIC results?

- Stress-energy tensor

$$W^{\alpha\beta} = \int f(\mathbf{u}) u^\alpha u^\beta \frac{d^3u}{\gamma}$$

$w^\alpha$  : heat flow

- Standard decomposition

$$W^{\alpha\beta} = w u^\alpha u^\beta + w^\alpha u^\beta + w^\beta u^\alpha + w^{\alpha\beta}$$

$$Q^{\alpha\beta} \equiv w^\alpha u^\beta + w^\beta u^\alpha$$

- Ohm's law ( $\partial_t=0$ )

$$\mathbf{E} + \frac{\mathbf{v}}{c} \times \mathbf{B} = \frac{1}{\gamma n q} \nabla \cdot (w u^i u^j + Q^{ij} + P^{ij})$$

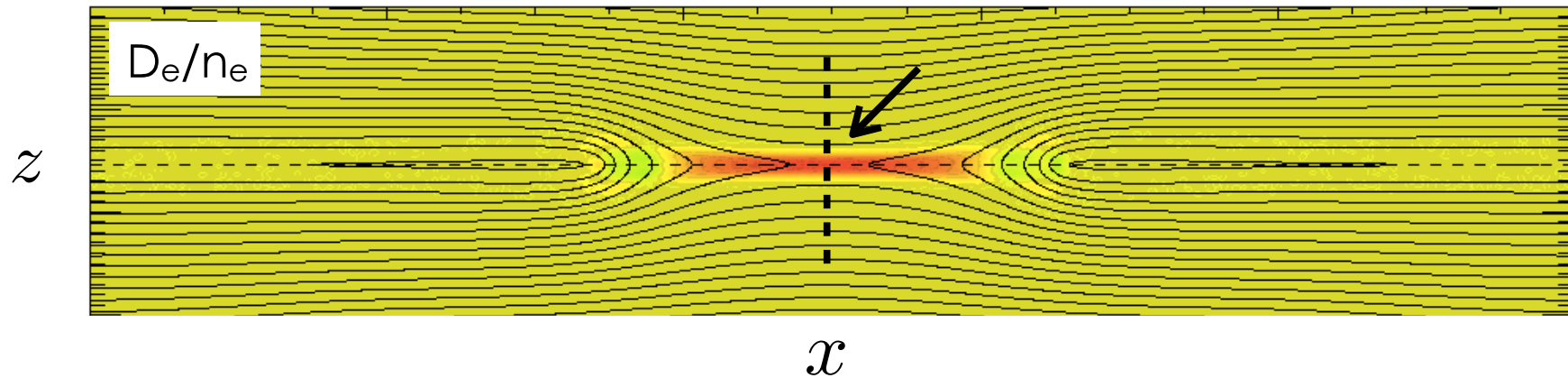
Heat flow term  
(Only in relativistic kinetic plasma)

Bulk term  
(incl. relativistic pressure)

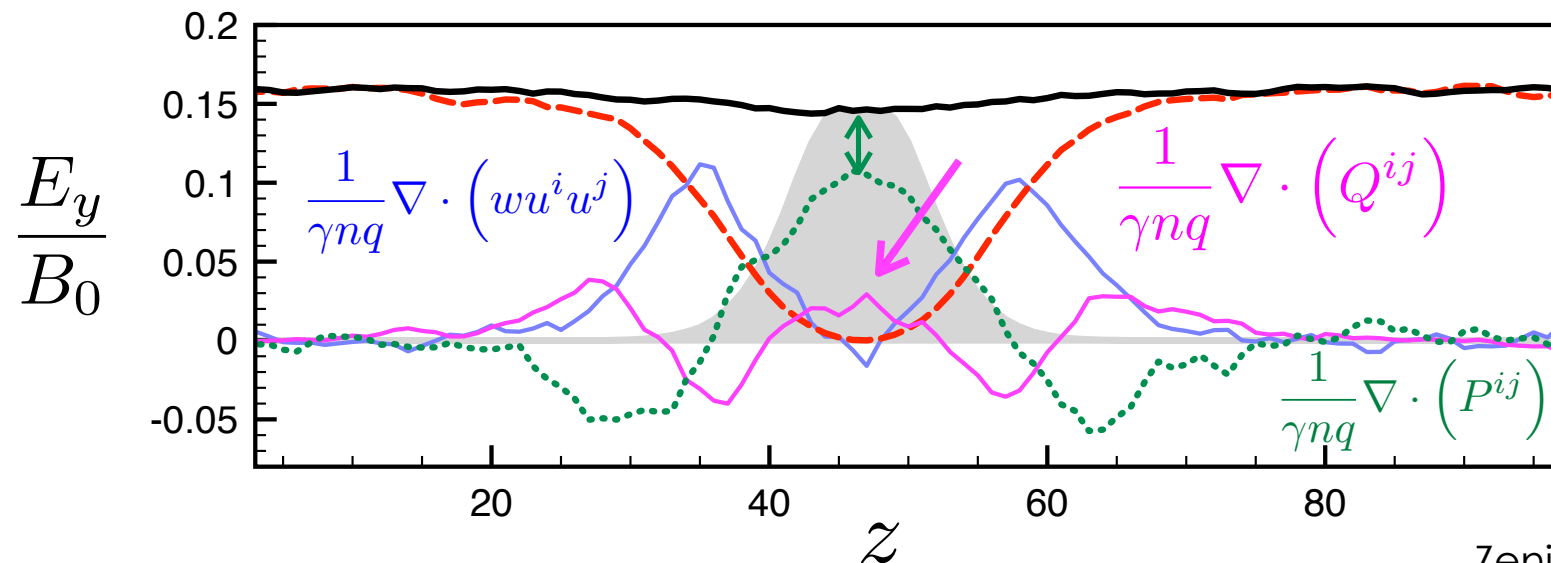
Local momentum transport  
(Incl. kinetic div.P term)

