

# PIC Simulations of relativistic transverse magnetosonic shocks

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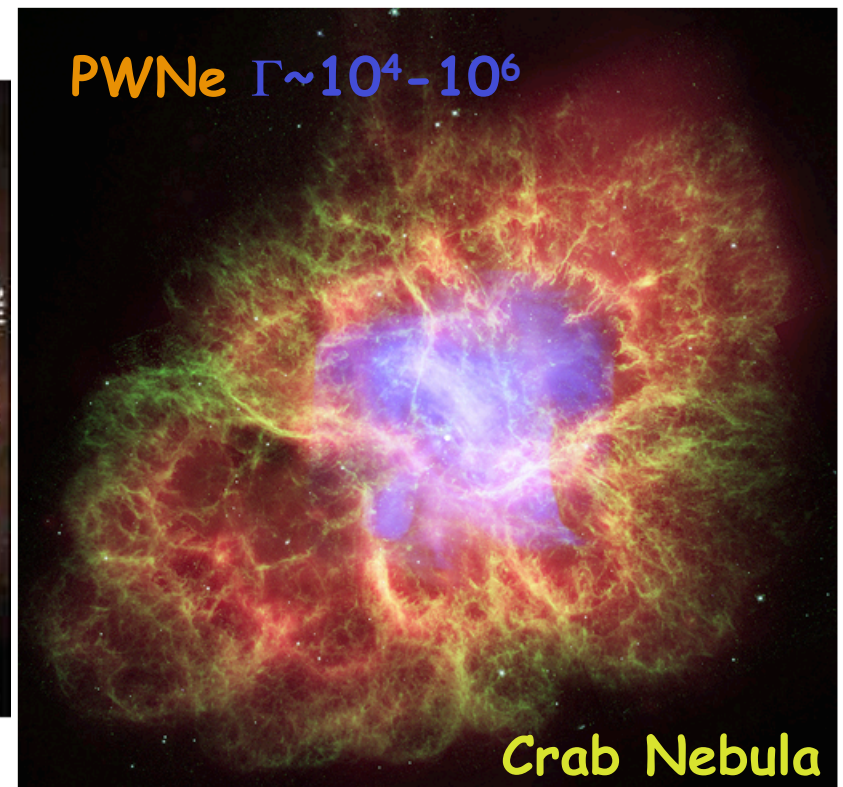
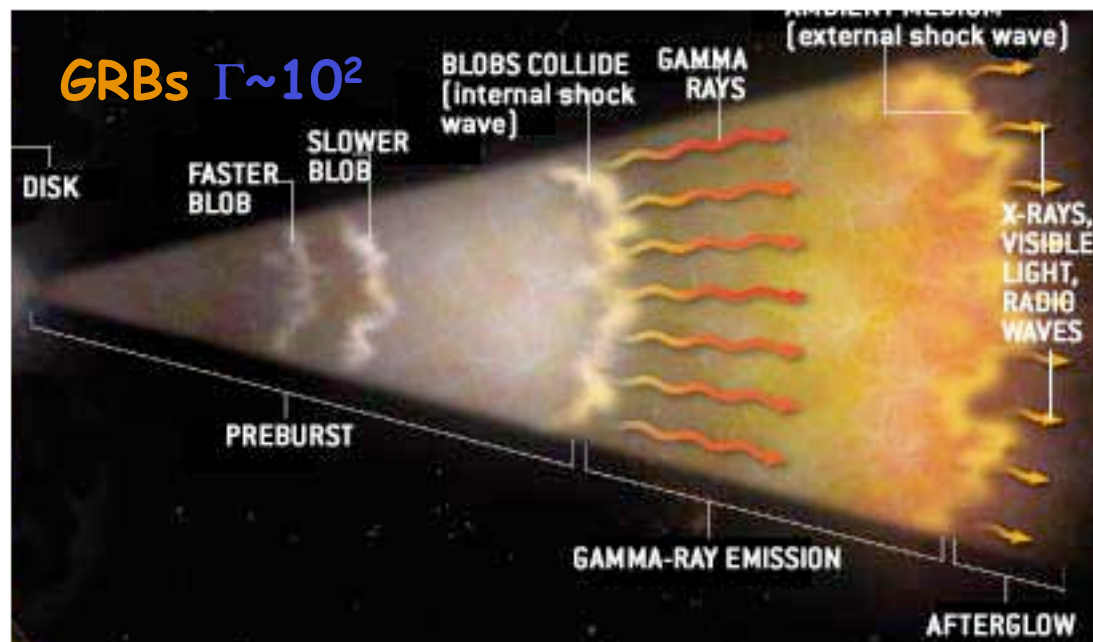
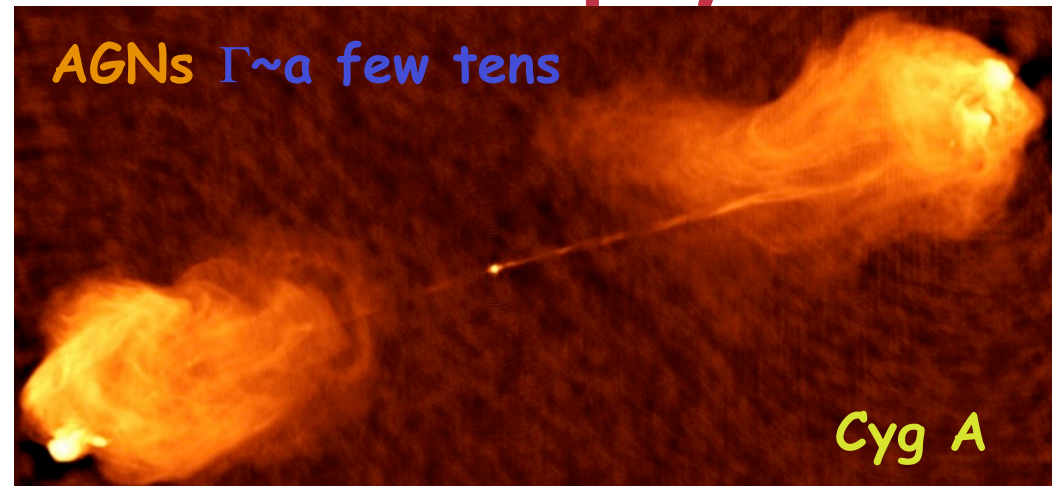
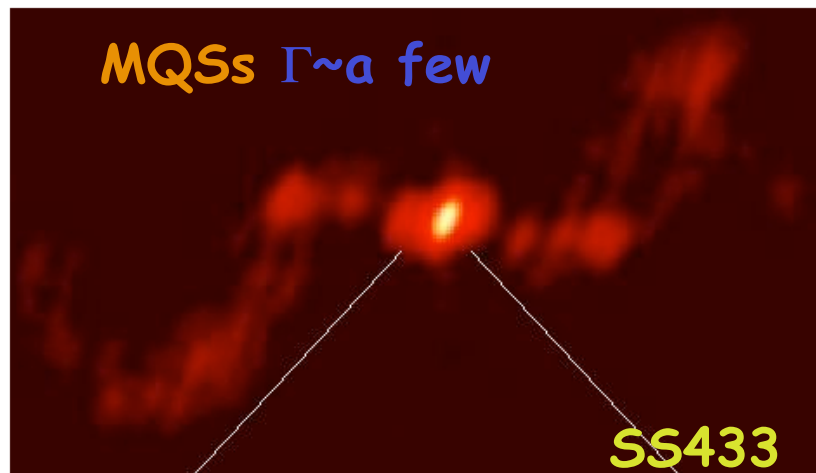
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di Arcetri

In collaboration with Jonathan Arons (Berkeley)

# Outline

- **Astrophysical relevance of the subject**
- **PIC simulations of relativistic transverse magnetosonic shocks in  $e^-e^+p$  plasmas**
  - Resonant cyclotron absorption
  - Questions left open by previous work on the subject
  - What can still be learned from 1D PIC
- **Simulations with increased mass-ratio between ions and pairs (up to 100): now outdated**
  - Acceleration mechanism still effective
  - Electron acceleration seen for the first time
  - Effects of finite temperature of the plasma
- **Summary and Conclusions**

# Relativistic shocks in astrophysics



# Properties of the flow and particle acceleration

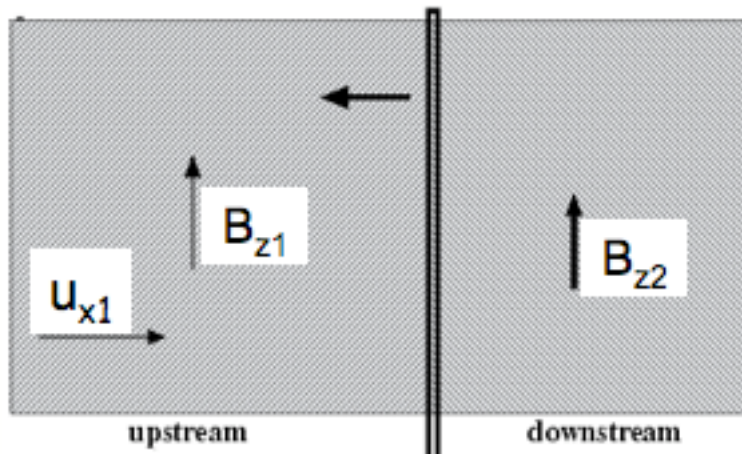
- **These shocks are collisionless**: transition between non-radiative (upstream) and radiative (downstream) takes place on scales too small for collisions to play a role
- They are generally associated with **non-thermal particle acceleration** but **with a variety of spectra and acceleration efficiencies**

**Self-generated electromagnetic turbulence** mediates the shock transition: it must provide both the **dissipation** and **particle acceleration** mechanism

The detailed physics and the outcome of the process strongly depend on  
**composition** ( $e^-e^+p?$ )  
**magnetization** ( $\sigma = B^2/4\pi n\Gamma mc^2$ )  
and **geometry** ( $\Gamma \times \Theta(B \cdot n)$ )  
of the flow, which are usually unknown....

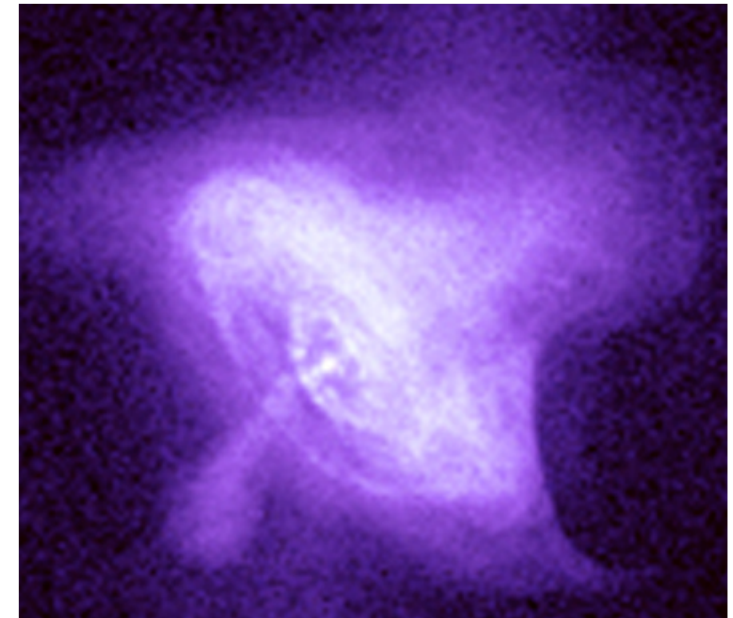


# Relativistic transverse magnetosonic shocks



shocks

$\Theta(\mathbf{B} \cdot \mathbf{n}) \gg 1/\Gamma$   
**Geometry**  
Common for  
Magnetized  
Relativistic  
shocks



Magnetized relativistic shocks in **PWNe**  
accelerate particles very efficiently!!!