# Kinetic Ohm's law (cont.)

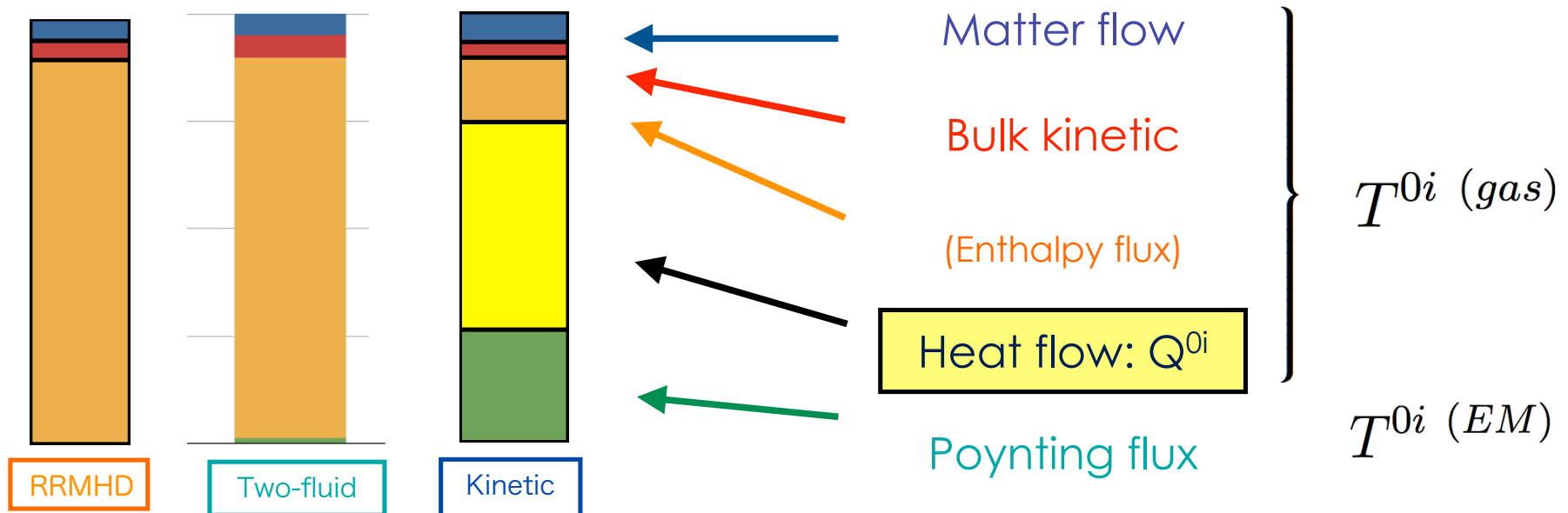
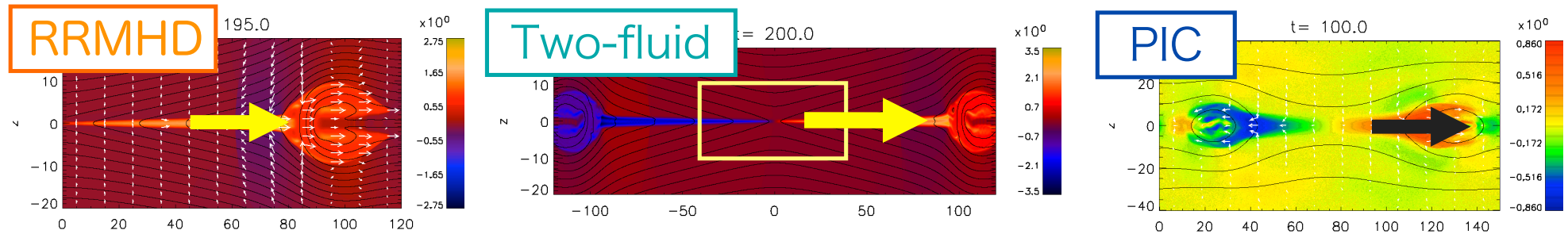
- Normalized energy dissipation ( $\sim j \cdot E/n \sim \eta j^2/n$ )



- Ohm's law: relativistic heat flow term appears



# PIC vs Two-fluid vs RRMHD - energy throughput



- Kinetic term (heat flow) appears to be important

# Summary

- Kinetic modeling
  - Reconnection features DC particle acceleration
  - 3D evolution - a kink instability
  - Now it is a field of active research!!
- RRMHD, Two-fluid modeling
  - Straightforward extension of nonrelativistic MHD reconnection
  - Narrower exhaust, faster reconnection rate, heat-dominated flow
  - High-speed fluid effects - adiabatic acc., shocks, shock diamonds
- Cross-code comparison
  - Heat flow appears in the Ohm's law and dominates in the energy budget (due to accelerated particles)