Look at the **Crab Nebula**:  
✓ Efficiency  $> 20\%$  of total  $L_{sd}$   
✓ Maximum energy: for Crab  $\sim \text{few} \times 10^{15}$  eV  
(close to total available  $\Delta V$  at the PSR)

3D PIC of **magnetized pair shocks** hint at **low efficiency**  
(Spitkovsky 08)

**Magnetic reconnection ?**

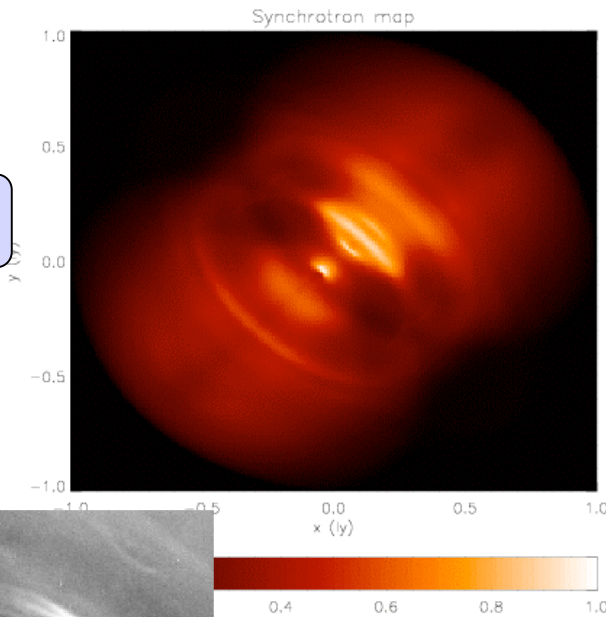
**Or maybe ions?**

- unmagnetized shock: efficient Fermi I (Spitkovsky 08)
- acceleration associated to reconnection (Lyubarsky & Petri 07)

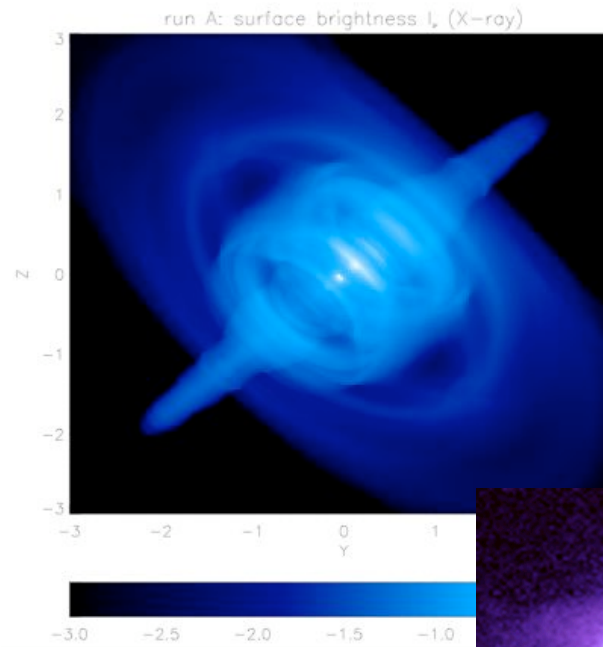
**Resonant cyclotron absorption**

# Synchrotron Emission maps from 2D MHD simulations of PWNe

optical

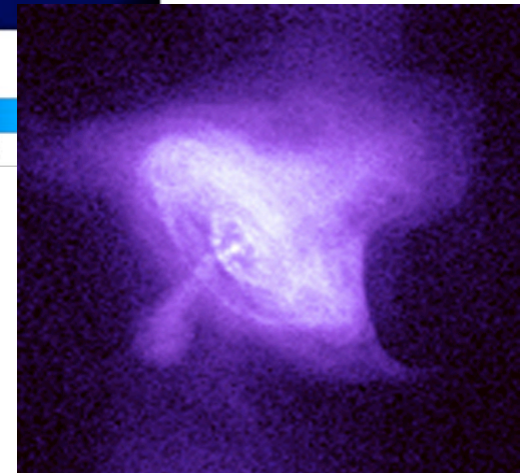
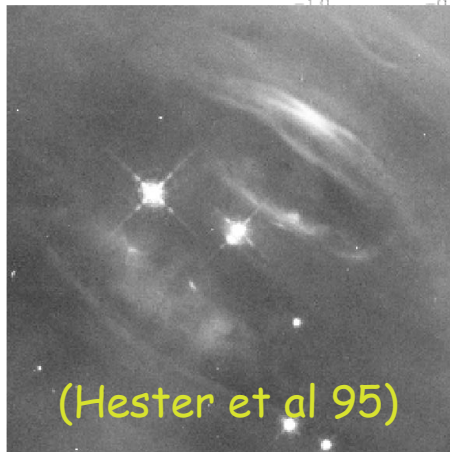


X-rays



$$\sigma=0.025, b=10$$

(Del Zanna et al. 06)



# Particle In Cell Simulations

## The method:

- ✓ Collect the current at the cell edges
- ✓ Solve Maxwell's eqs. for fields on the mesh
- ✓ Compute fields at particle positions
- ✓ Advance particles under e.m. force

## Approximations

In principle only cloud in cell algorithm

Powerful investigation tool for collisionless plasma physics: allowing to resolve the kinetic structure of the flow on all scales

## But Computational limitations force:

Reduced spatial and time extent

Mistaken transients

Far-from-realistic values of the parameters

An example of the effects of reduced  $m_i/m_e$  in the following

reduced dimensionality of the problem

$e^- - e^+$  plasma flow:

▪ in 1D:

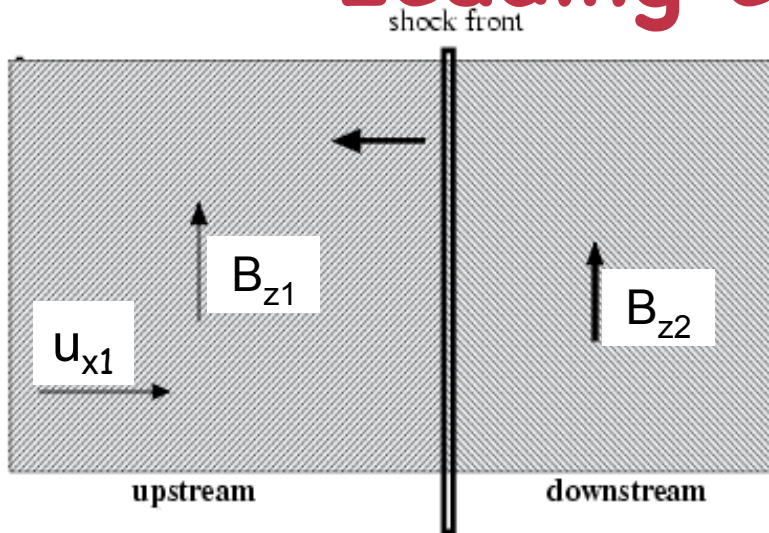
- No shock if  $\sigma=0$
- No accel. for any  $\sigma$

▪ in 3D

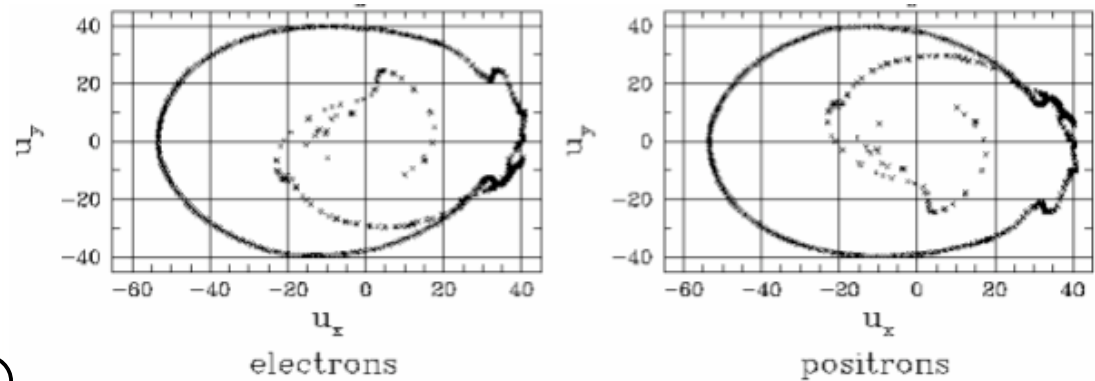
- Shock for any  $\sigma$
- Fermi accel. for  $\sigma=0$

For some aspects of problems involving species with different masses 1D WAS still the only way to go

# Leading edge of the shock



Configuration at the leading edge  
~ cold ring in momentum space

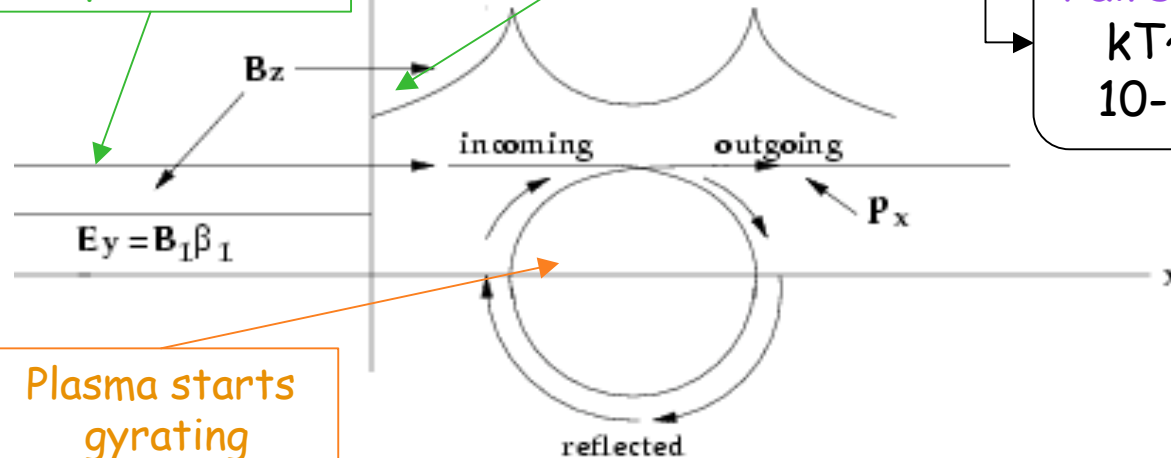


Magnetic reflection mediates the transition

Coherent gyration leads to collective emission of cyclotron waves

Drifting  $e^+e^-p$  plasma

$B$  increases



Plasma starts gyrating

Pairs thermalize to  $kT \sim m_e \Gamma c^2$  over  $10-100 \times (1/\Omega_{ce})$

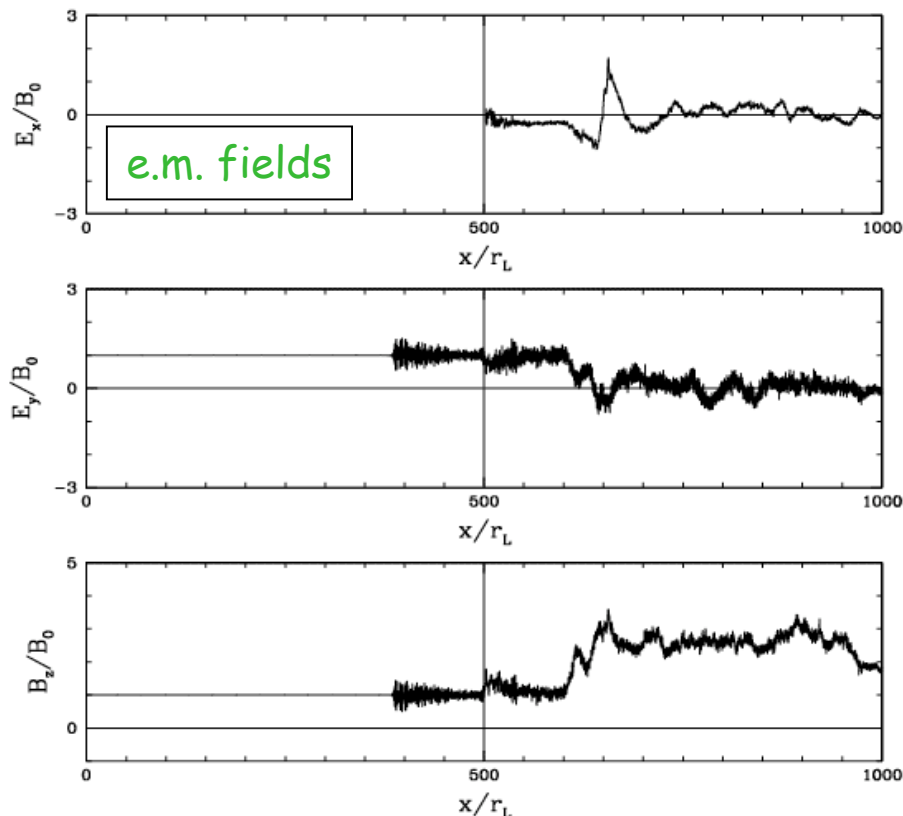
Ions take their time:  $m_i/m_e$  times longer

Pairs can absorb ion radiation resonantly

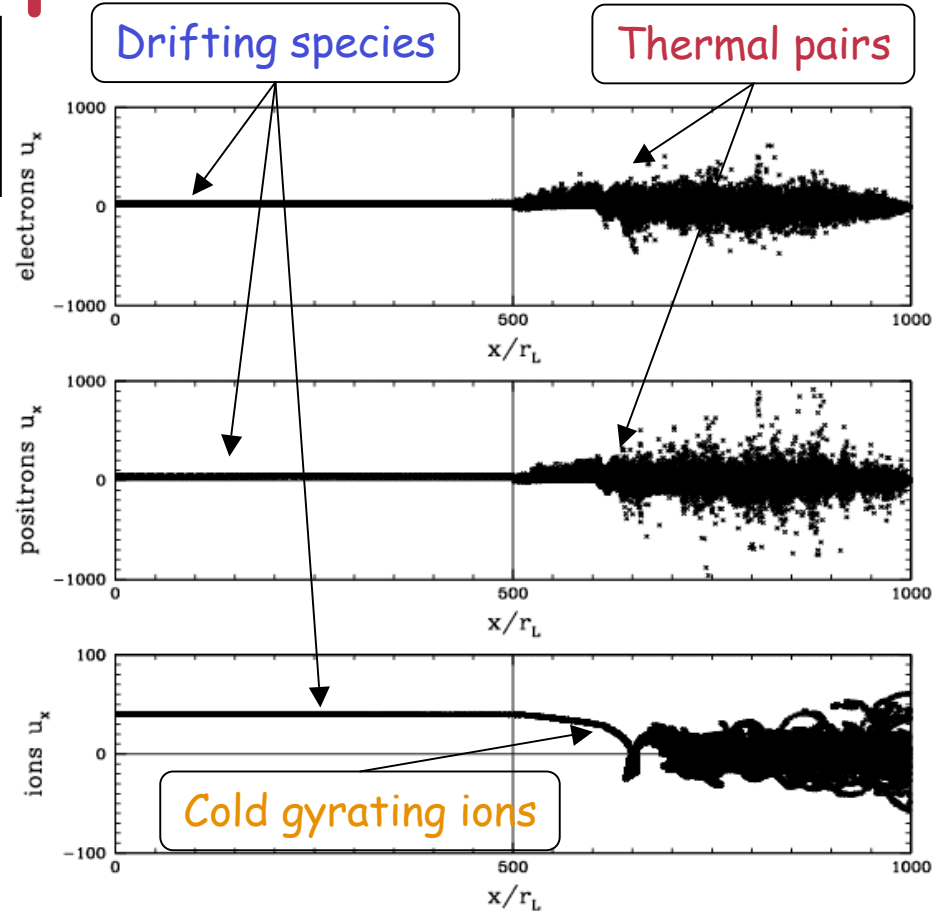


# 1D PIC Simulations of shocks in $e^- - e^+ - p$ plasmas

From 1D PIC with  $m_i/m_e=100$   
(Amato & Arons 06)  
Using XOOPIC (Verboncoeur et al. 95)



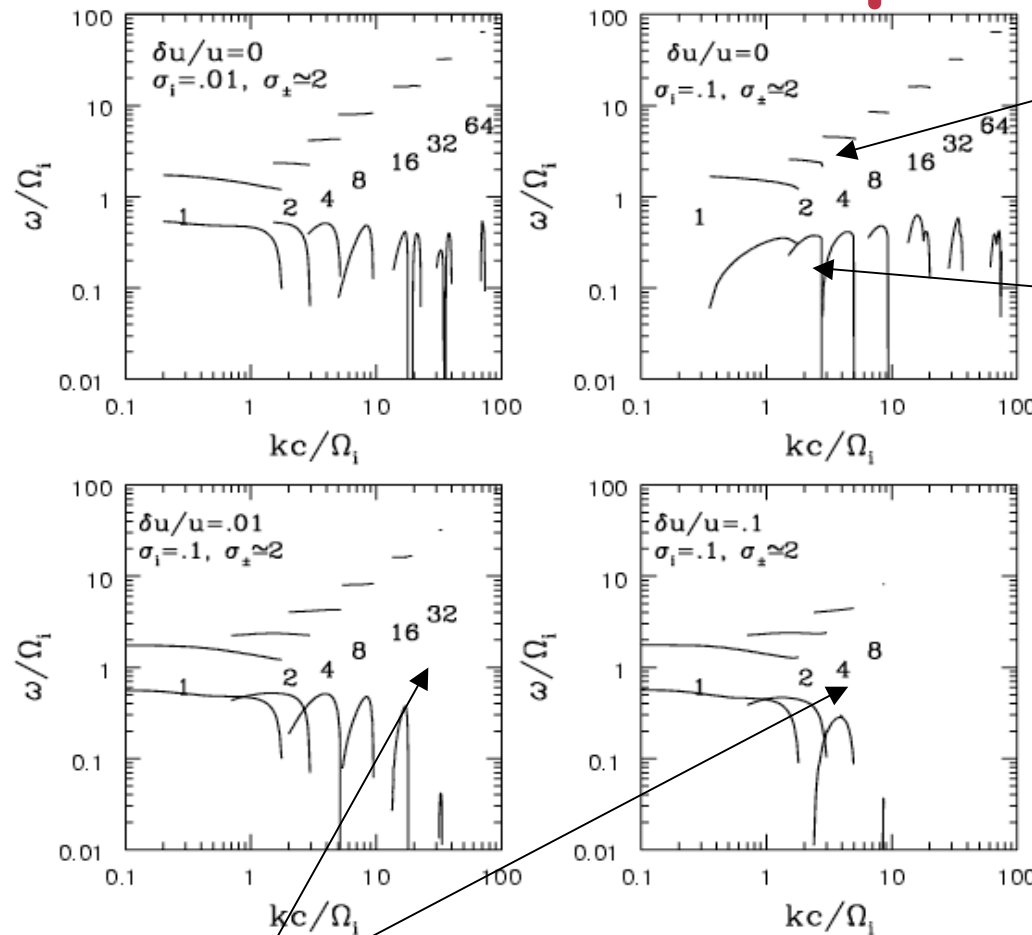
- Particles enter simulation box from left
- Impact on a wall on the right
- Wait until shock far from right boundary



1D PIC sim. with  $m_i/m_e$  up to 20  
(Hoshino & Arons 91, Hoshino et al. 92)  
 $e^+$  effectively accelerated  
if  $U_i/U_{tot} > 0.5$

# Resonant cyclotron absorption in ion-doped plasma

$$\Omega_{ci} = m_e/m_i \Omega_{ce}$$



frequency

Growth-rate

Pairs **initially** need  $n \sim m_i/m_e$  for resonant absorption!!!  
Then lower  $n$

Growth-rate  $\sim$  independent of  $n$   
(Hoshino & Arons 91)

$m_i/m_e$  much lower than reality  
implies  $n_i/n_e$  correspondingly  
larger to guarantee sufficiently  
large  $U_i/U_{tot}$

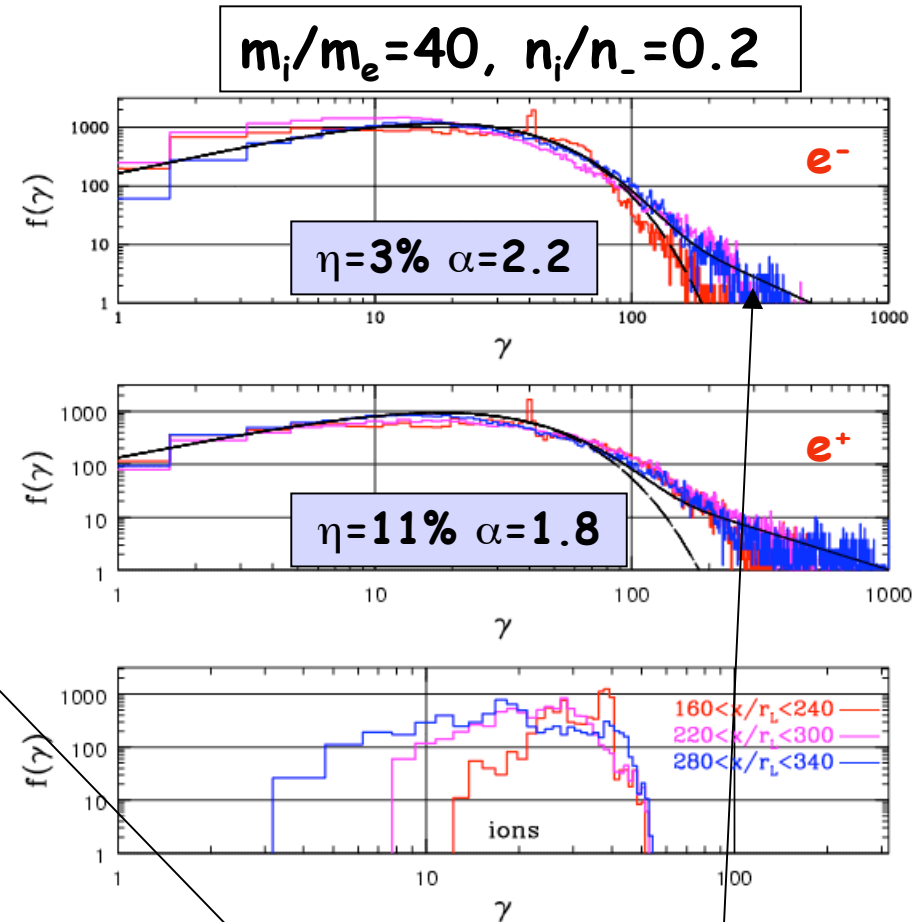
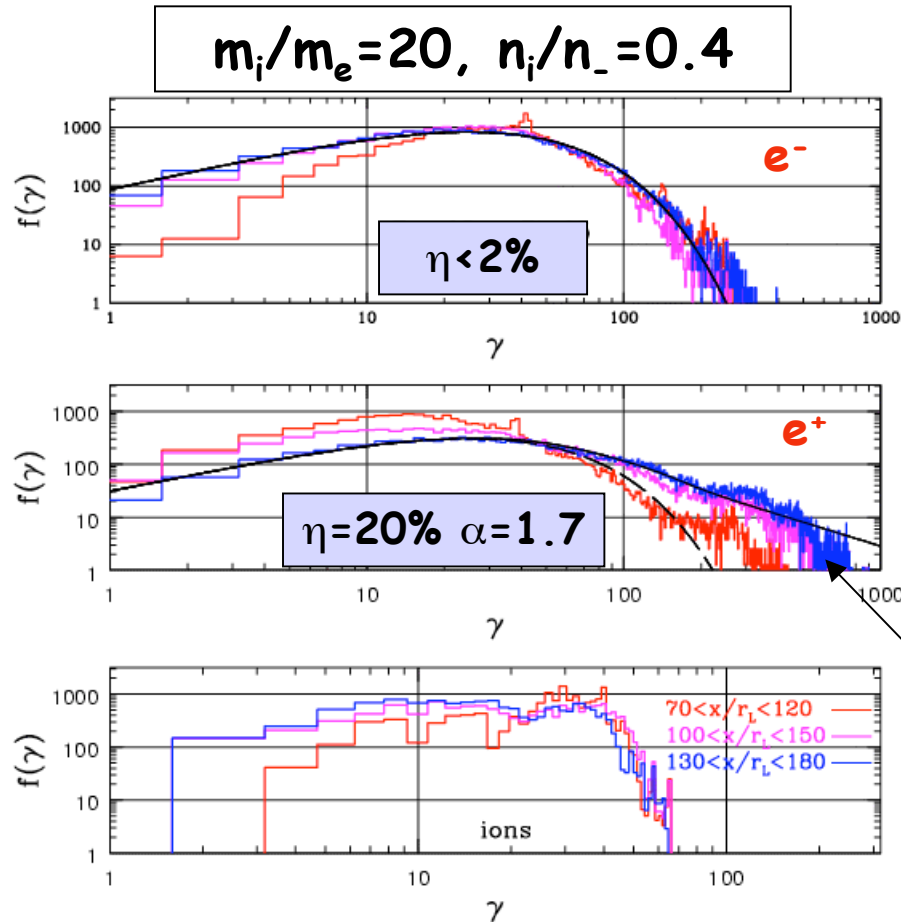
Elliptical polarization of ion waves

Spectrum is cut  
off at  $n \sim u/\delta u$

growth-rate  $\sim$  independent of  $n$   
if plasma cold (Amato & Arons 06)

Preferential  
absorption by  $e^+$

# Polarization of the waves



Upstream flow:  
 Lorentz factor:  $\Gamma=40$   
 Magnetization:  $\sigma_{\pm}=2$

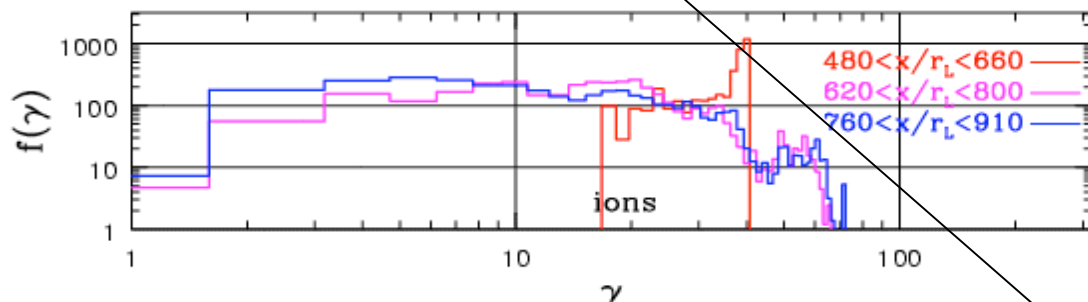
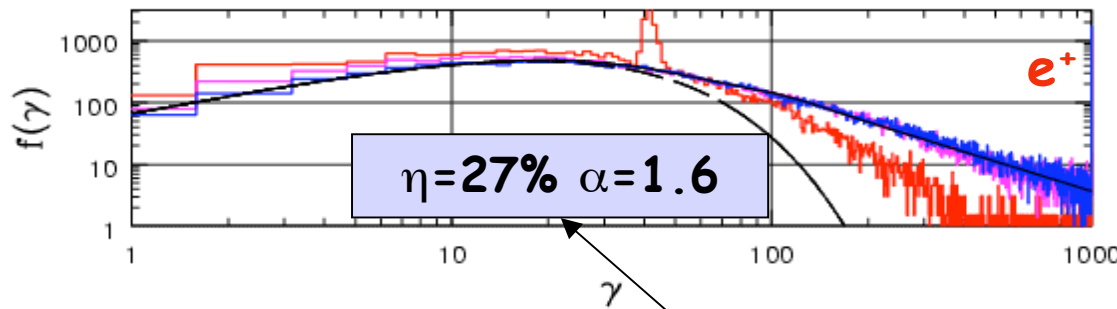
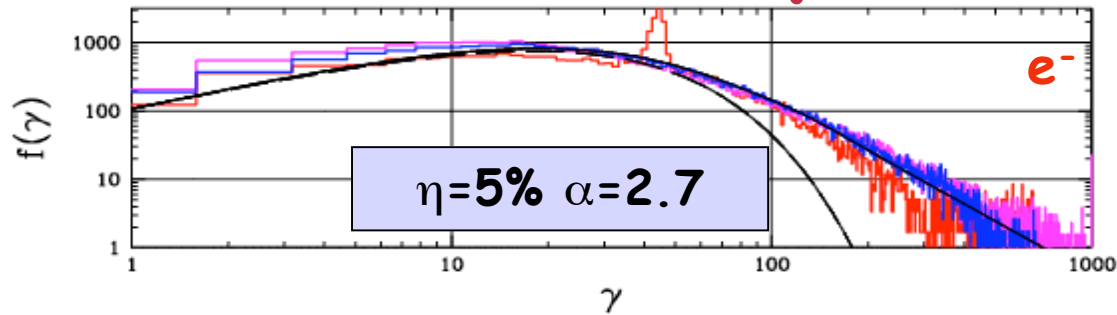
Simulation box:  
 $\Delta x = r_{Le}/10$   
 $Lx = r_{Li} \times 10$

$U_i/U_{tot}=0.7$  same in both simulations

Positron tail  
 extends to  
 $\gamma_{max} = m_i/m_e \Gamma$

First evidence  
 of electron  
 acceleration

# Particle spectra and acceleration efficiency for $m_i/m_e=100$



Upstream flow:  
Lorentz factor:  $\Gamma=40$   
Magnetization:  $\sigma_{\pm}=2$

Simulation box:  
 $\Delta x = r_{Le}/10$   
 $Lx = r_{Li} \times 10$

$n_i/n_e=0.2$   
 $U_i/U_{tot}=0.8$

Acceleration efficiency:

$\sim \text{few}\%$  for  $U_i/U_{tot} \sim 60\%$   
 $\sim 30\%$  for  $U_i/U_{tot} \sim 80\%$

Spectral slope:

$>3$  for  $U_i/U_{tot} \sim 60\%$   
 $<2$  for  $U_i/U_{tot} \sim 80\%$

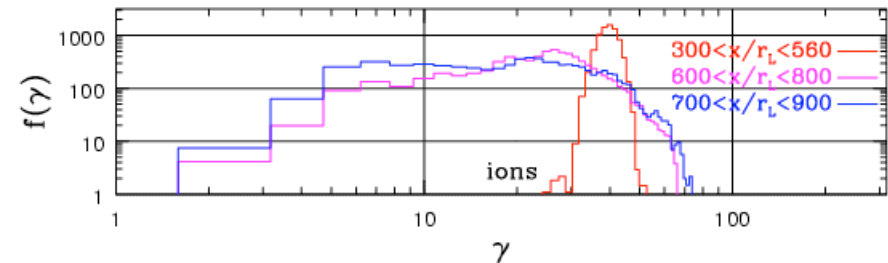
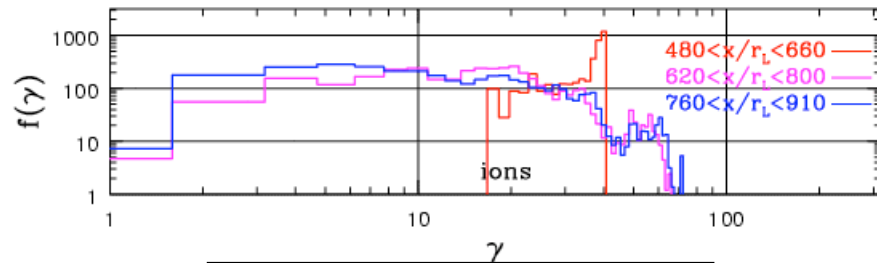
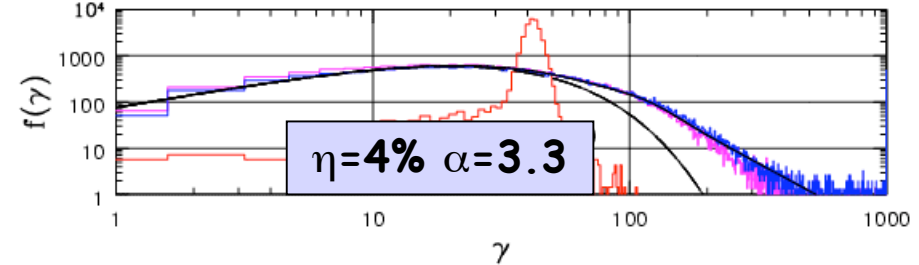
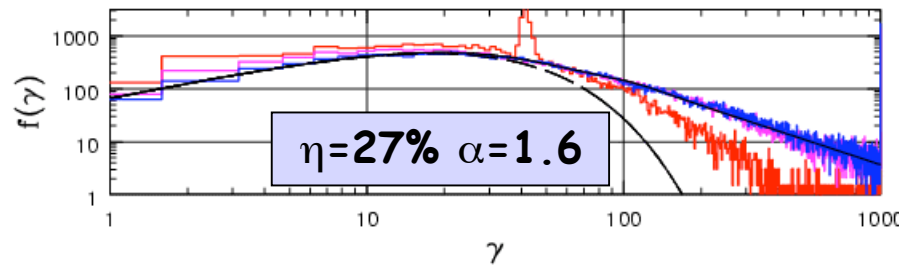
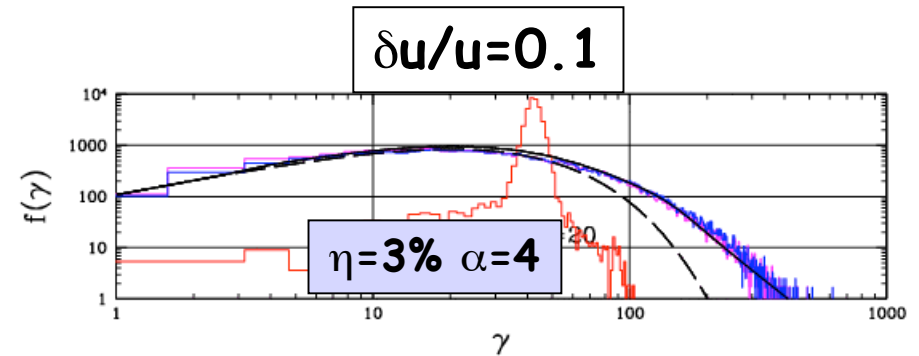
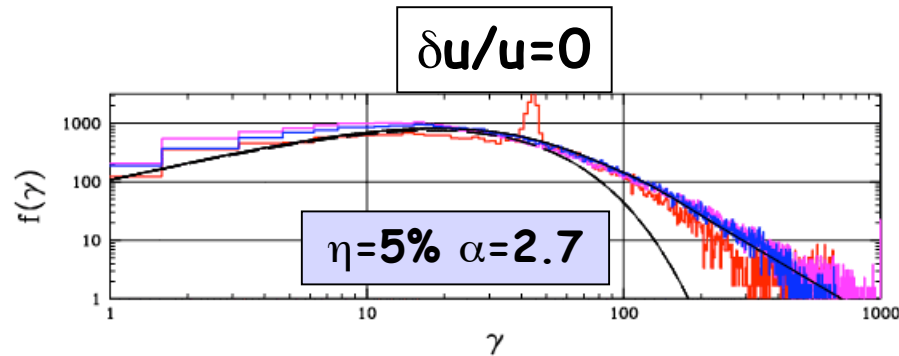
Maximum energy:

$\sim 20\% m_i c^2 \Gamma$  for  $U_i/U_{tot} \sim 60\%$   
 $\sim 80\% m_i c^2 \Gamma$  for  $U_i/U_{tot} \sim 80\%$

Mechanism still works at  
large  $m_i/m_e$   
for both  $e^+$  and  $e^-$



# Effects of thermal spread



$n_i/n_- = 0.2 \quad m_i/m_e = 100$   
 $U_i/U_{\text{tot}} = 0.8$

Initial particle distribution  
function is a gaussian of width  $\delta u$

Upstream flow:  
Lorentz factor:  $\Gamma=40$   
Magnetization:  $\sigma_{\pm}=2$

Simulation box:  
 $\Delta x = r_{Le}/10$   
 $Lx = r_{Li} \times 10$

**Acceleration effectively suppressed!!!**

# Summary and Conclusions

We have explored the physics of  
relativistic transverse magnetosonic shocks in ion-doped plasmas  
through 1D PIC simulations: still about the only possibility to explore the  
behaviour of the system for large  $m_i/m_e$

## Aims:

- Checking whether RCA would still provide any particle acceleration
- Checking whether any electron acceleration for larger mass-ratios (upstream plasma closer to quasi-neutrality)

## Results:

- Pairs are efficiently accelerated even for  $m_i/m_e=100$  if  $U_i/U_{\text{tot}} > 0.5$ 
  - Electron acceleration finally seen!!!
- Less efficient than for positrons due to elliptical polarization of the waves (forced by low  $m_i/m_e$  which implies large  $n_i/n_e$  to ensure  $U_i/U_{\text{tot}} > 0.5$ )
- Extrapolation to realistic  $m_i/m_e$  predicts same efficiency for accelerating  $e^+$  and  $e^-$
- Efficiencies and spectra as observed in PWNe can be obtained depending on ion fraction
- The acceleration is effectively suppressed if initial thermal spread larger than  $m_e/m_i$